

# Deriving Pulsar Properties from Multi-Wavelength Observations

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- PWNe are the most numerous class of galactic gamma-ray sources at TeV energies (~40% of known emitters).
- A key question is whether emission from PWNe is purely Inverse Compton, or if there's a hadronic component.
- A key metric that determines if hadrons can escape the pulsar into the PWN is the pair-production multiplicity.

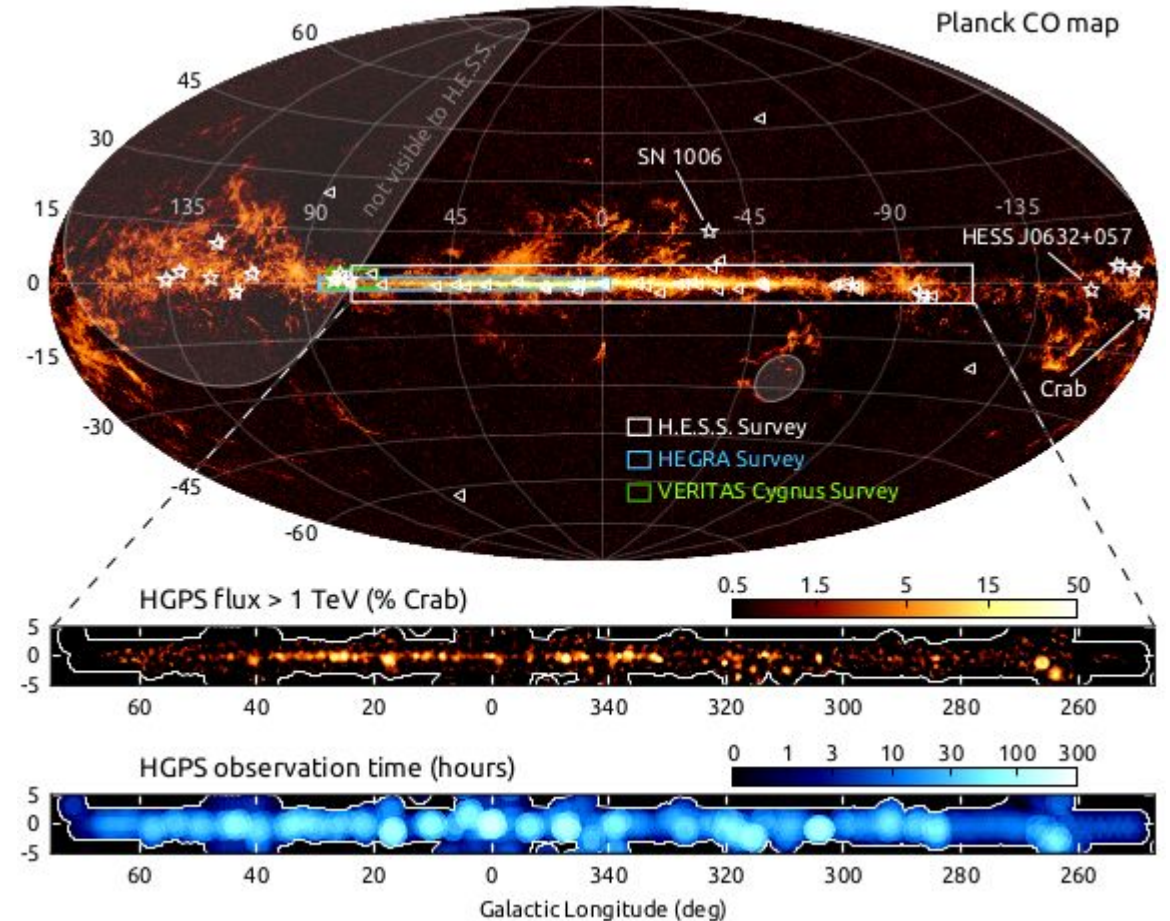


Image Credit: H.E.S.S. Collaboration

- The pair production multiplicity ( $\kappa$ ) describes the number of  $e^+/e^-$  pairs that escape the light cylinder per electron that escapes the pulsar.
- Protons can only make up  $1/\kappa$  particles as they don't multiply in cascades in the pulsar magnetosphere.
- In this project, we aimed to constrain  $\kappa$  for a population of pulsars that have been observed in the TeV and Radio.
- Built on previous work, just more sources.

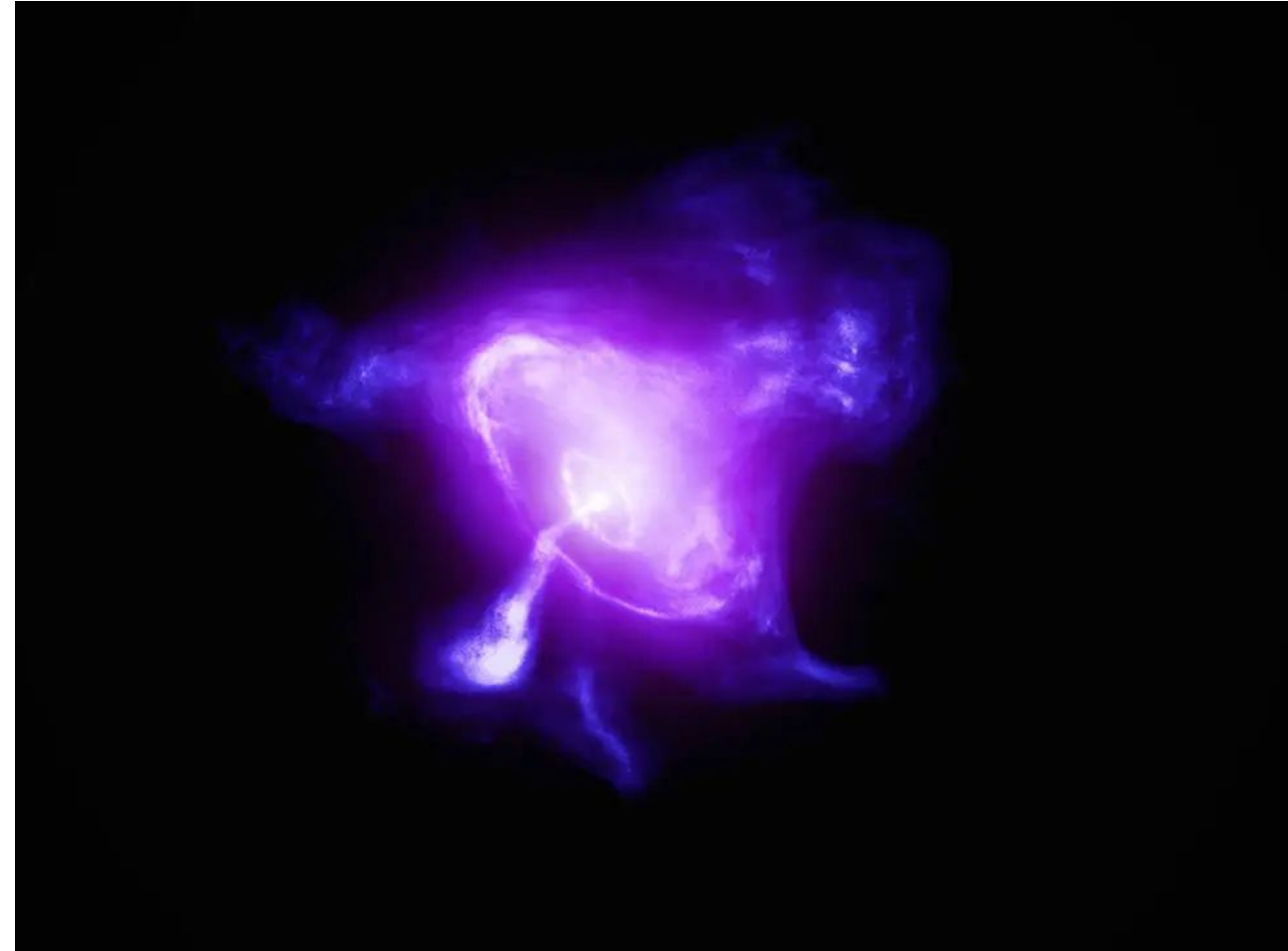


Image Credit: IXPE Collaboration

# Relating Birth Period to Current Day Sizes

- Based on the simulation studies of Van der Swaluw and Wu (2001), one can estimate the birth period of a pulsar using this formula.
- Valid for spherically symmetric systems  $10^3$ - $10^4$  years old.
- Makes use of the radio PWN and SNR radii to map the true extent of the PWN.

$$P_0 = 2\pi \left[ \frac{2E_0}{\eta_1 I} \left( \frac{R_{PWN}}{\eta_3 R_{SNR}} \right)^3 + \left( \frac{2\pi}{P_t} \right)^2 \right]^{-1/2}$$

# Relating Multiplicity to Electrons

- The Goldreich-Julian density represents the number of electrons stripped from the pulsar caps
- We then assume the spin-down luminosity of the pulsar evolves as
- The pair production multiplicity is then
- And the age of the pulsar is then

$$N_{GJ} = \int_{t=0}^{t=-\tau(P_0)} \frac{[6c\dot{E}(t)]^{1/2}}{e} (-dt)$$

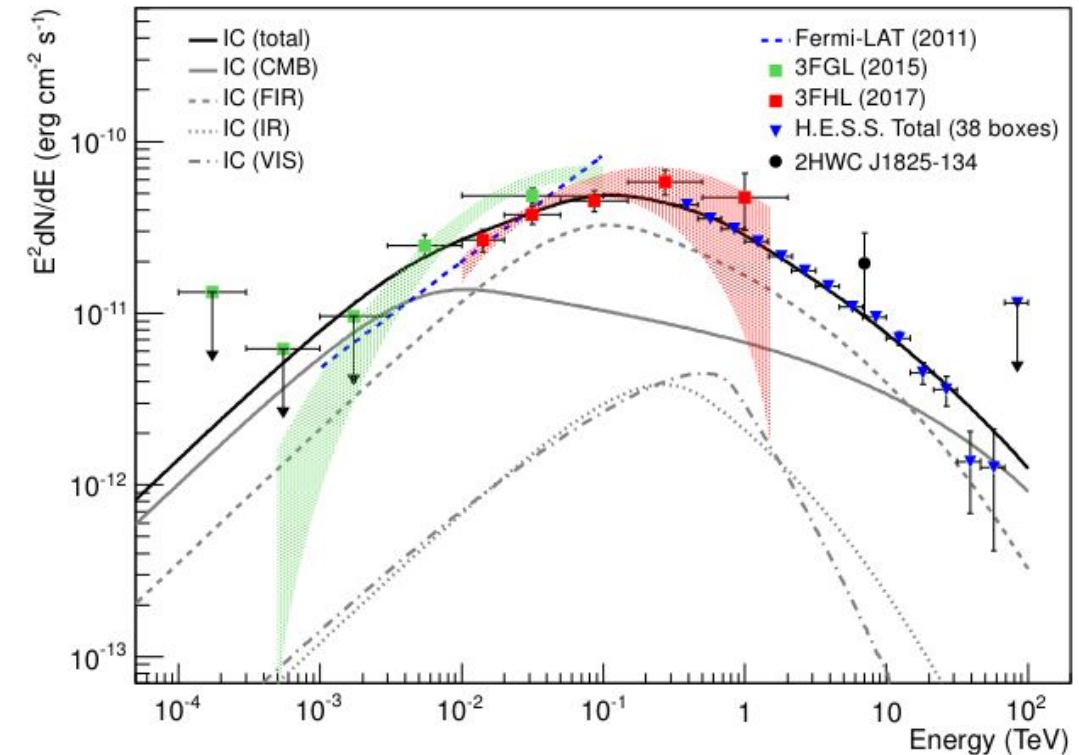
$$\dot{E}(t) = \dot{E}_0 \left(1 + \frac{t}{\tau_0}\right)^{-\frac{(n+1)}{(n-1)}}$$

$$\langle K \rangle = \frac{N_{el}}{2N_{GJ}}$$

$$\tau(P_t, \dot{P}_t, P_0, n) = \left(1 - \left(\frac{P_0}{P_t}\right)^{n-1}\right) \times \frac{P_t}{(n-1)\dot{P}_t}$$

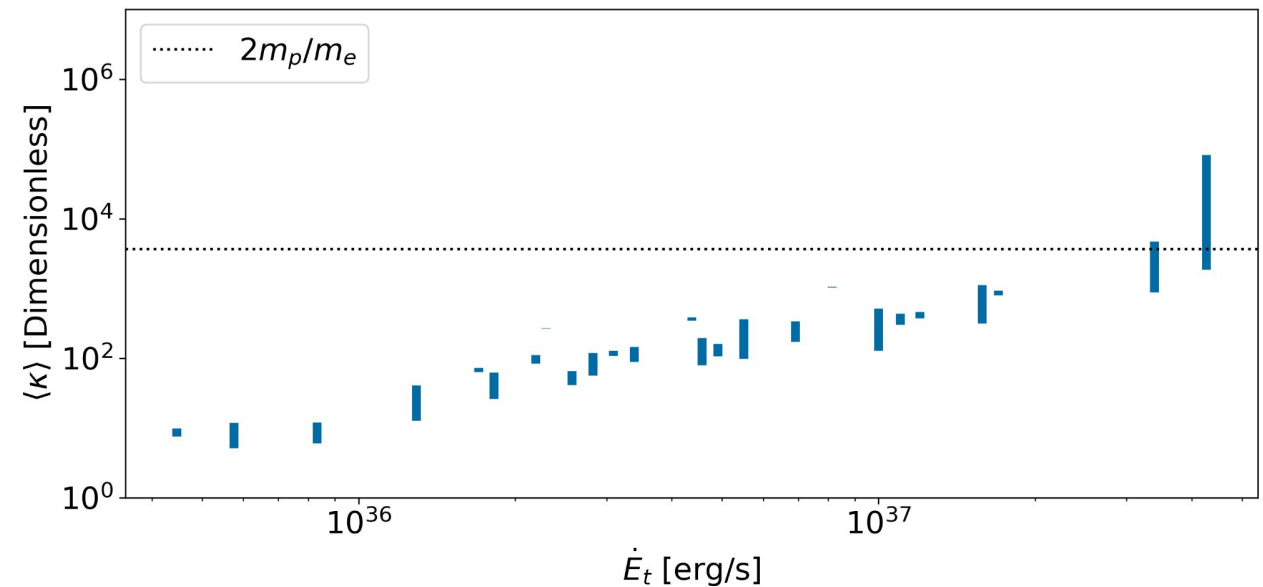
# Obtained the Number of Electrons via Gamma-ray Data

- As the multiplicity depends on the GJ density, which depends on the pulsar age, which depends on the pulsar birth period, we can create curves of kappa as a function of P0.
- This is provided the number of electrons in the PWN is known.
- Use the previous modelling in the literature and to find this. Multiplicities are strictly lower limits because non-gamma-ray emitting electrons not considered.



PSR J1826-1334, from H.E.S.S.  
Collaboration A&A 621, A116 (2019)

- As a first limit, we can estimate ranges of values for the lower limit of kappa for sources in the ATNF pulsar catalogue and the H.E.S.S. Galactic Plane Survey (HGPS).
- Assume birth period in the range 10-50ms.
- All sources in this sample have ranges that are compatible with hadrons escaping into the PWN (needs to have kappa below  $2m_p/m_e$  (3672)).

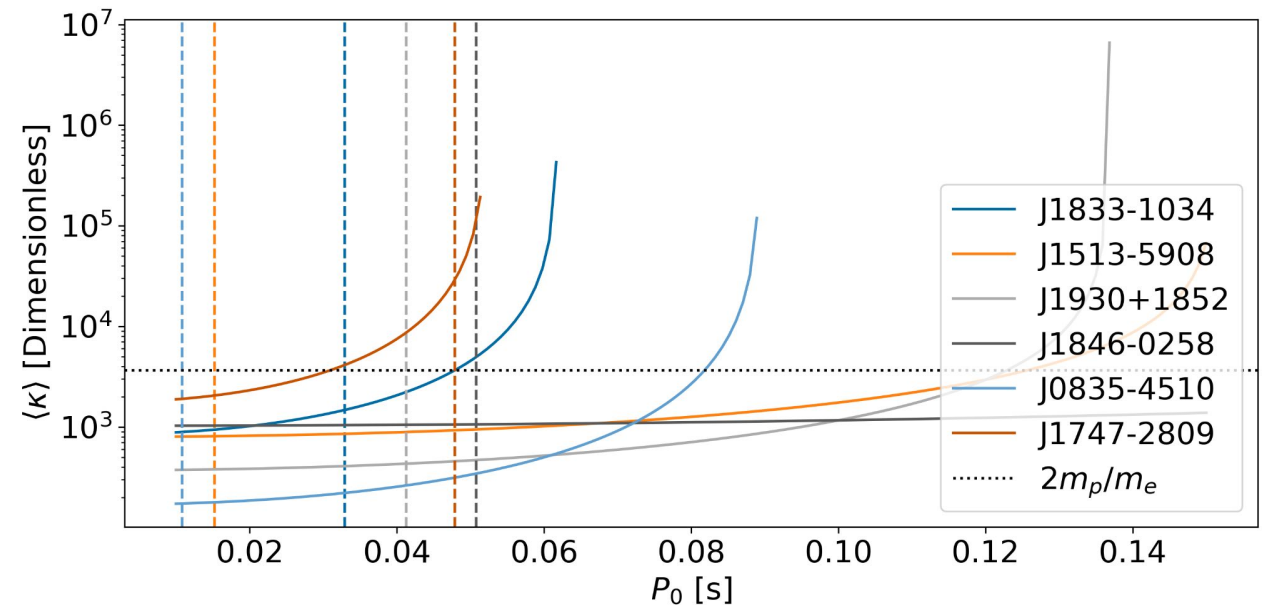


System	Crab	MSH 15-52	G21.5-0.9	G0.9+0.1	Vela X	G327.1-1.1	J1825-137	Geminga
Age (kyr) <sup>(a)</sup>	0.94	1.56	4.85	5.31	11.3	18	21.4	342
PSR <sup>(b)</sup>	B0531+21	B1509-58	J1833-1034	J1747-2809	B0833-45	<sup>(c)</sup>	B1823-13	J0633+1746
$\log(\dot{E})$ (erg s <sup>-1</sup> )	38.65	37.23	37.53	37.63	36.84	36.49	36.45	34.51
Distance (kpc)	2	4.4	4.1	8.5	0.28	9	3.93	0.25
$R_{\text{SNR}}$ (pc)	? <sup>(d)</sup>	38.4	2.98	19.8	19.5	22	120	?
$R_{\text{PWN}}$ (pc) <sup>(e)</sup>	2.8	19.2	0.8	2.5	12.2	10.5	?	0.01
$v \times t$ (pc) <sup>(f)</sup>	0.27	0.45	1.4	1.5	3.3	5.2	6.2	100
$R_{\text{TeV}}$ (pc) <sup>(g)</sup>	<3	11	<4	<7	2.9	3	50	16.2
$R_{\text{X-ray}}$ (pc)	0.24	10.2	0.8	4.9	3.08	13	9.1	0.15
Stage <sup>(h)</sup>	1	1	1b	1b	2	2	2b	3
Refs.	I	II	III	IV	V	VI	VII	VIII

Collated table from Giacinti et al. 2020 (A&A 636, A113). Uses data from e.g. VLA to give us radii of SNR and PWN counterparts.

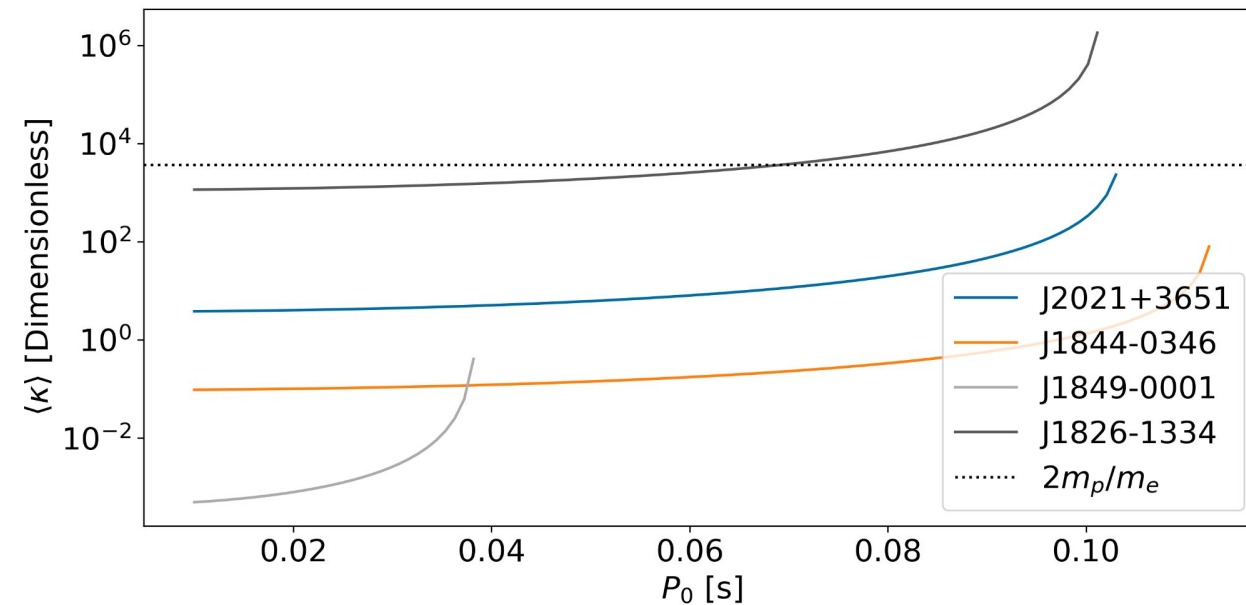


- Then for the six sources with measured PWN and SNR radii in both the radio, and seen by H.E.S.S., can calculate curves of kappa as a function of  $P_0$ .
- Using the radio data, we can then estimate  $P_0$ . Intersection point gives us (a lower limit for) kappa.
- For all except PSR J1747-2809, cannot exclude presence of hadrons in the PWN.



- For all except one source (PSR J1833-1034) we derive birth periods in the range 10-50ms that are broadly consistent with previous estimates (Helfland+ 2001, Camillo+ 2009).
- The value of 55ms we obtain for PSR J1833-1034 disagrees with Camillo+ 2009 who obtain 33ms, this is possibly because the system is too young for the Van der Swaluw+ approach to be valid.
- We don't find any sources with ms birth periods, these have been proposed as potential PeVatrons in the past (Kotera+ 2015).
- Pair production multiplicity limits also reasonable, theoretical cap at  $10^5$  (Timokhin+ 2019).

- Can utilise the same approach for sources recently observed by LHAASO.
- Again cannot exclude the possibility of hadronic escape for reasonable  $P_0$  values.



- Pulsar properties can be constrained using a mixture of radio and TeV data.
- We looked at a sample of 26 pulsars observed by ATNF, H.E.S.S. and LHAASO.
- For a subset of these sources, mostly reasonable estimates of  $P_0$  and  $\kappa$  were found. But more radio measurements would allow for the properties of more systems to be constrained.
- PSR J1747-2809 is the only source for which we can exclude the possibility of hadronic escape into the associated PWNe.

# Backup

**Table 1.** Properties of selected well-known PWN systems in different evolutionary stages, ordered according to the system age.

System	Crab	MSH 15-52	G21.5-0.9	G0.9+0.1	Vela X	G327.1-1.1	J1825-137	Geminga
Age (kyr) <sup>(a)</sup>	0.94	1.56	4.85	5.31	11.3	18	21.4	342
PSR <sup>(b)</sup>	B0531+21	B1509-58	J1833-1034	J1747-2809	B0833-45	<sup>(c)</sup>	B1823-13	J0633+1746
log( $\dot{E}$ ) (erg s <sup>-1</sup> )	38.65	37.23	37.53	37.63	36.84	36.49	36.45	34.51
Distance (kpc)	2	4.4	4.1	8.5	0.28	9	3.93	0.25
$R_{\text{SNR}}$ (pc)	? <sup>(d)</sup>	38.4	2.98	19.8	19.5	22	120	?
$R_{\text{PWN}}$ (pc) <sup>(e)</sup>	2.8	19.2	0.8	2.5	12.2	10.5	?	0.01
$v \times t$ (pc) <sup>(f)</sup>	0.27	0.45	1.4	1.5	3.3	5.2	6.2	100
$R_{\text{TeV}}$ (pc) <sup>(g)</sup>	<3	11	<4	<7	2.9	3	50	16.2
$R_{\text{X-ray}}$ (pc)	0.24	10.2	0.8	4.9	3.08	13	9.1	0.15
Stage <sup>(h)</sup>	1	1	1b	1b	2	2	2b	3
Refs.	I	II	III	IV	V	VI	VII	VIII

**Notes.** <sup>(a)</sup>The pulsar characteristic age is used for the age of the system, except where historical values are known. <sup>(b)</sup>Associated pulsar (PSR). Pulsar properties are taken from Manchester et al. (2005). <sup>(c)</sup>Putative pulsar candidate identified without pulsed emission detected by Temim et al. (2009). <sup>(d)</sup>Unknown quantities are marked by “?”. <sup>(e)</sup> $R_{\text{PWN}}$  is the size of the PWN in radio (as opposed to the radio SNR shell). <sup>(f)</sup> $v \times t$  is the pulsar kick velocity multiplied by the age of the system, where a value of 300 km s<sup>-1</sup> is adopted for the velocity, corresponding to the average of known values (Hansen & Phinney 1997). <sup>(g)</sup> $R_{\text{TeV}}$  is the one sigma radius taken from Abdalla et al. (2018b) for sources within the H.E.S.S. Galactic Plane Survey (HGPS), unless a reference is provided. <sup>(h)</sup>Stage of system evolution is assigned loosely based on age, which corresponds to Fig. 1.

**References.** I: Frail et al. (1995), Kargaltsev et al. (2015), II: Caswell et al. (1981), Du Plessis et al. (1995), Trussoni et al. (1996), Mineo et al. (2001); III: Matheson & Safi-Harb (2010), Safi-Harb et al. (2001); IV: Green (2014), Green (2017), Dubner et al. (2008), Porquet et al. (2003); V: Duncan et al. (1996), Dwarakanath (1991), Tibaldo et al. (2018); VI: Ma et al. (2016), Temim et al. (2015); VII: Stupar et al. (2008), Duvidovich et al. (2019), Pavlov et al. (2008), Uchiyama et al. (2009); VIII: Pellizzoni et al. (2011), Abeysekara et al. (2017a), Posselt et al. (2017), Caraveo et al. (2003).

Collated table from Giacinti et al. 2020 (A&A 636, A113). Uses data from e.g. VLA to give us radii of SNR and PWN counterparts.