

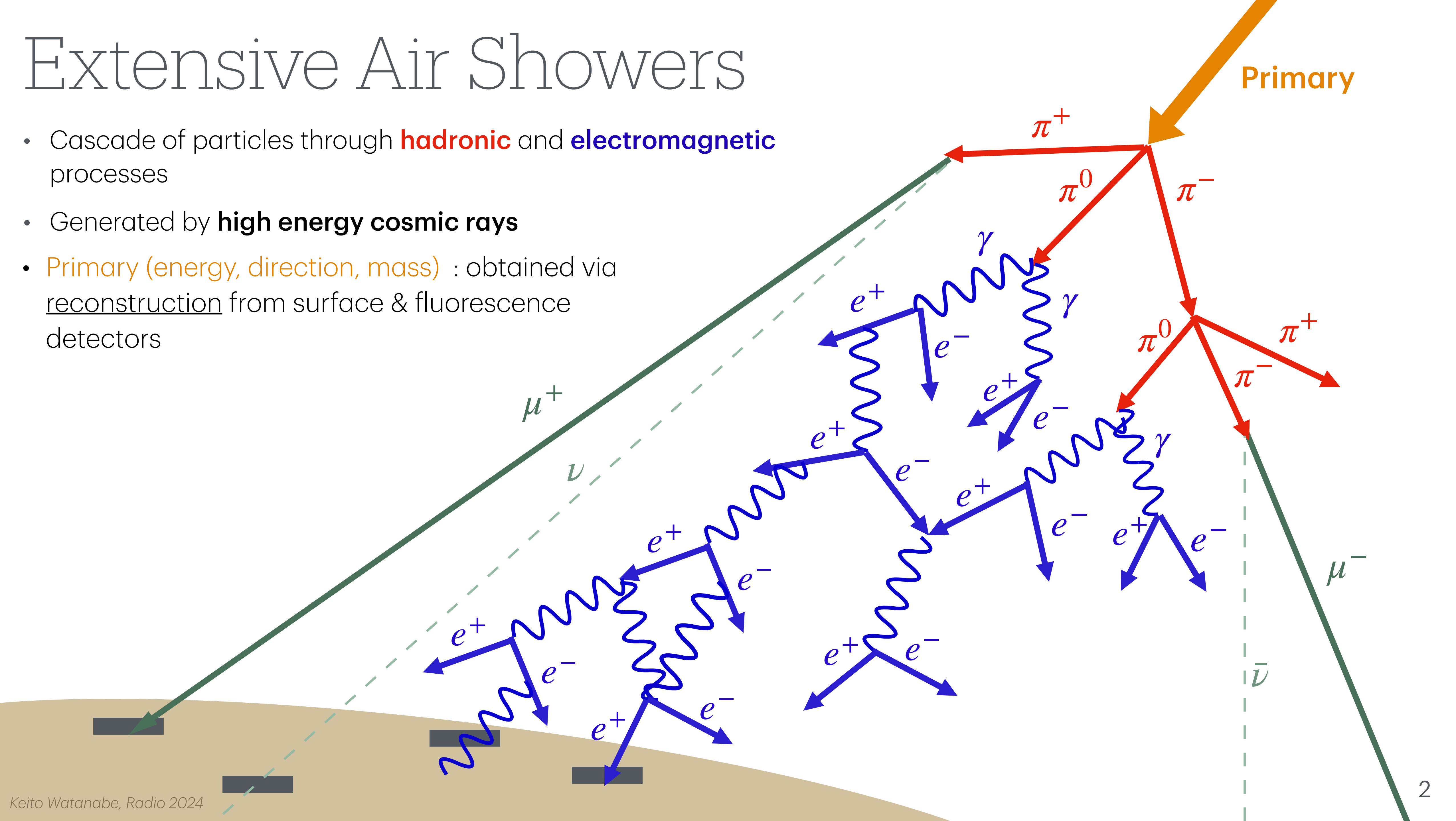
# Towards Cosmic Ray **Air Shower** **Imaging** using **Radio** Measurements

Keito Watanabe, Tim Huege

Radio 2024, 12.11.2024

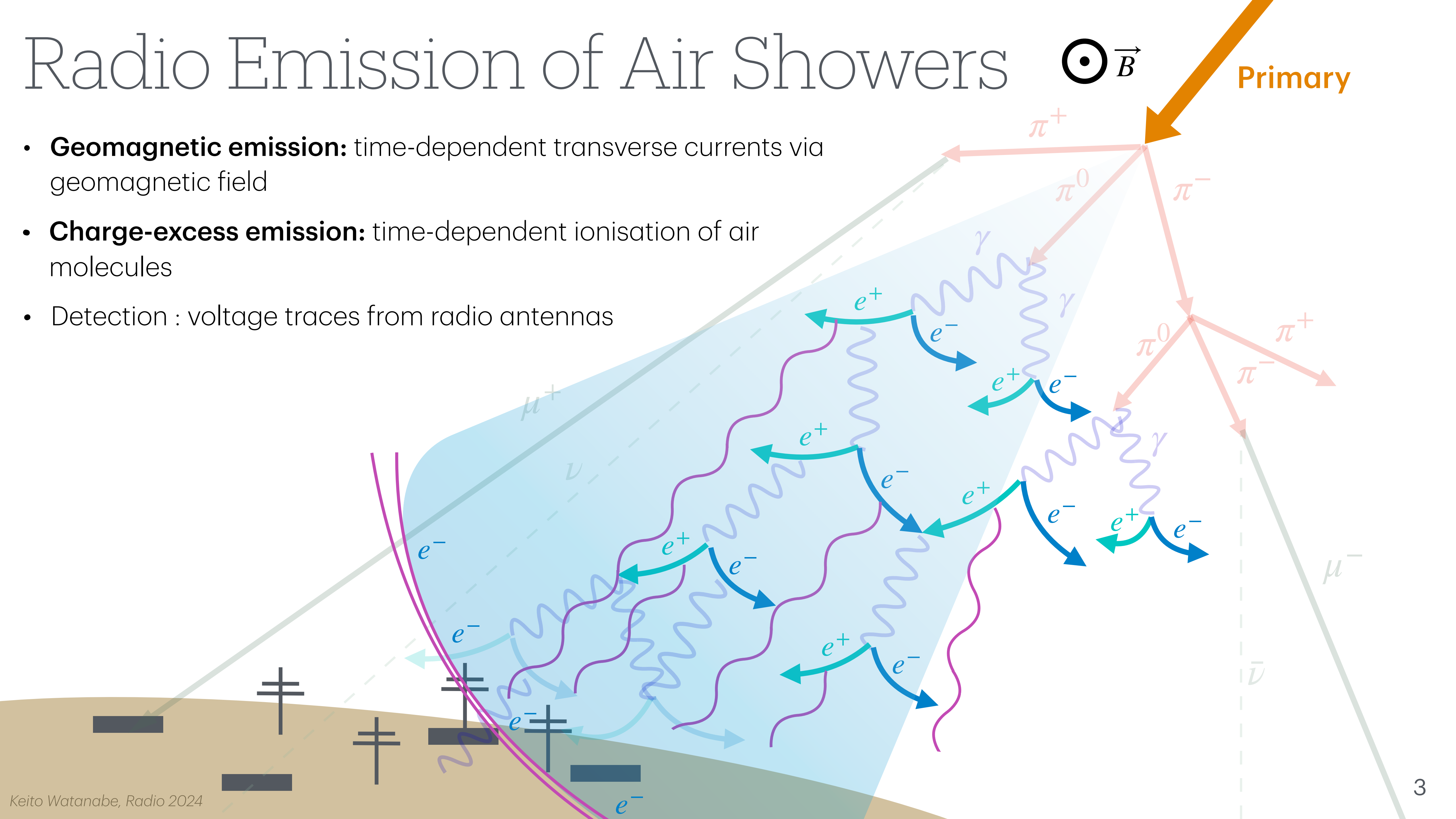
# Extensive Air Showers

- Cascade of particles through **hadronic** and **electromagnetic** processes
- Generated by **high energy cosmic rays**
- **Primary (energy, direction, mass)** : obtained via reconstruction from surface & fluorescence detectors



# Radio Emission of Air Showers

- **Geomagnetic emission:** time-dependent transverse currents via geomagnetic field
- **Charge-excess emission:** time-dependent ionisation of air molecules
- Detection : voltage traces from radio antennas

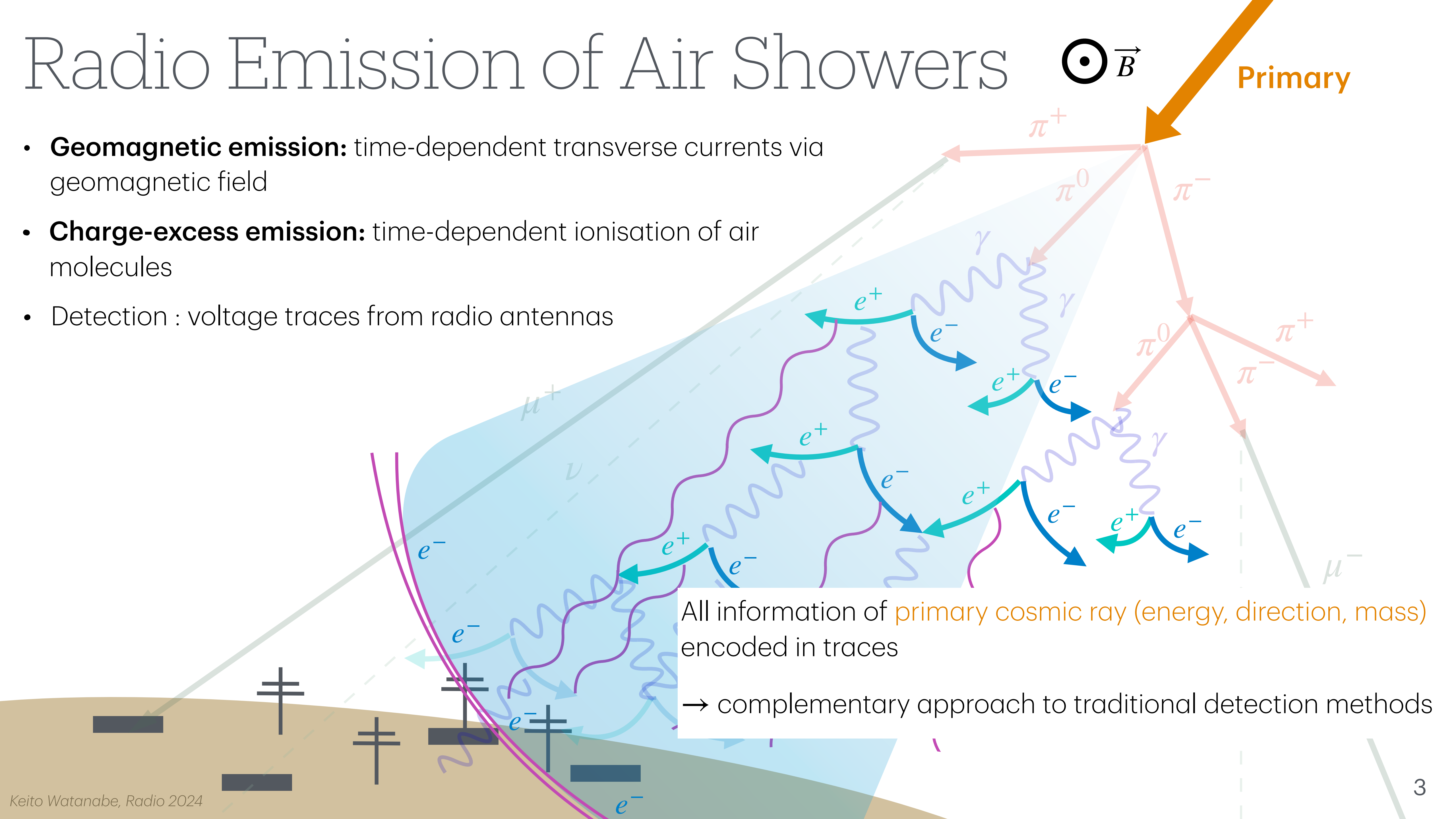


# Radio Emission of Air Showers

- **Geomagnetic emission:** time-dependent transverse currents via geomagnetic field
- **Charge-excess emission:** time-dependent ionisation of air molecules
- Detection : voltage traces from radio antennas



Primary

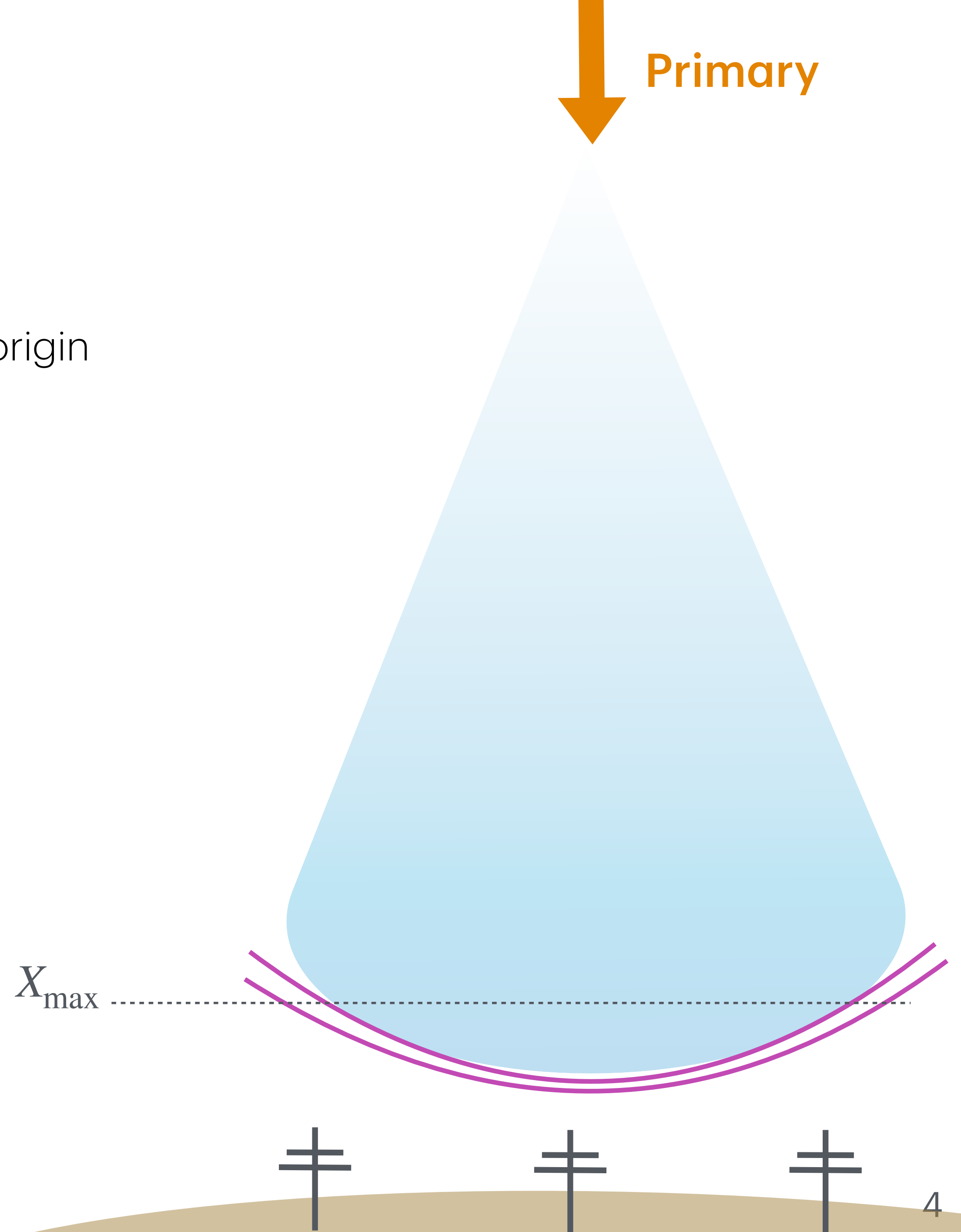


All information of primary cosmic ray (energy, direction, mass) encoded in traces  
→ complementary approach to traditional detection methods

# $X_{\max}$ Reconstruction

$X_{\max}$  : atmospheric depth of shower maximum ( $\text{g cm}^{-2}$ )

- Proxy for **primary mass**  $\rightarrow$  crucial piece to understand UHECR origin

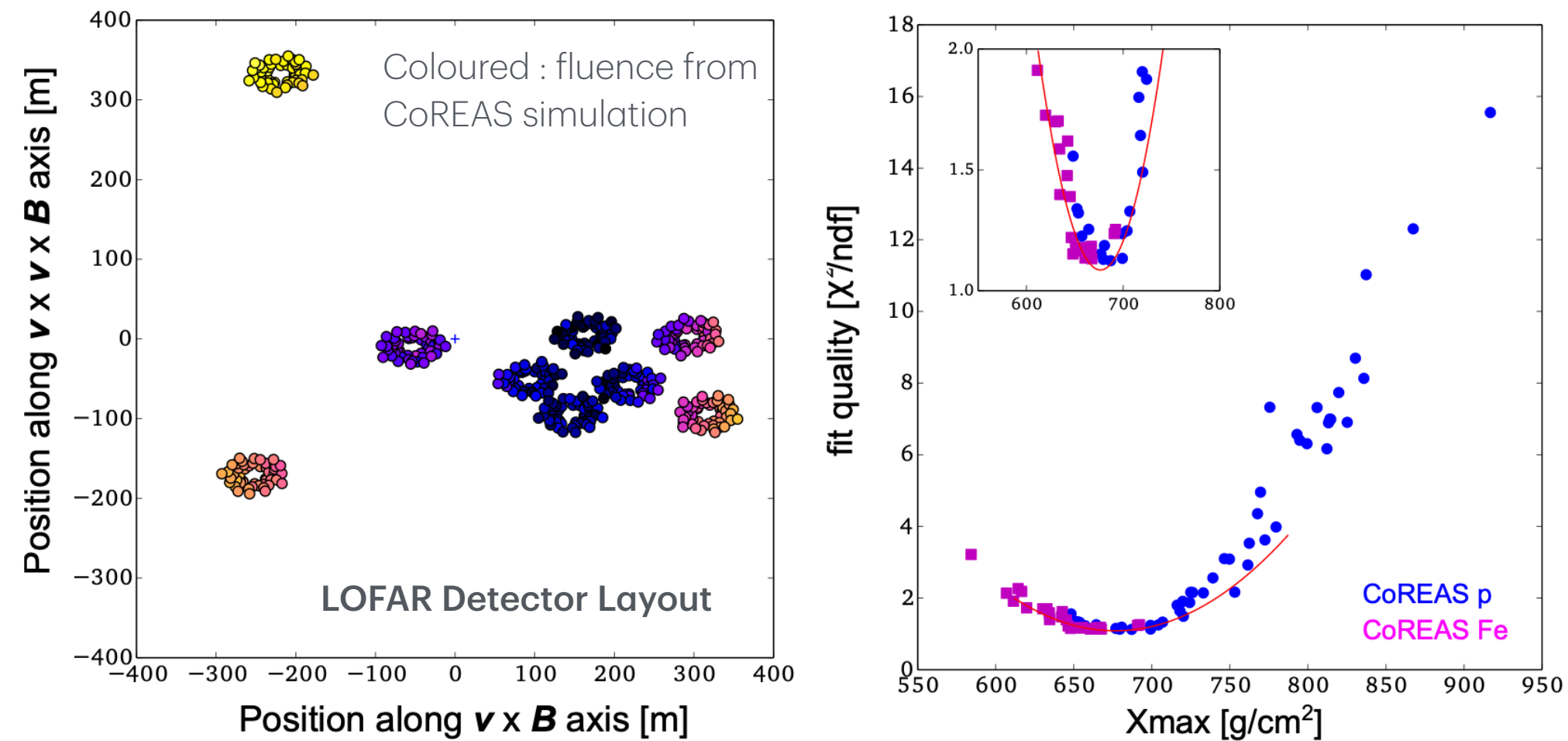


# $X_{\max}$ Reconstruction

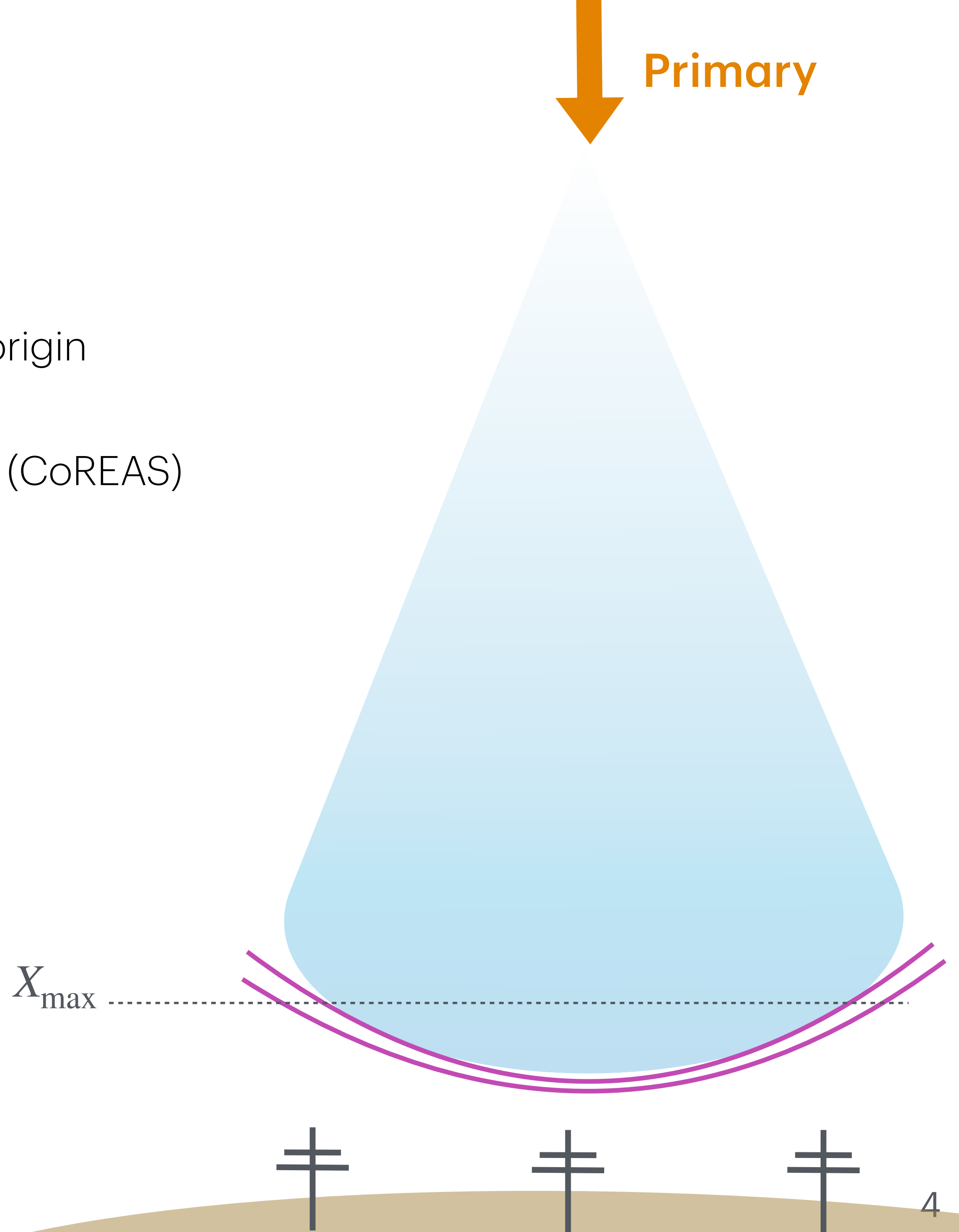
$X_{\max}$  : atmospheric depth of shower maximum ( $\text{g cm}^{-2}$ )

- Proxy for **primary mass**  $\rightarrow$  crucial piece to understand UHECR origin

Current: through fit quality of measurements with MC simulations (CoREAS)



S. Buitink et al. Phys.Rev.D 90 (2014) 082003



- Only energy deposited (fluence) used  $\rightarrow$  not all information utilised

$\Rightarrow$  can we extract more information for the **primary mass** ?

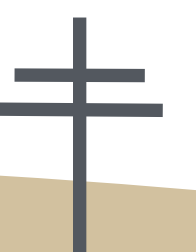
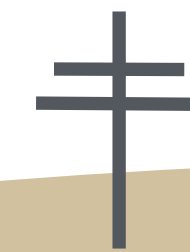
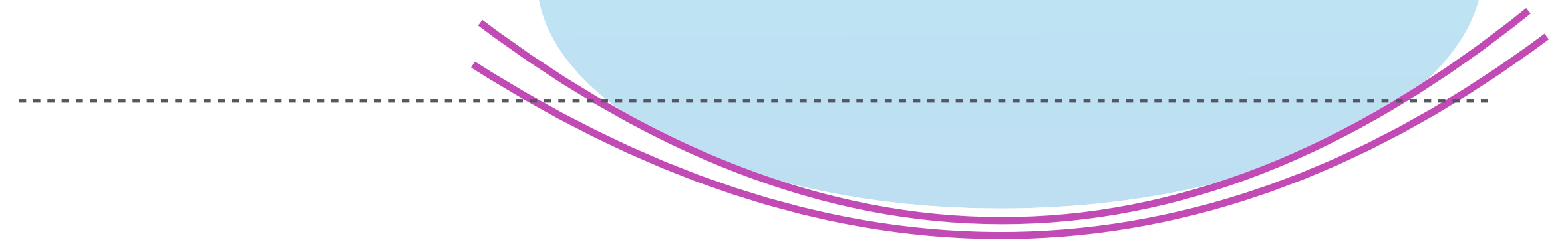
# $X_{\max}$ Shower Profile Reconstruction



**Goal:** reconstruct the **full air shower profile**

- Extract **more profile parameters** → more accurate **mass reconstruction**
- Leverage *extremely precise measurements* from dense + homogeneous antenna layout of **Square Kilometre Array**
- All information already available through traces!

$X_{\max}$



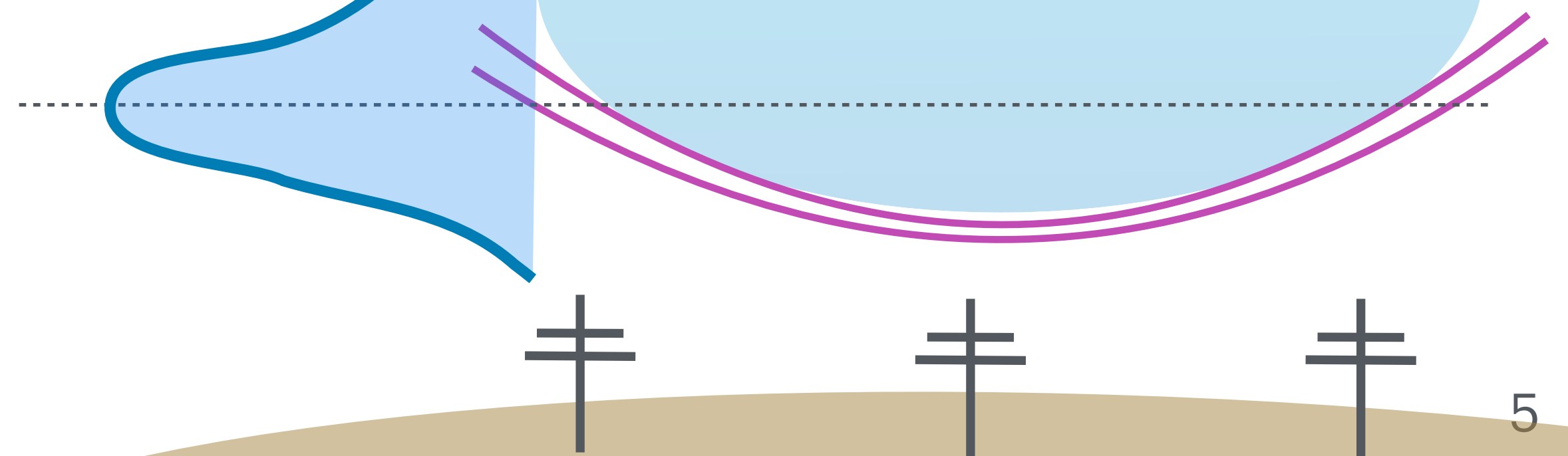
# $X_{\max}$ Shower Profile Reconstruction



**Goal:** reconstruct the **full air shower profile**

- Extract **more profile parameters** → more accurate **mass reconstruction**
- Leverage *extremely precise measurements* from dense + homogeneous antenna layout of **Square Kilometre Array**
- All information already available through traces!

$X_{\max}$





# $X_{\max}$ Shower Profile Reconstruction



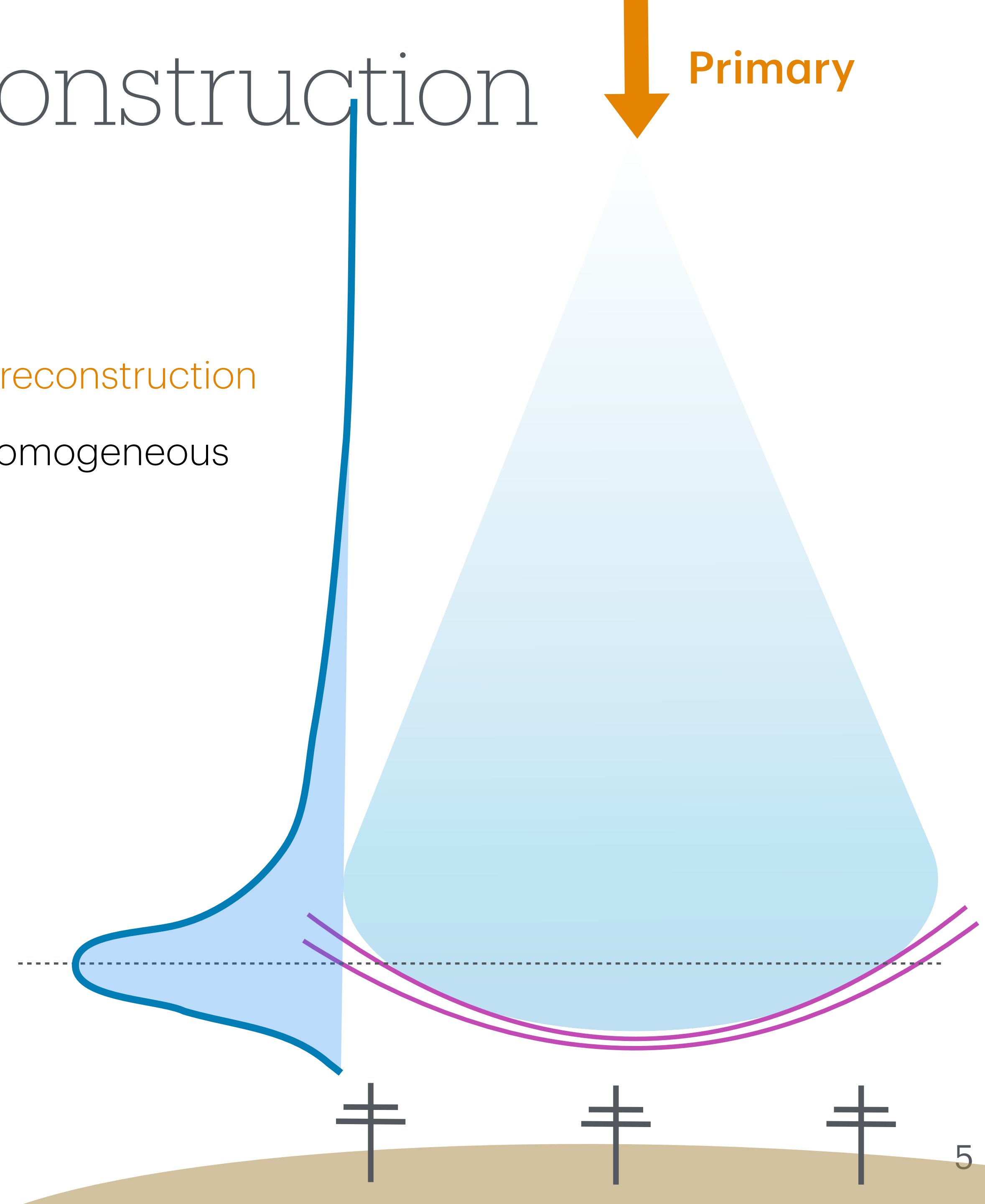
**Goal:** reconstruct the **full air shower profile**

- Extract **more profile parameters** → more accurate **mass reconstruction**
- Leverage *extremely precise measurements* from dense + homogeneous antenna layout of **Square Kilometre Array**
- All information already available through traces!

## Challenges:

- Spatial & time-dependent processes → **4-D problem**
- Trace = field → **many d.o.f.** ( $> O(10^3)$ )

$X_{\max}$



# $X_{\max}$ Shower Profile Reconstruction

Primary

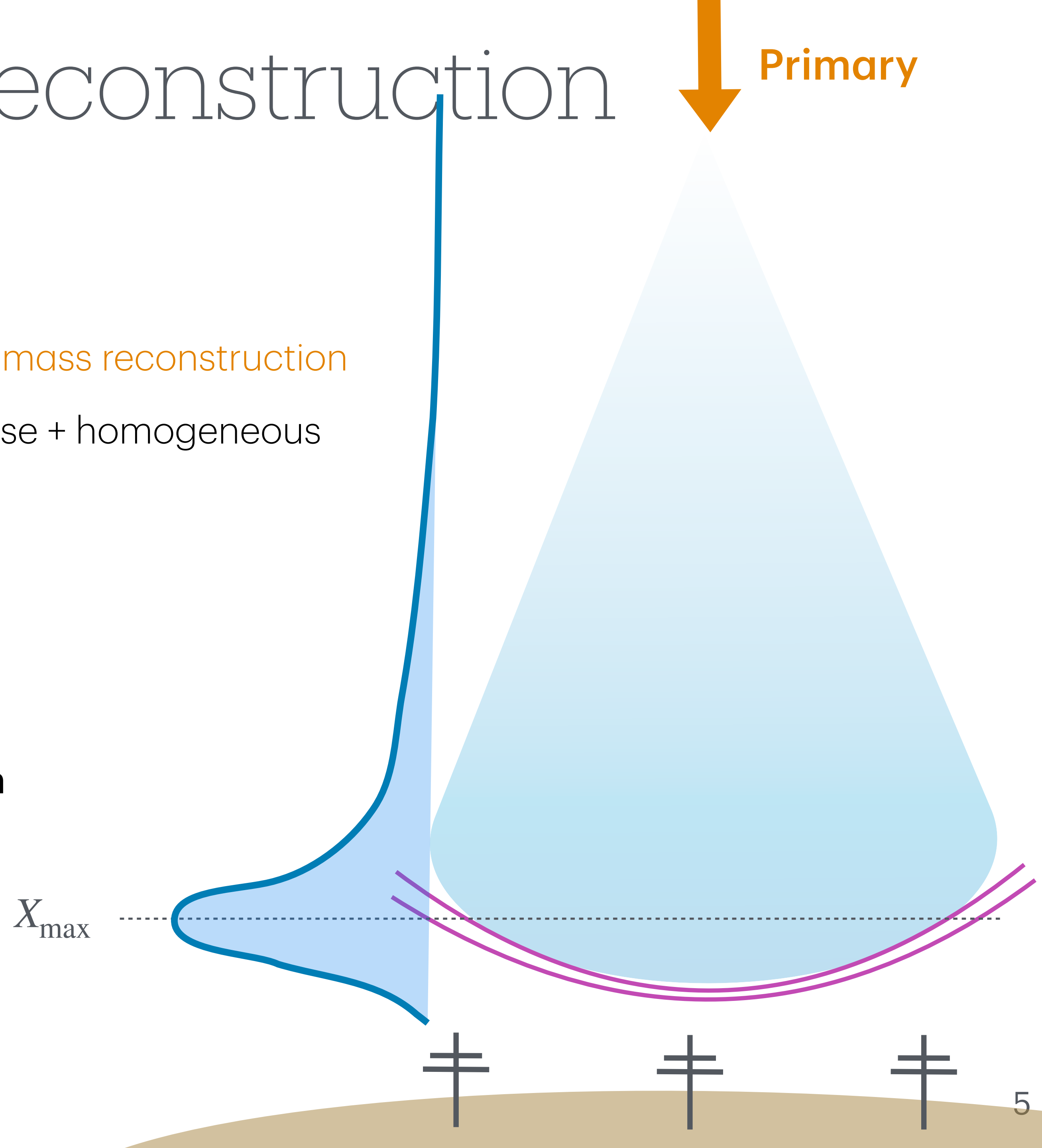
**Goal:** reconstruct the **full air shower profile**

- Extract **more profile parameters** → more accurate **mass reconstruction**
- Leverage *extremely precise measurements* from dense + homogeneous antenna layout of **Square Kilometre Array**
- All information already available through traces!

## Challenges:

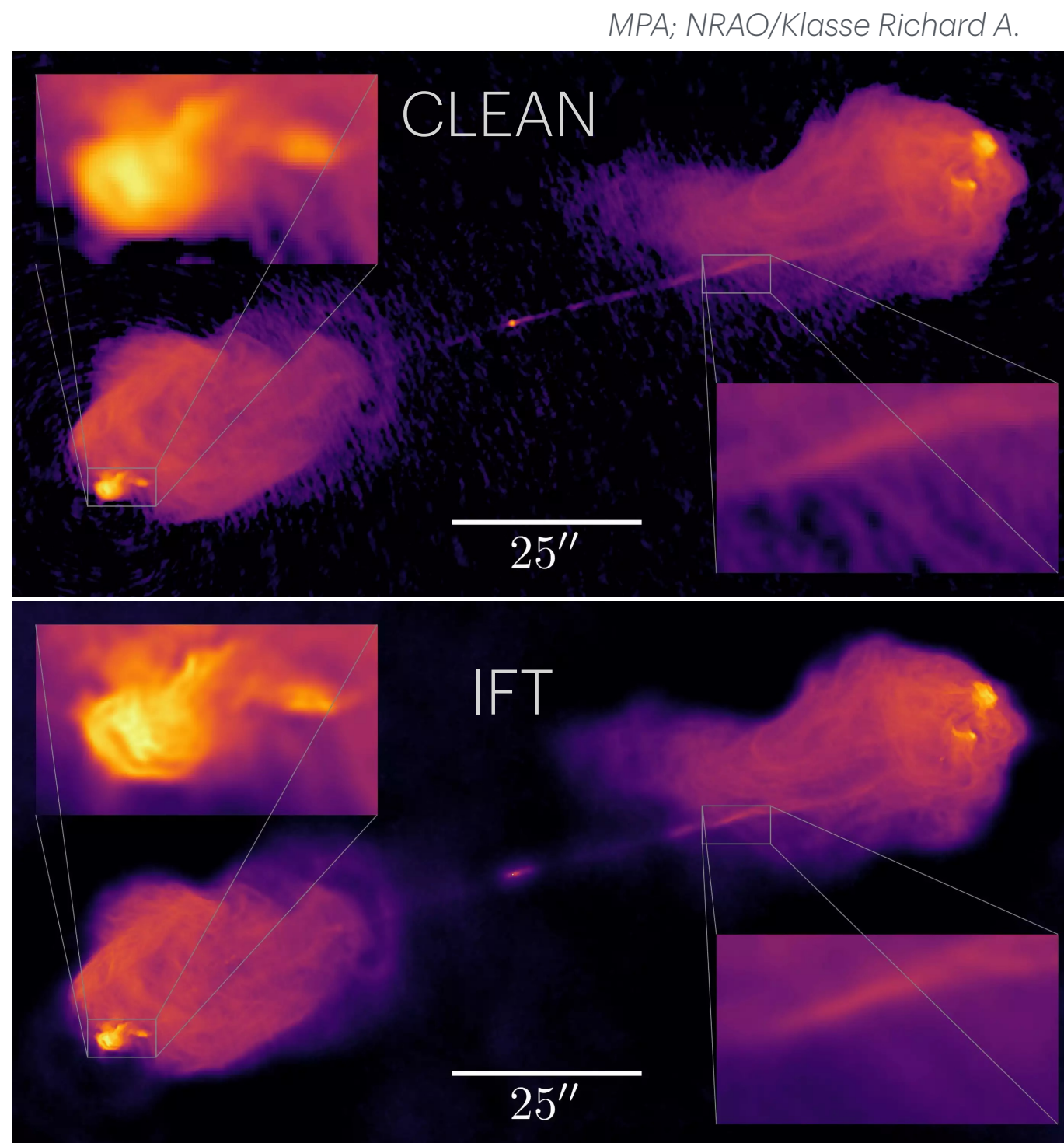
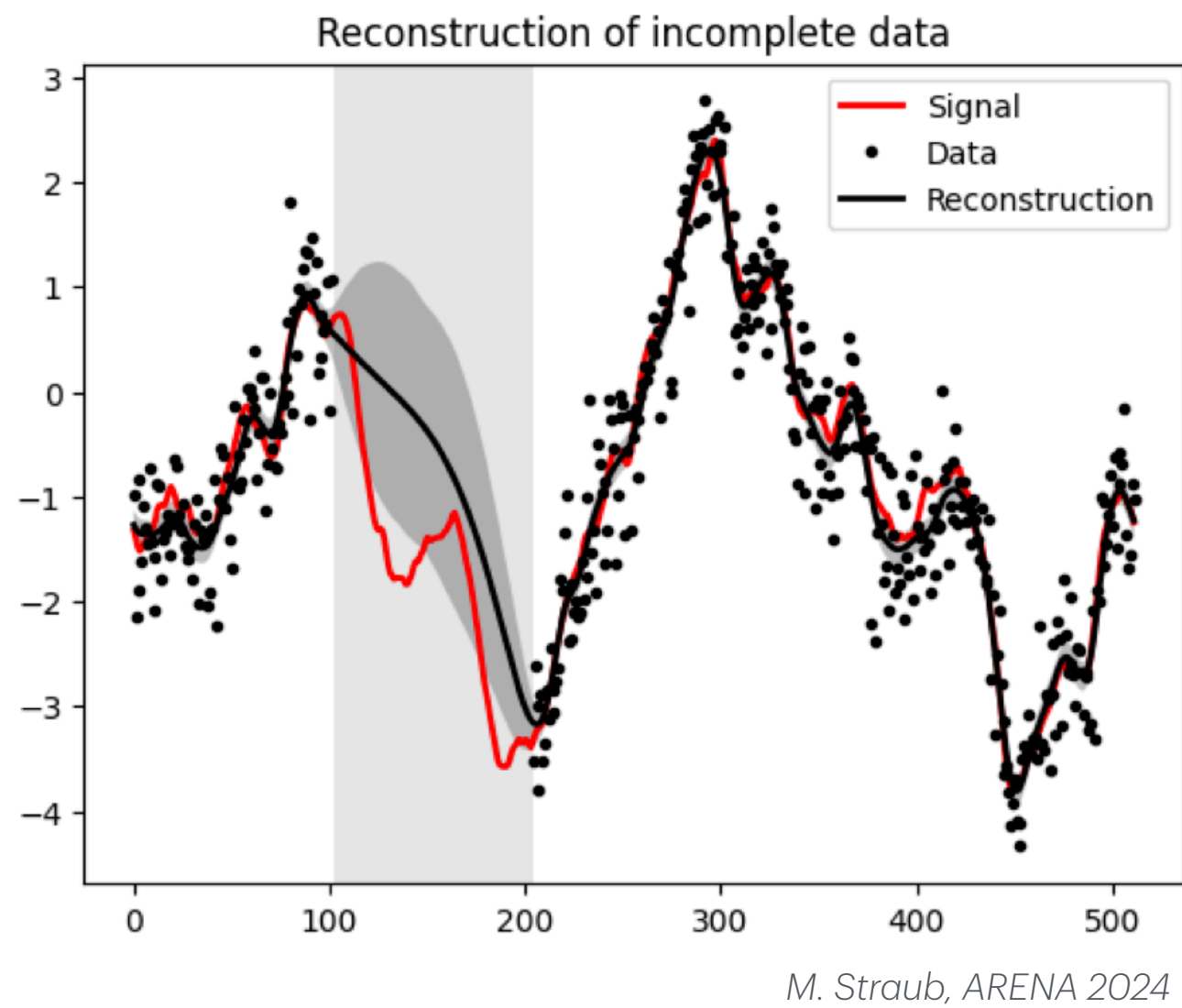
- Spatial & time-dependent processes → **4-D problem**
- Trace = field → **many d.o.f.** ( $> O(10^3)$ )

**Solution:** Information Field Theory!

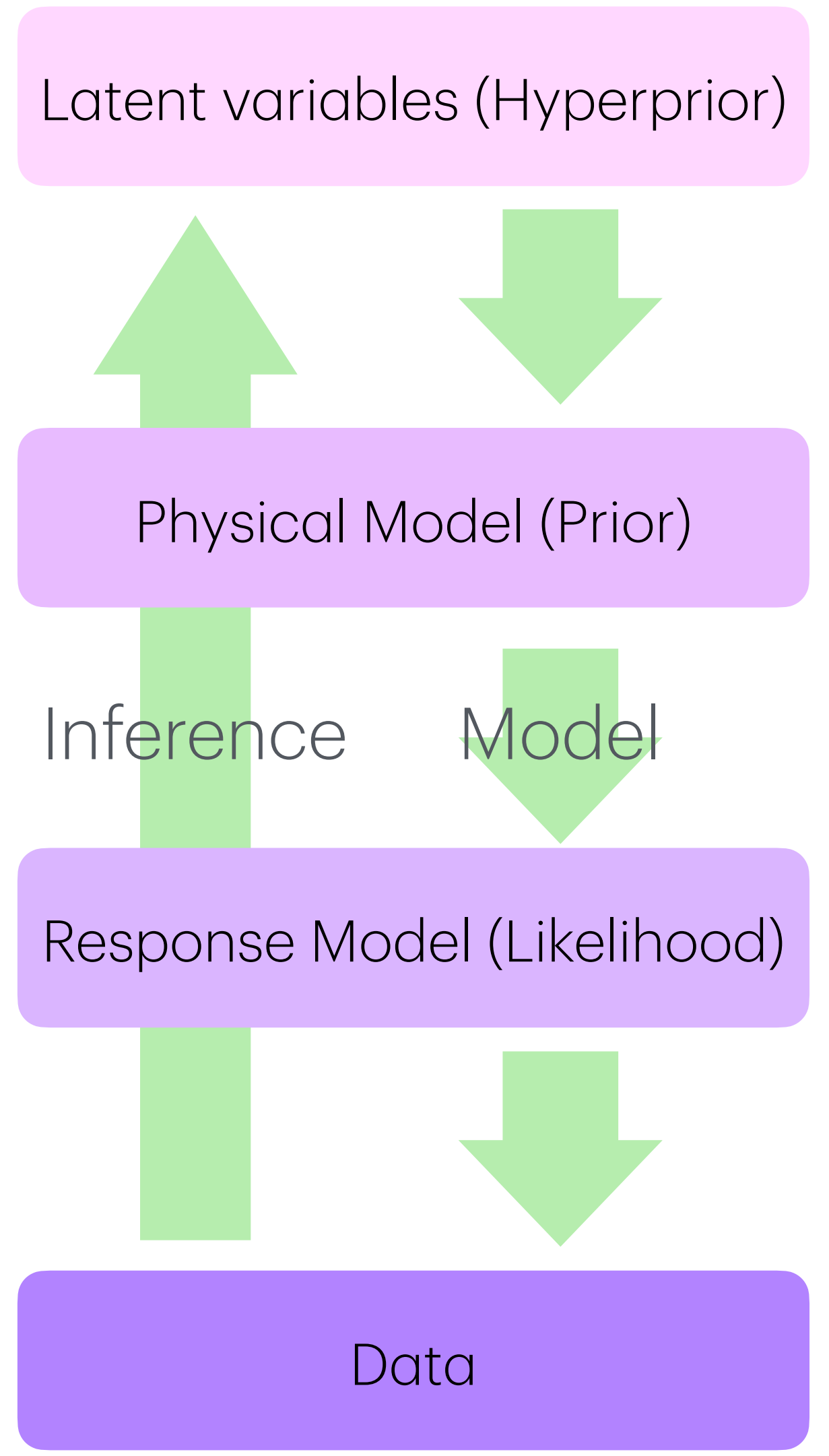


# Information Field Theory (IFT)

- Bayesian framework applied on field-like structures
- Easy-to-use Pythonic interface with **NIFTY**
- **Requirements:** fast & invertible forward model
- More information on [MPA/Ensslin/IFT](#)



Reconstruction of Cygnus A



# Shower Profile Model

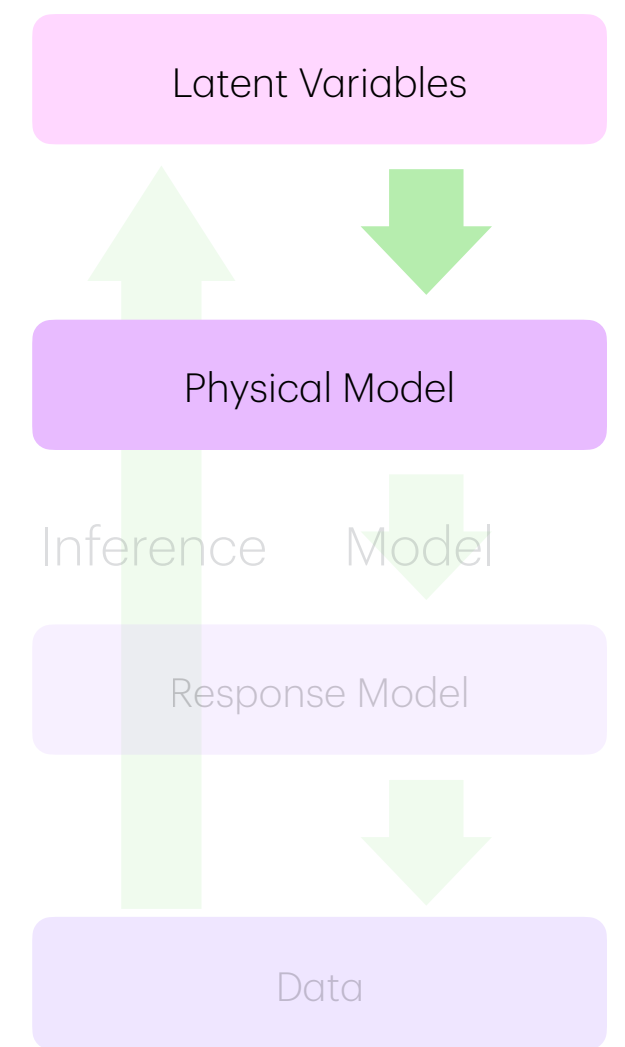
1. Sample **shower parameters** ( $X_{\max}$ ,  $N_{\max}$ ) from prior distributions

$$X_{\max} \sim \text{Uniform}(\min(X_{\max}), \max(X_{\max}))$$

$X_{\max}$  : atmospheric depth at shower maximum

$$N_{\max} \sim \text{LogNormal}(\mu_{N_{\max}}, \sigma_{N_{\max}})$$

$N_{\max}$  : number of particles at  $X_{\max}$



# Shower Profile Model

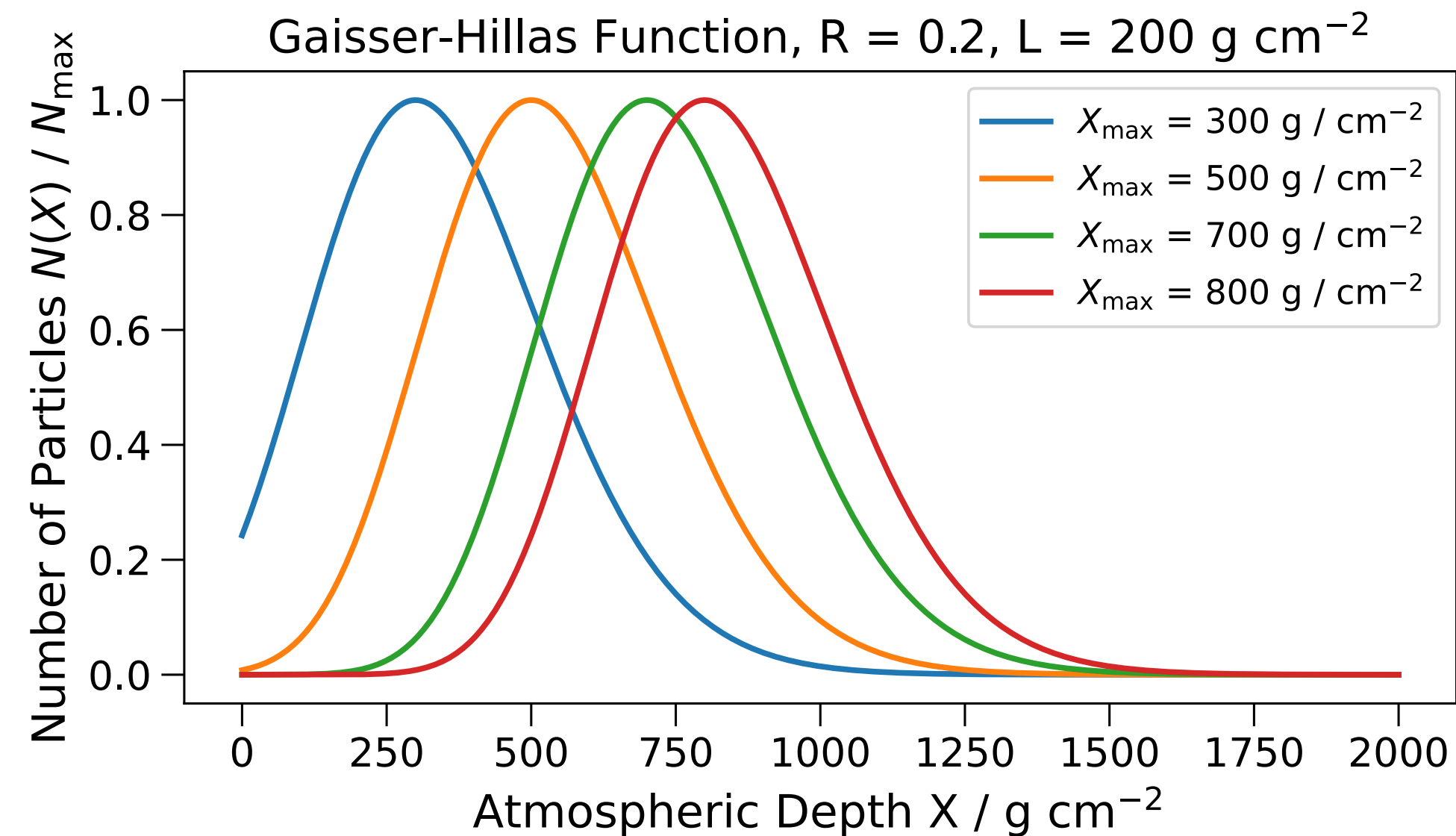
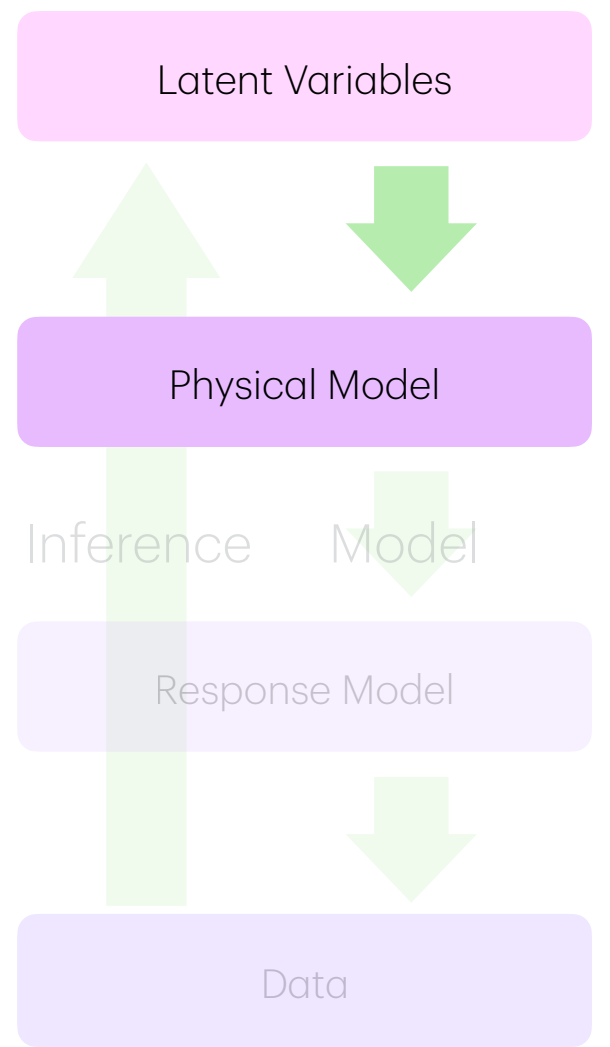
1. Sample **shower parameters** ( $X_{\max}$ ,  $N_{\max}$ ) from prior distributions

$$X_{\max} \sim \text{Uniform}(\min(X_{\max}), \max(X_{\max}))$$

$X_{\max}$  : atmospheric depth at shower maximum

$$N_{\max} \sim \text{LogNormal}(\mu_{N_{\max}}, \sigma_{N_{\max}})$$

$N_{\max}$  : number of particles at  $X_{\max}$



2. Describe **spatial evolution of shower** using Gaisser-Hillas function:

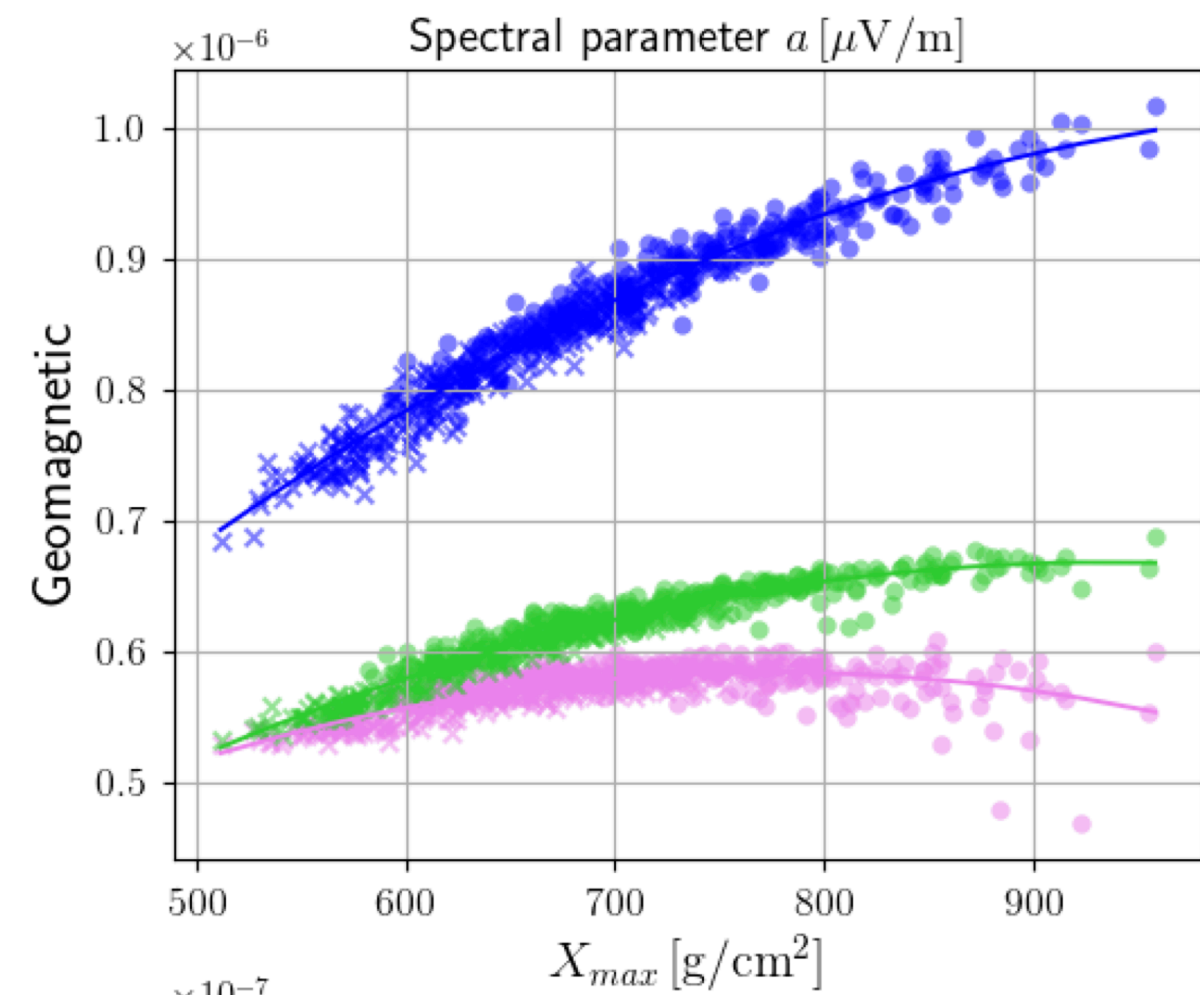
$$N(X) = N_{\max} \exp\left(\frac{X_{\max} - X}{L \cdot R}\right) \left(1 + \frac{R \cdot (X - X_{\max})}{L}\right)^{R-2}$$

NB: We only consider 1-D spatial evolution for now and fix  $L$ ,  $R$  parameters

# Radio Emission Model

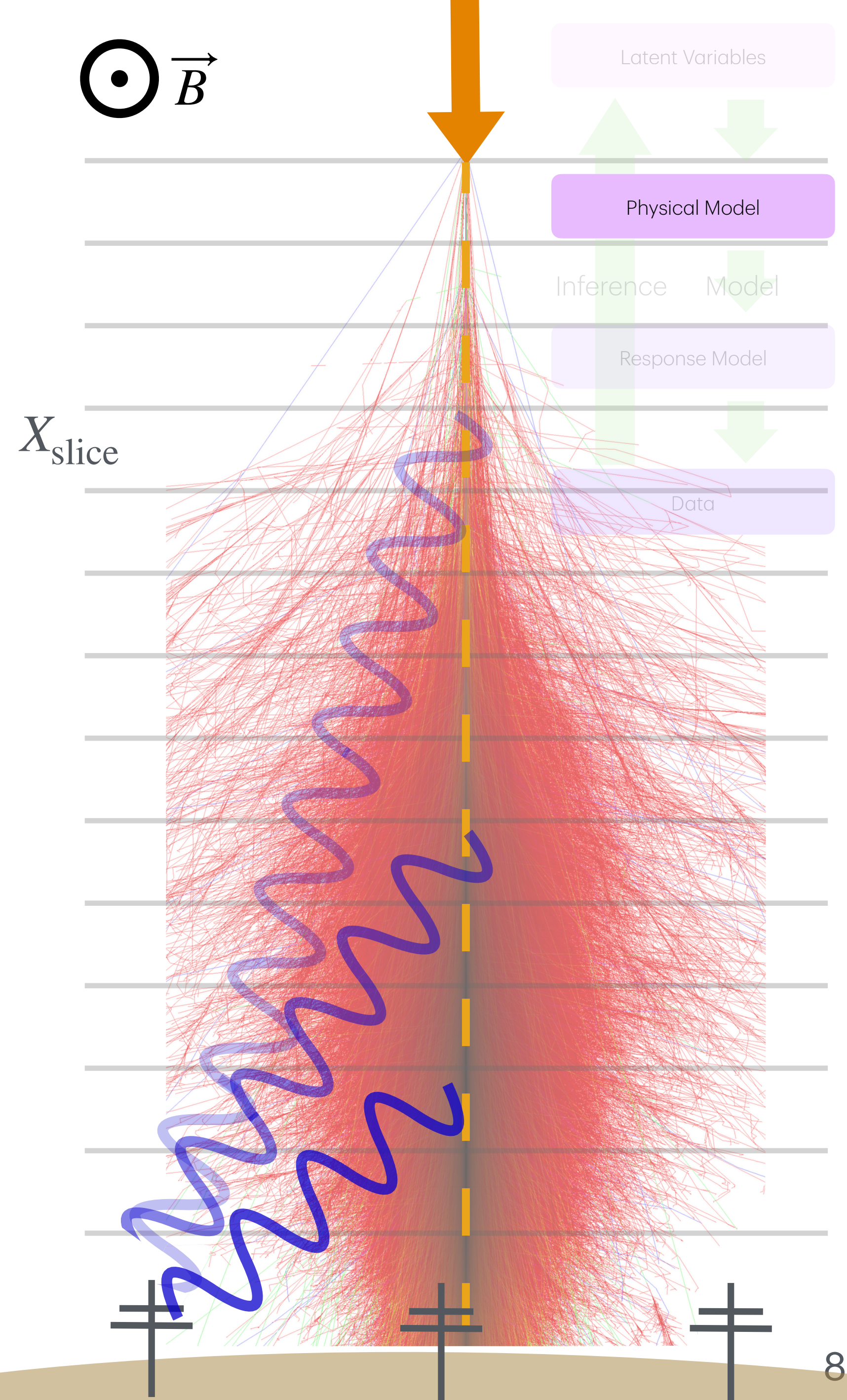
## Template Synthesis (Desmet+ 2024)

1. Parametrise relations between showers using MC simulations for each **atmospheric slice**  $X_{\text{slice}}$  & antennas



Spectral Parameter  $a$  computed from MC simulations at  $X_{\text{slice}}$ ,  $X_{\text{max}}$  and  $\vec{r}_{\text{ant}}$

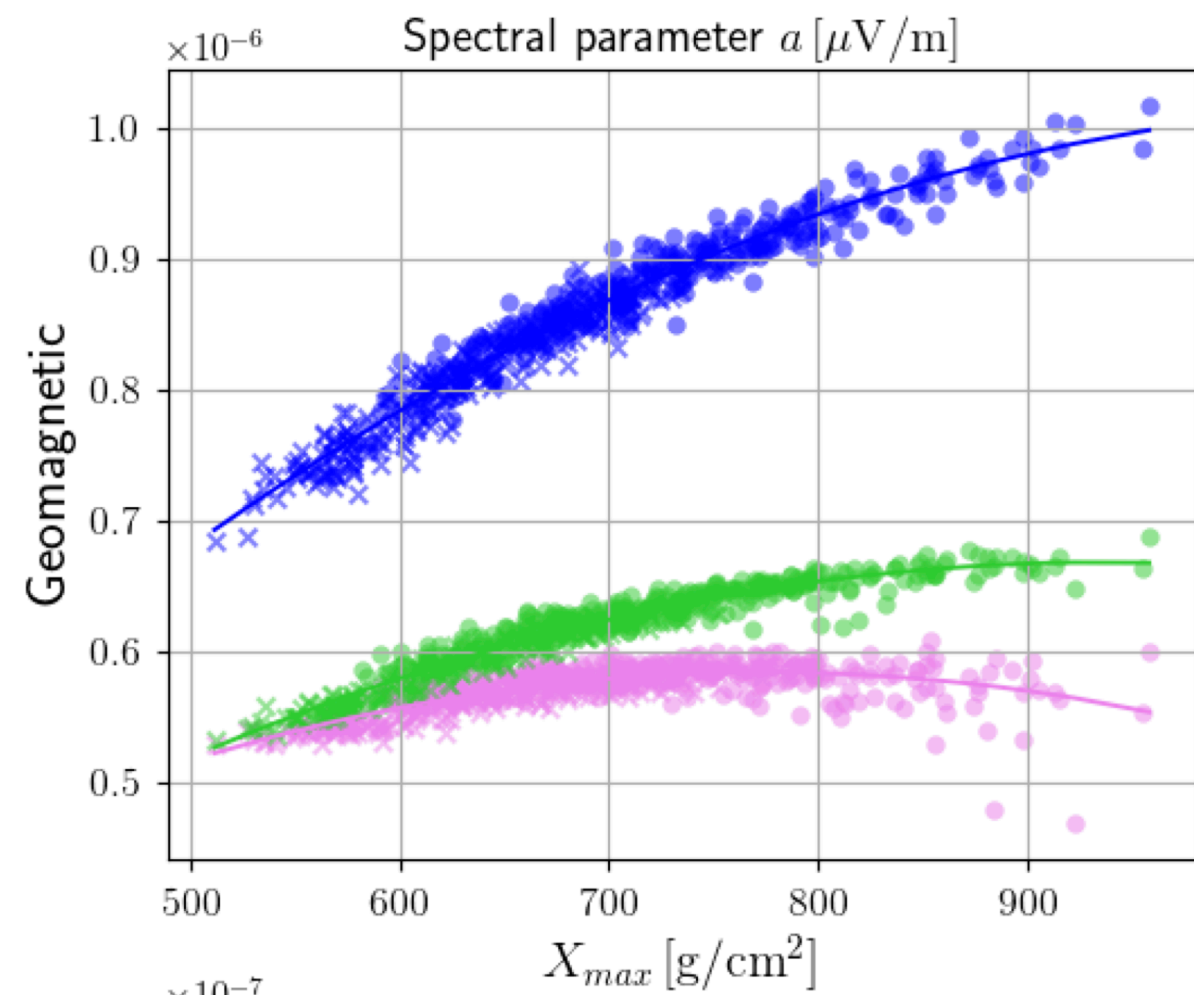
$$d_{\text{core}} = 75 \text{ m } \mathbf{[50, 200] \text{ MHz}}$$



# Radio Emission Model

## Template Synthesis (Desmet+ 2024)

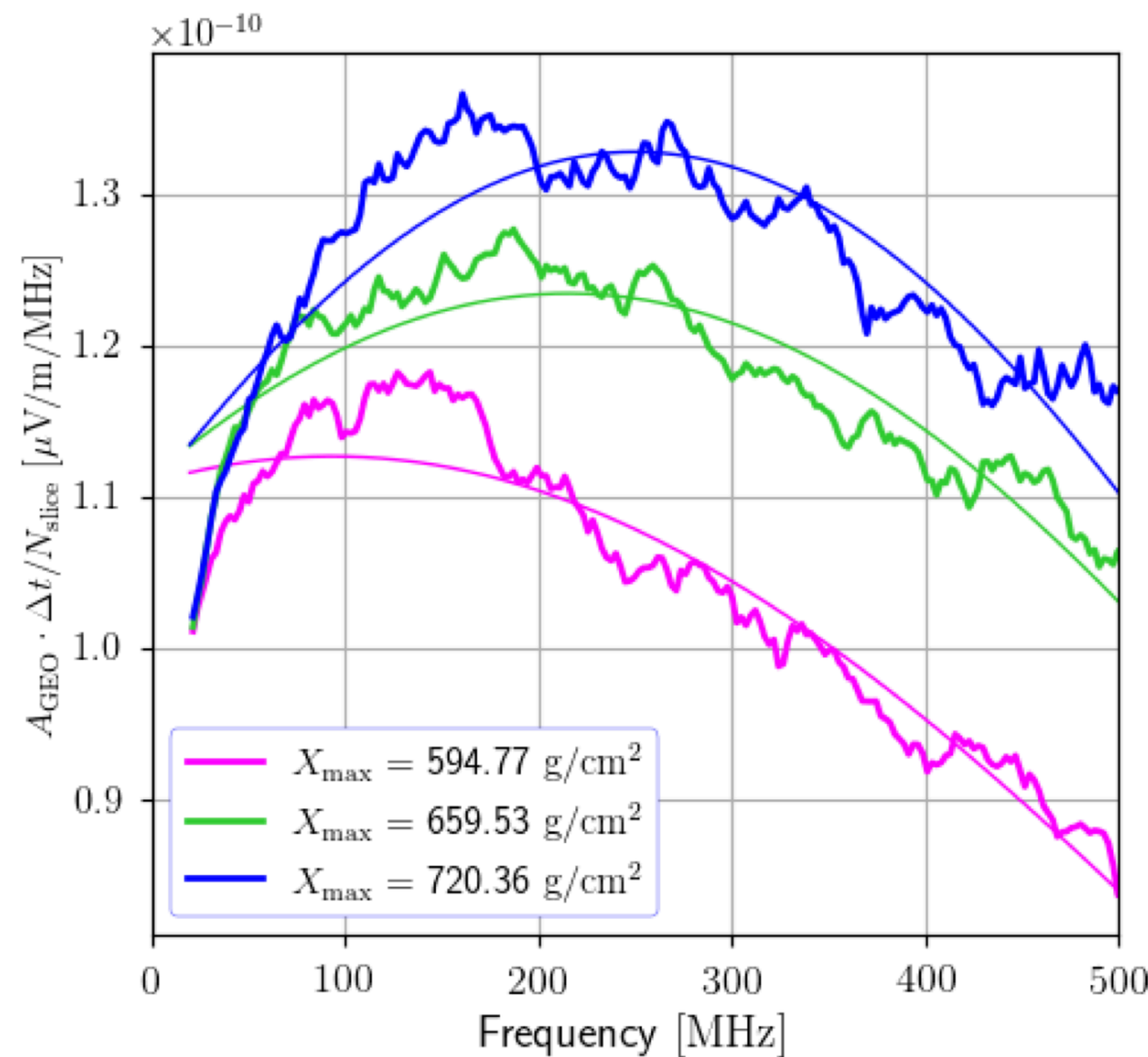
1. Parametrise relations between showers using MC simulations for each **atmospheric slice**  $X_{\text{slice}}$  & antennas



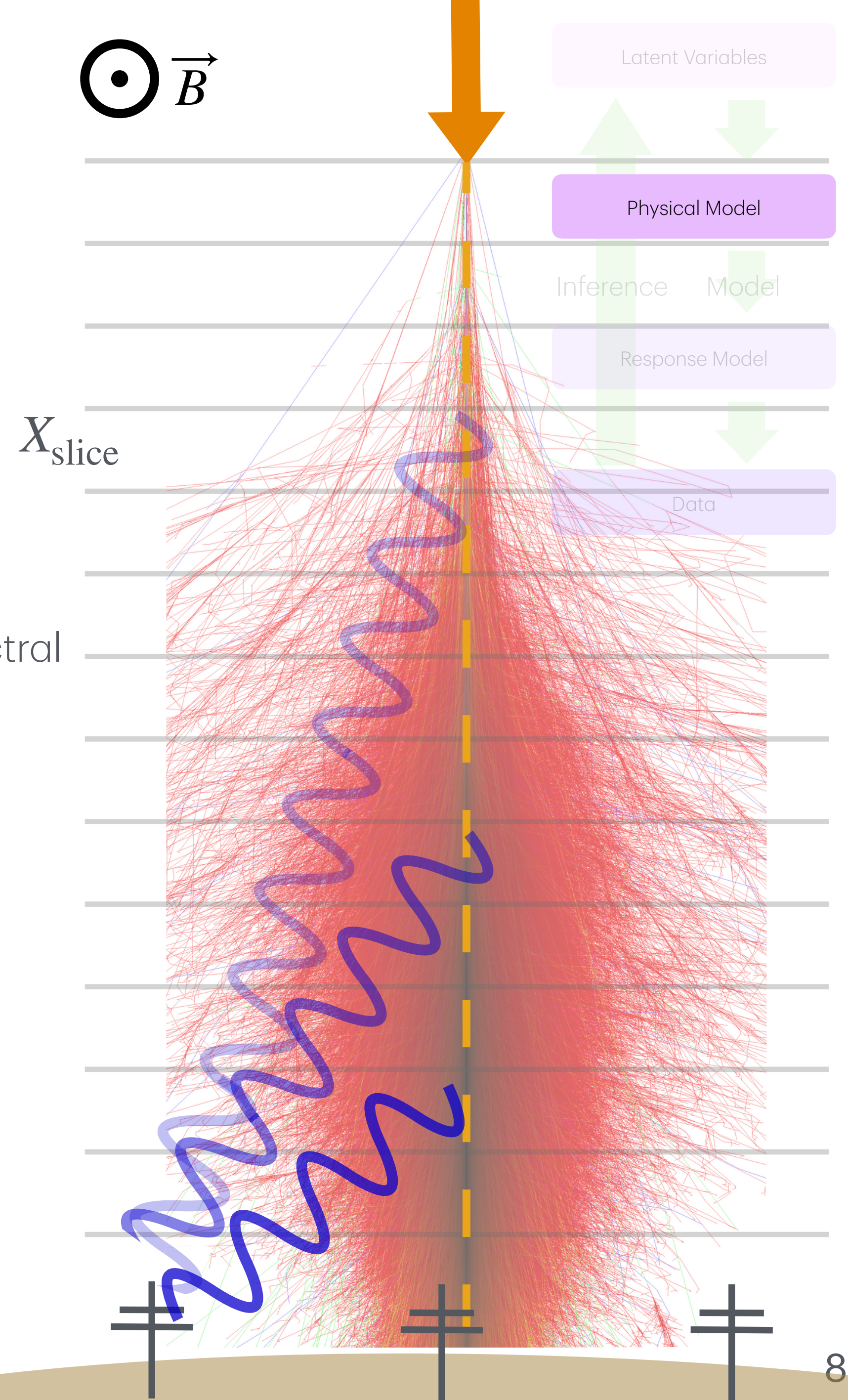
Spectral Parameter  $a$  computed from MC simulations at  $X_{\text{slice}}$ ,  $X_{\text{max}}$  and  $\vec{r}_{\text{ant}}$

$$d_{\text{core}} = 75 \text{ m } [50, 200] \text{ MHz}$$

Amplitude spectrum computed from spectral parameters at  $X_{\text{slice}} = 600 \text{ g cm}^{-2}$



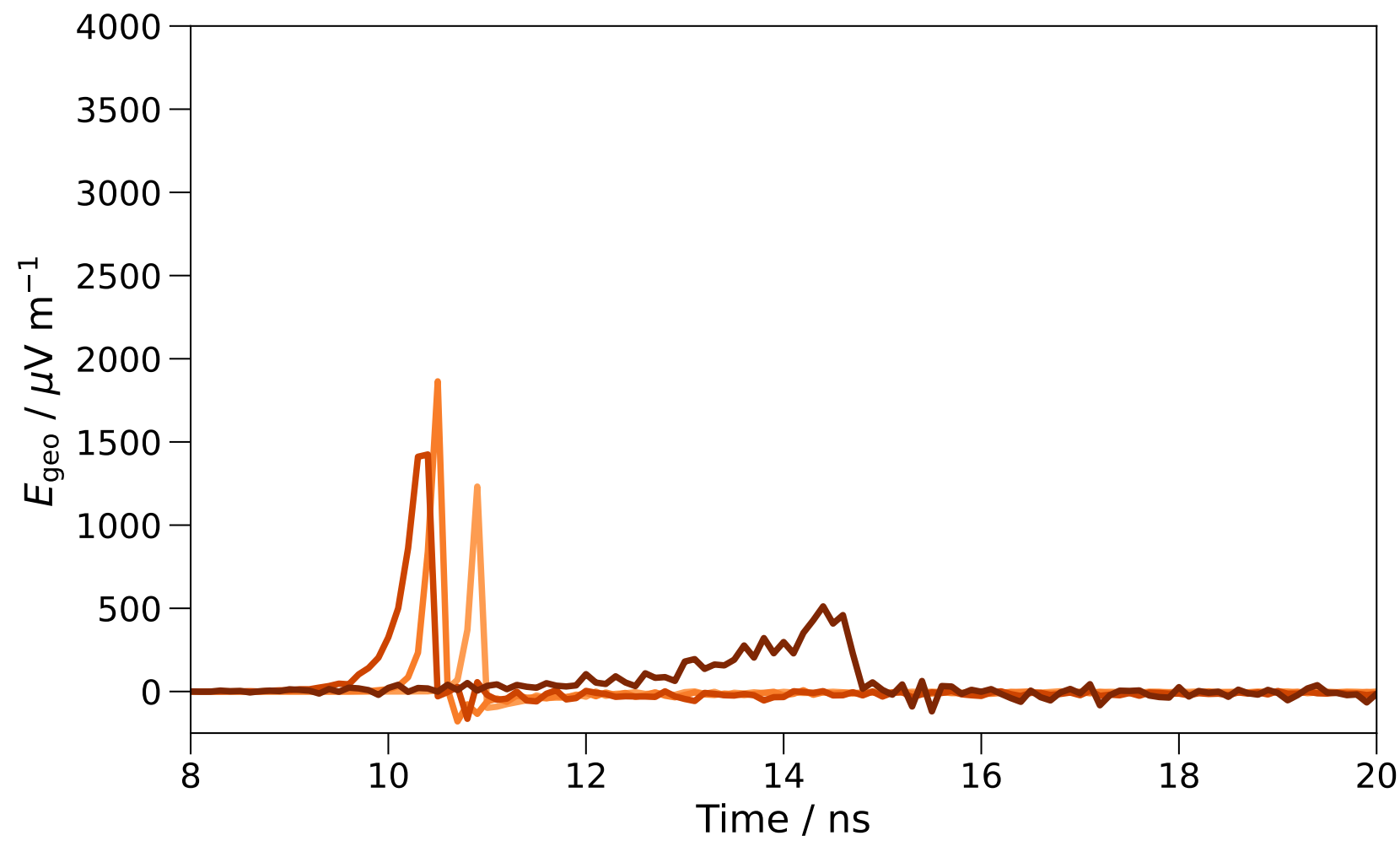
Desmet et al. 2024, Astroparticle Physics, 157, 102923



# Radio Emission Model

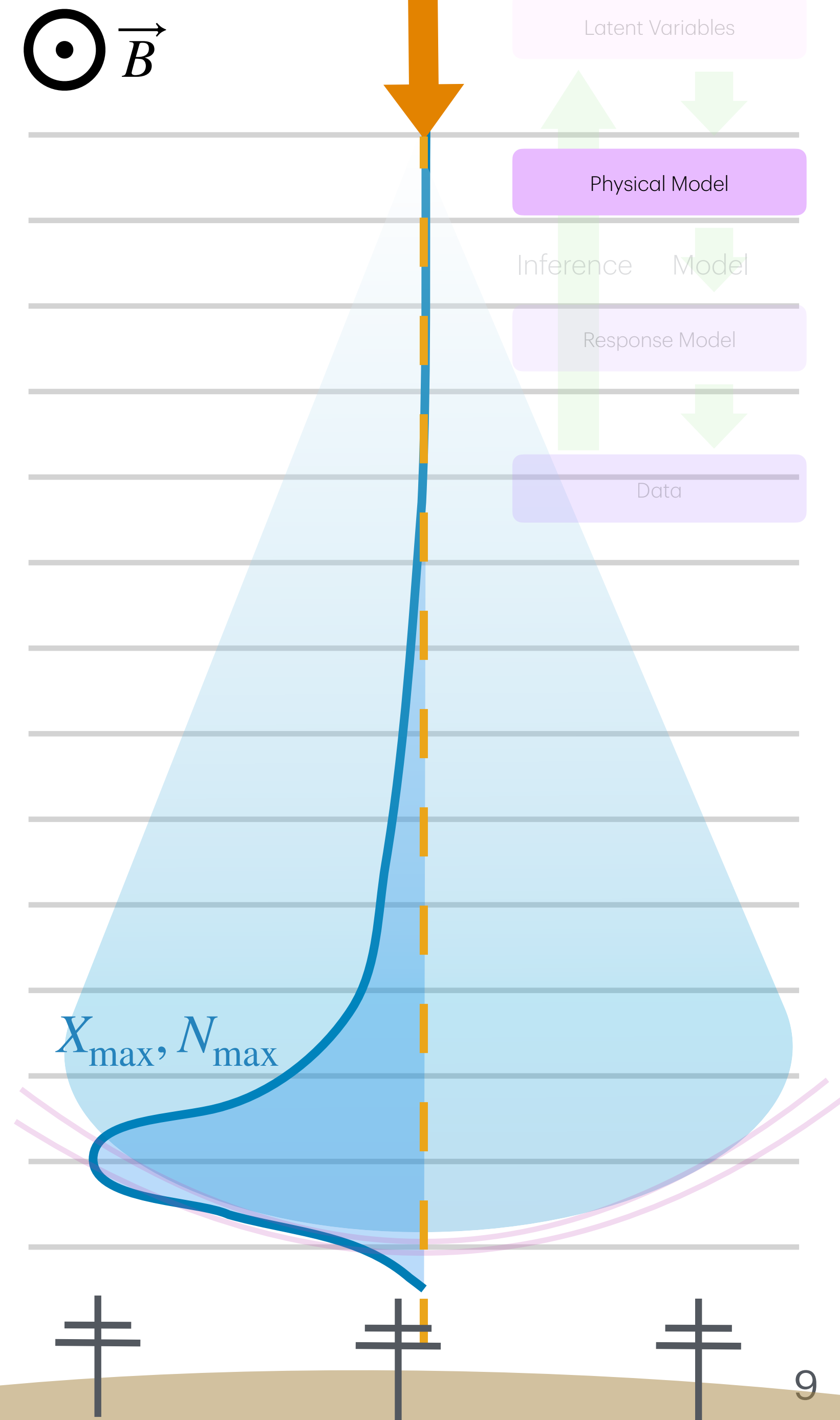
## Template Synthesis (Desmet+ 2024)

2. Calculate amplitude spectrum from **simulated traces** of an **origin shower** for each slice & antenna



Electric field traces of origin shower

$$d_{\text{core}} = 75 \text{ m } [30, 80] \text{ MHz}$$

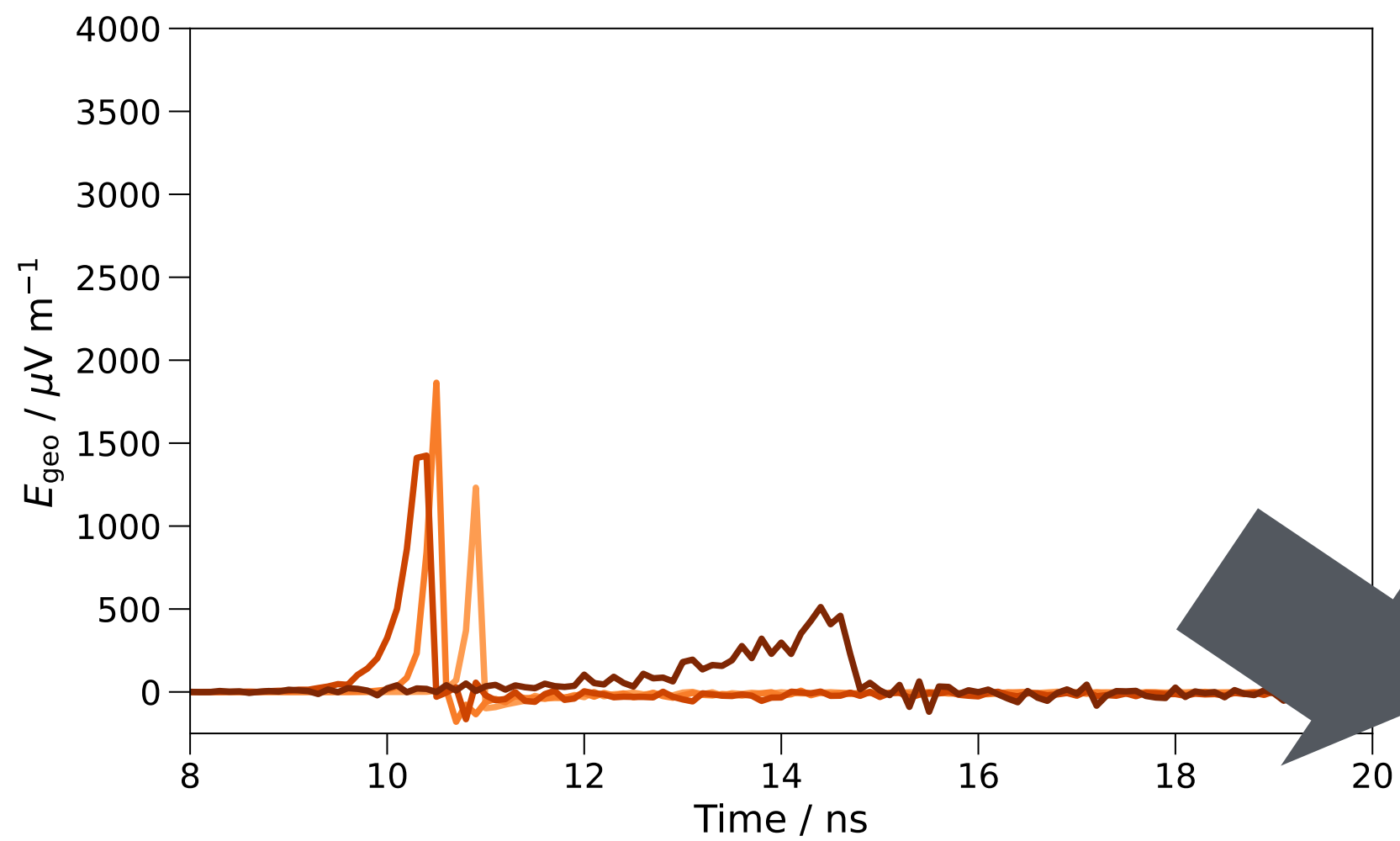




# Radio Emission Model

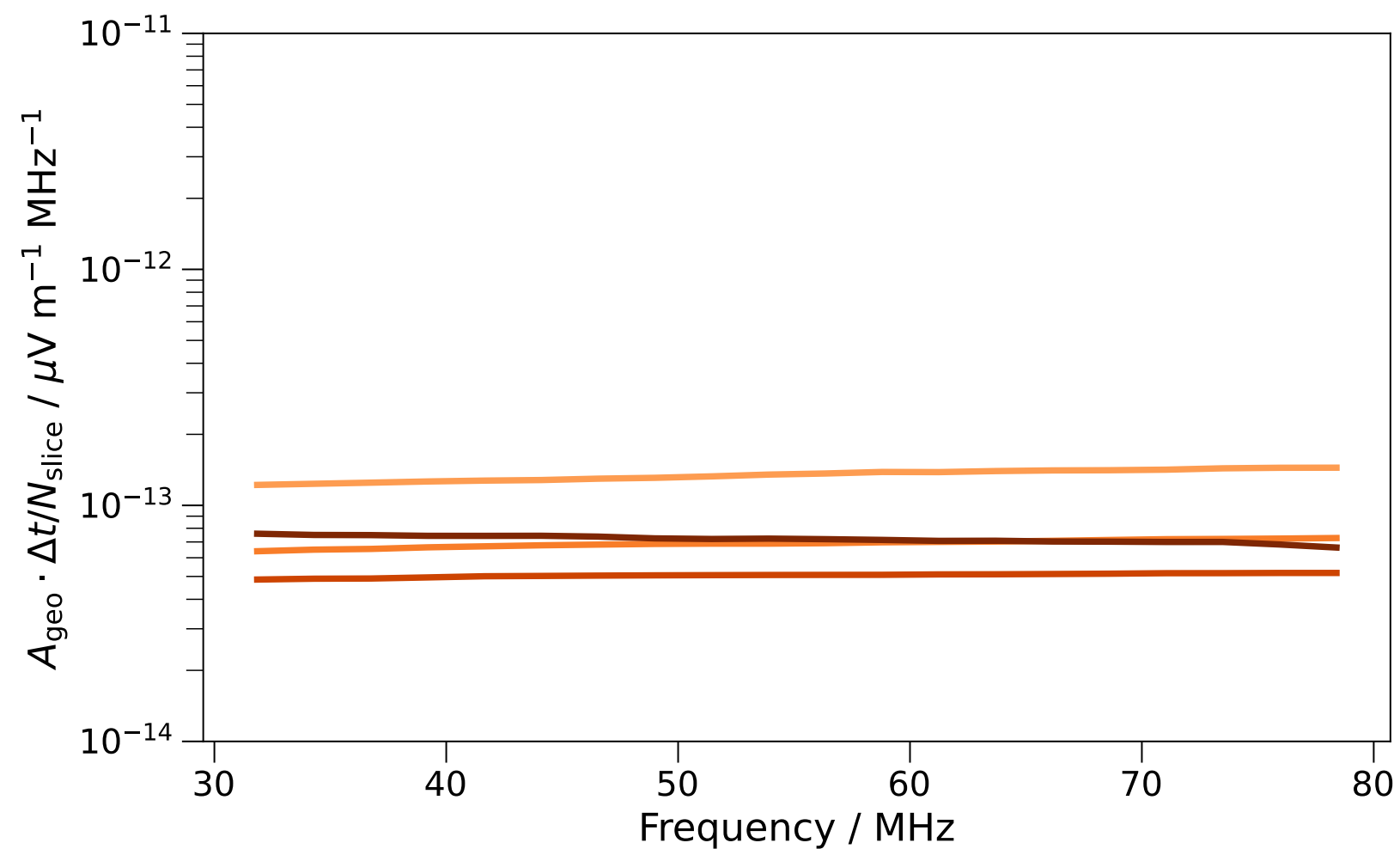
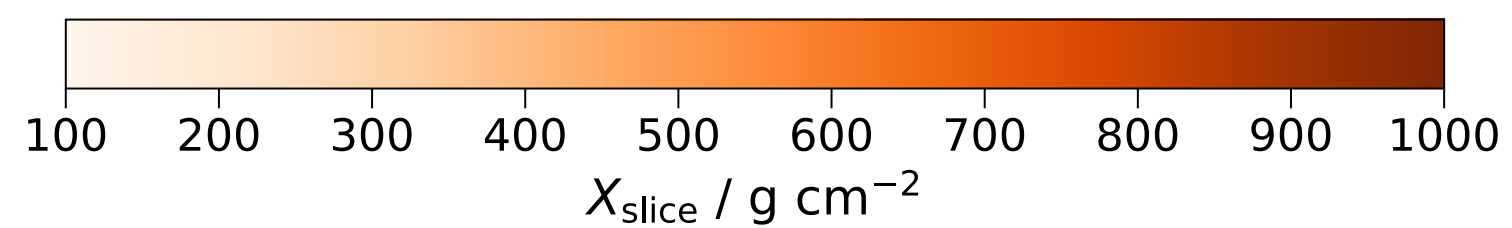
## Template Synthesis (Desmet+ 2024)

2. Calculate amplitude spectrum from **simulated traces** of an **origin shower** for each slice & antenna

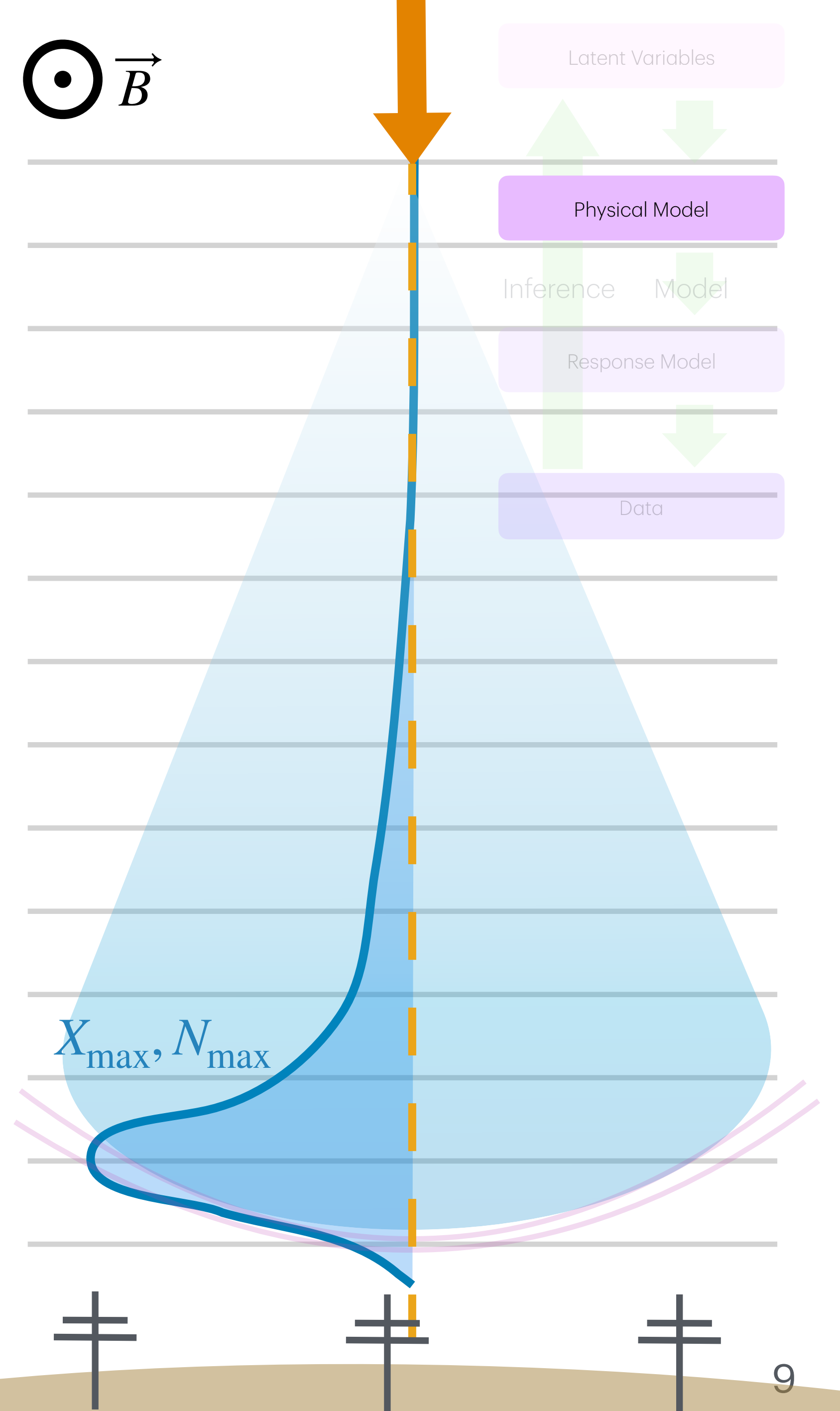


Electric field traces of origin shower

$$d_{\text{core}} = 75 \text{ m } [30, 80] \text{ MHz}$$



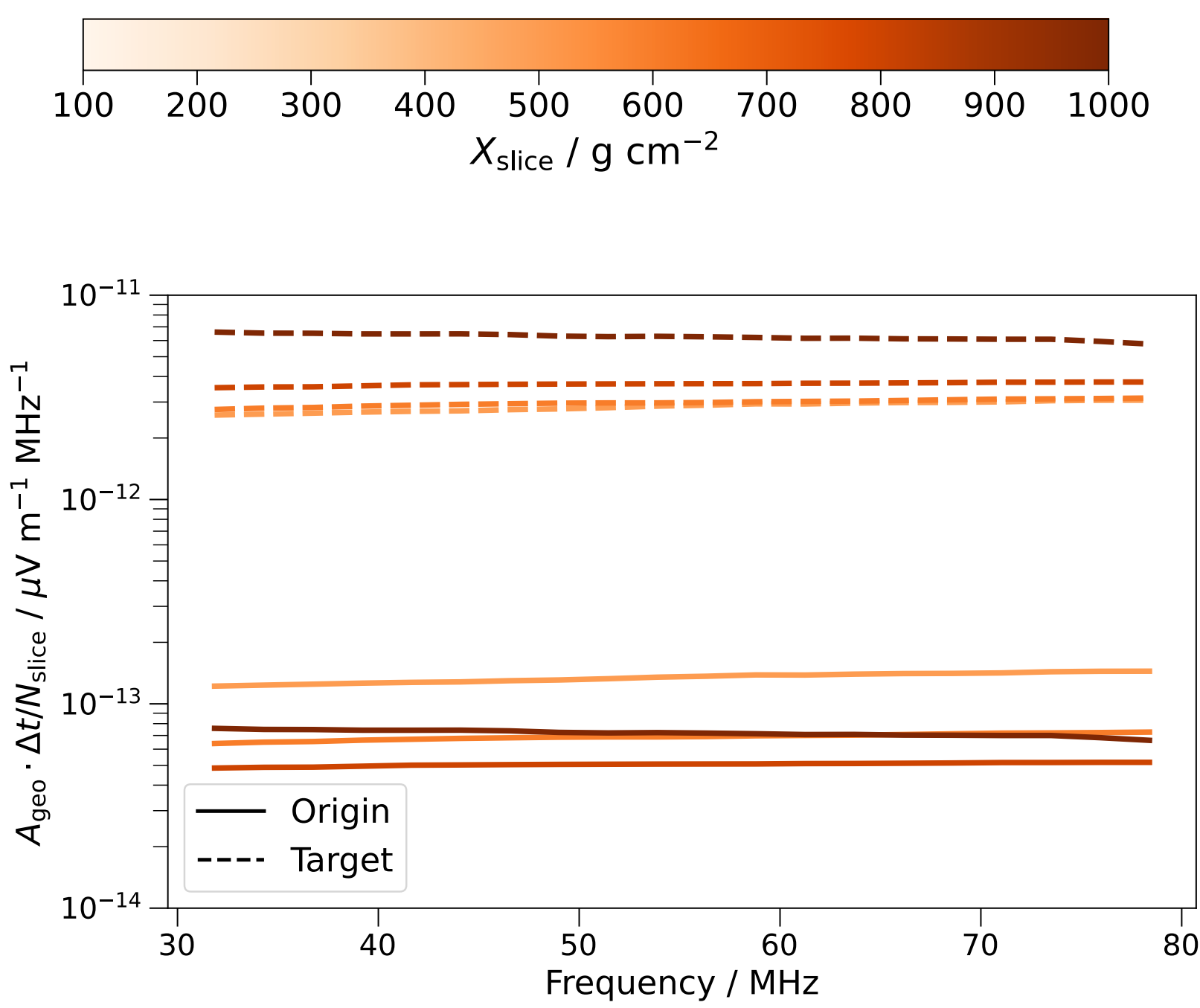
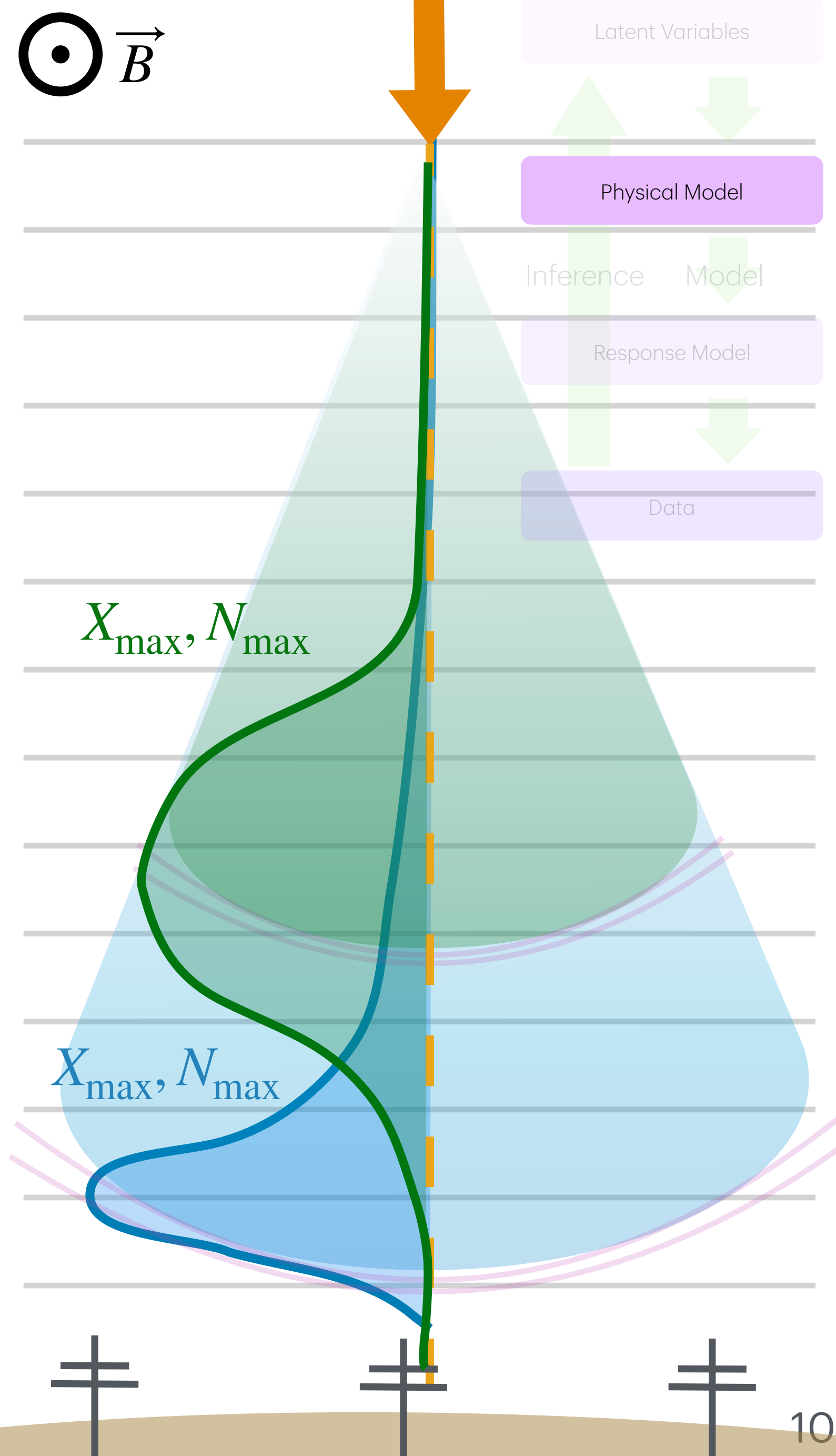
Amplitude spectrum



# Radio Emission Model

## Template Synthesis (Desmet+ 2024)

3. Synthesise emission from **target shower** using relations with origin shower



Solid: Origin Shower  
Dashed: Target Shower

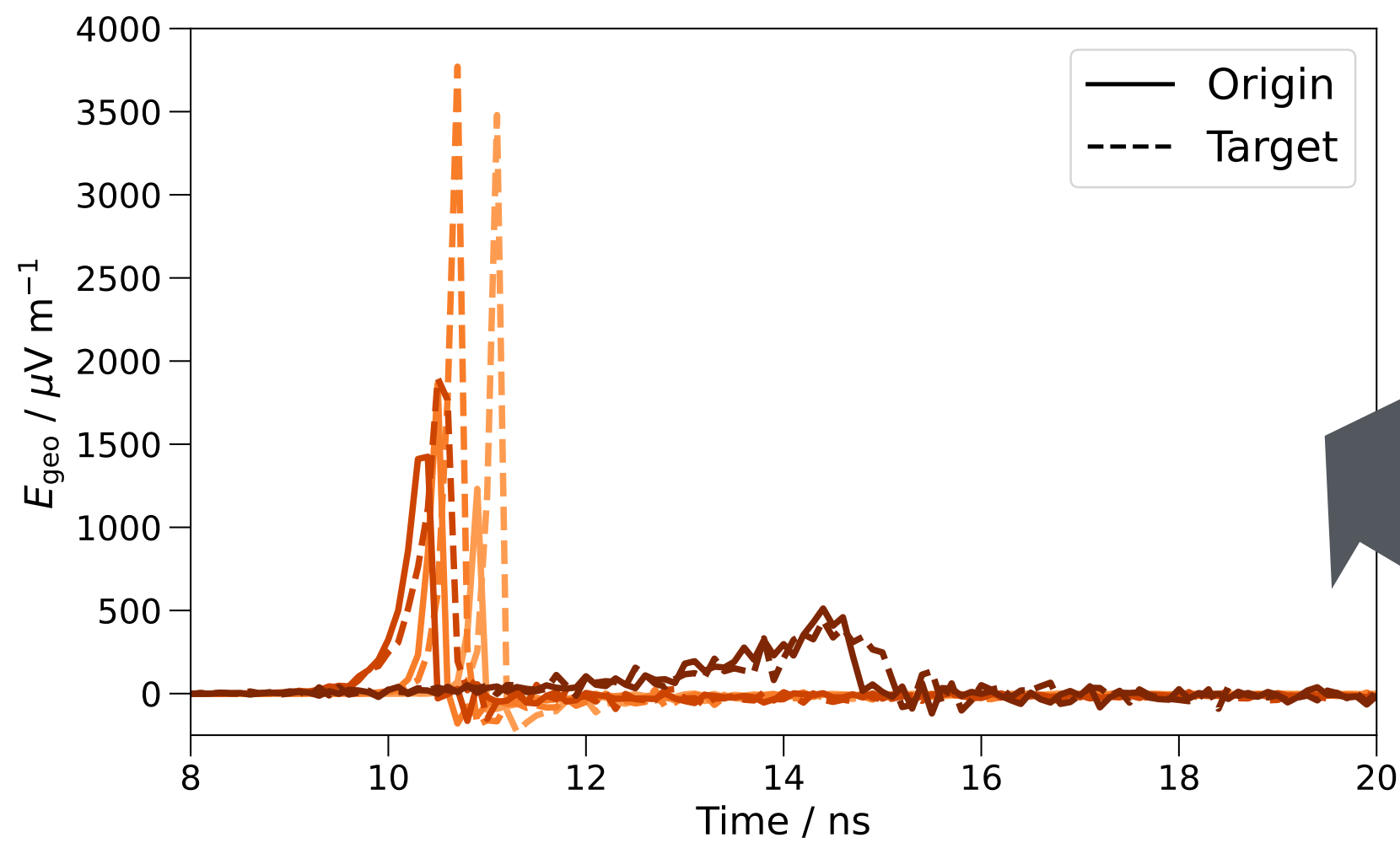
$$d_{\text{core}} = 75 \text{ m } [30, 80] \text{ MHz}$$

Amplitude spectrum

# Radio Emission Model

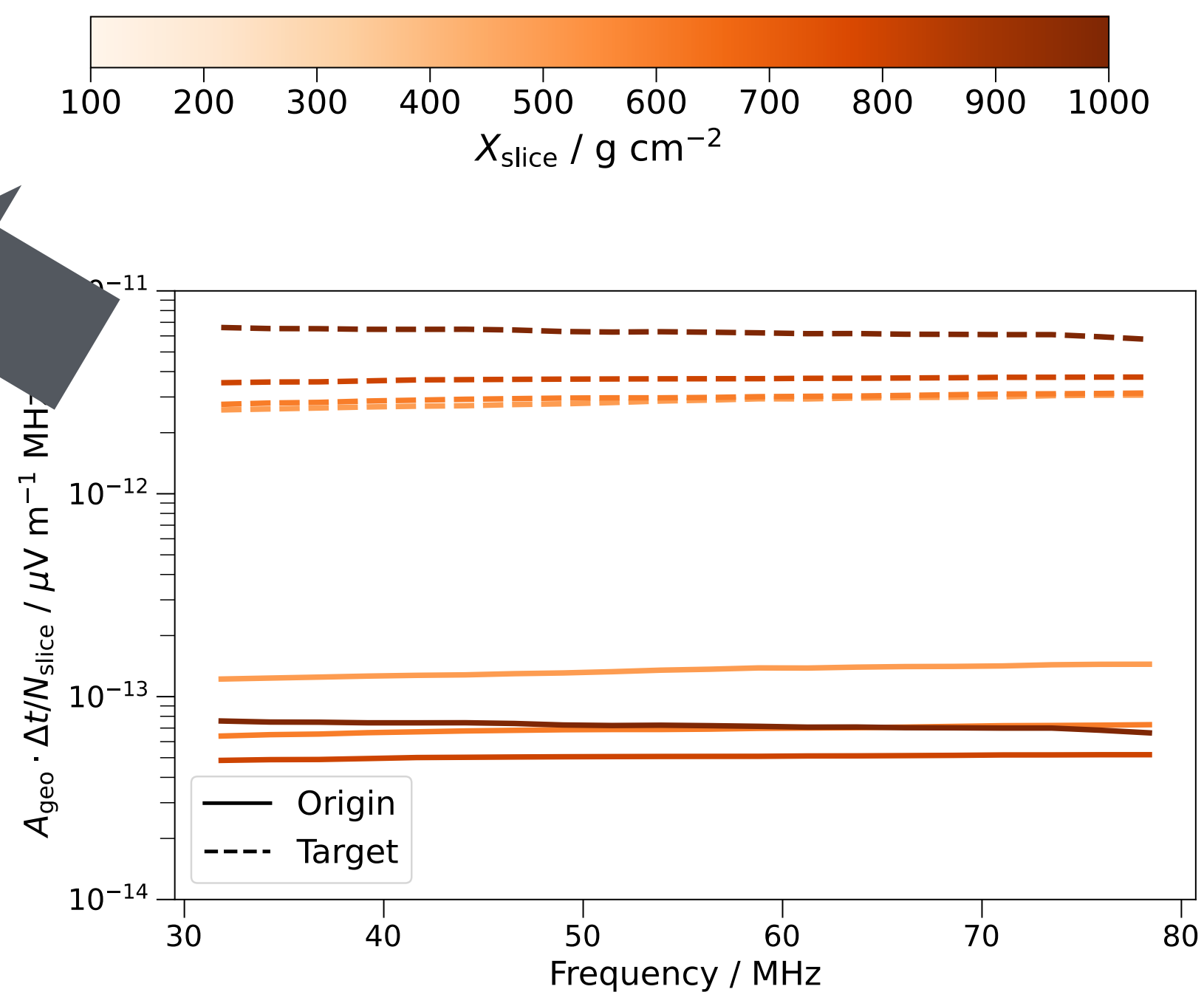
## Template Synthesis (Desmet+ 2024)

3. Synthesise emission from **target shower** using relations with origin shower

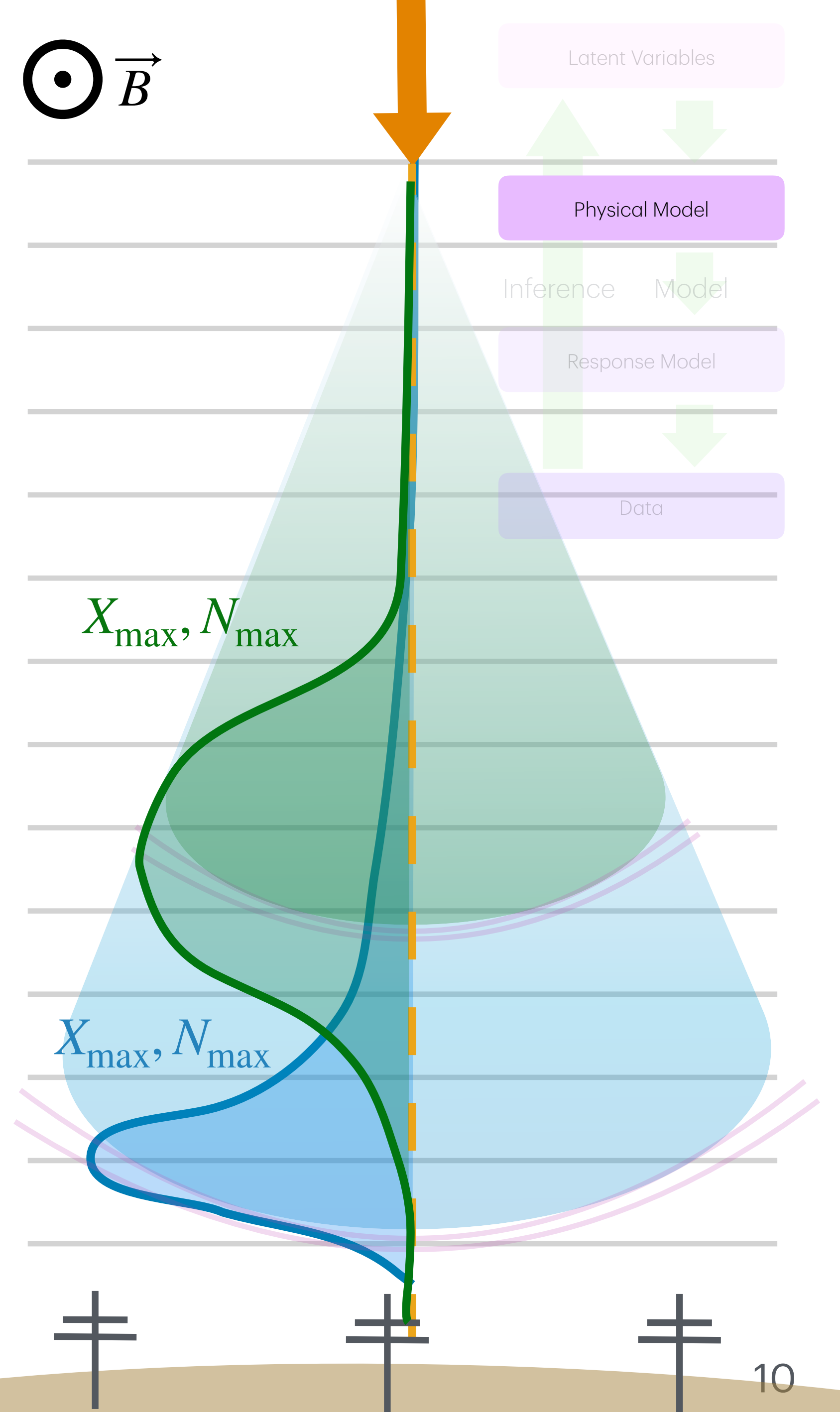


Solid: Origin Shower  
Dashed: Target Shower

$$d_{\text{core}} = 75 \text{ m } [30, 80] \text{ MHz}$$

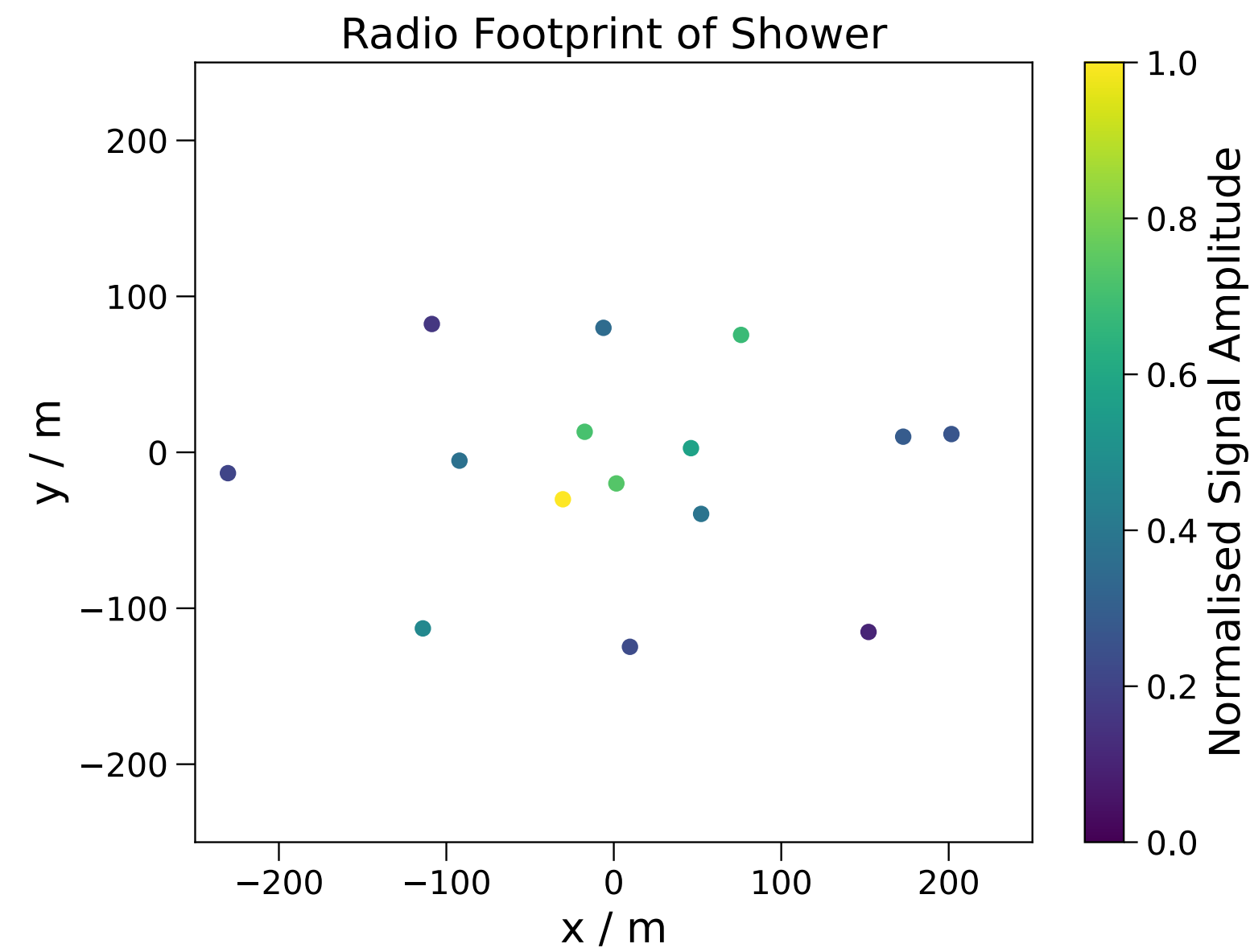
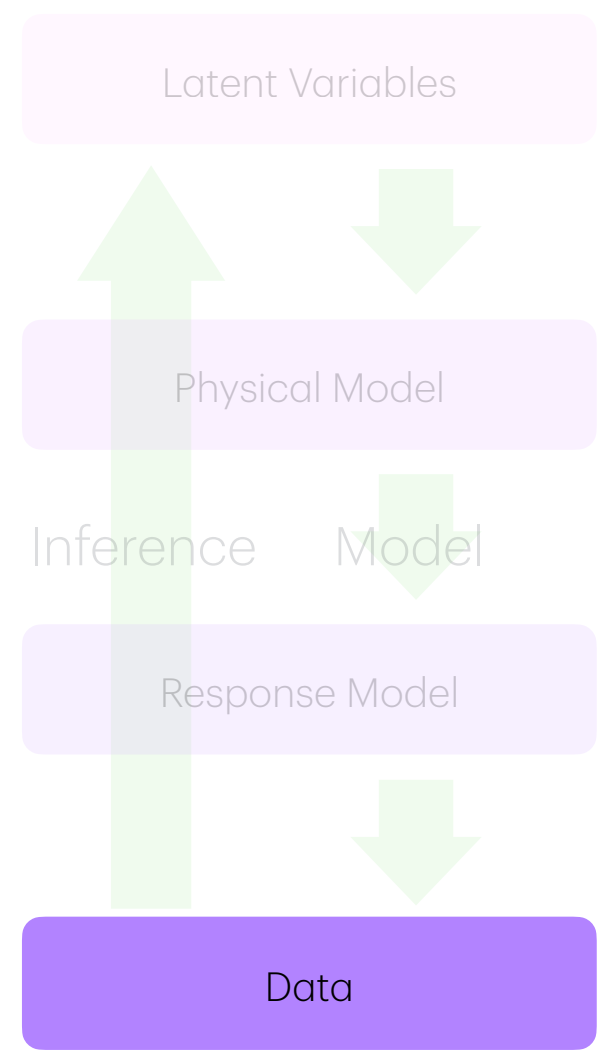


Amplitude spectrum

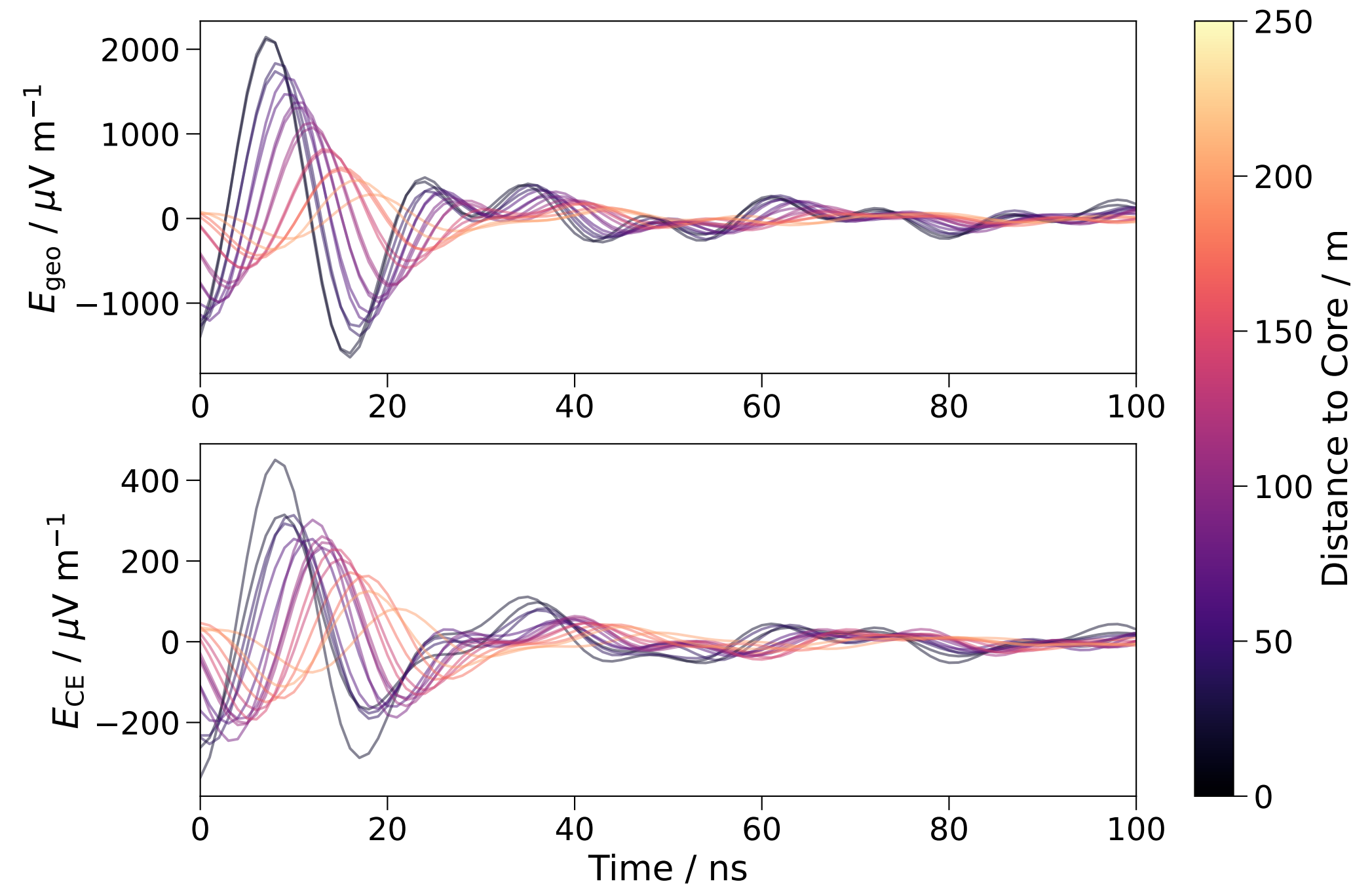


# Verification with Synthetic Data

- **Synthetic data** in **[30, 80] MHz** band, **16 antennas** following star-shape pattern with  $\Delta t = 1$  ns
- **Noise** added through covariance matrix:
  - **3%** of maximum amplitude from **all** antennas (calibration uncertainty)
  - **5%** of maximum amplitude from **each** antenna (antenna-to-antenna uncertainty)



Radio Footprint of Shower

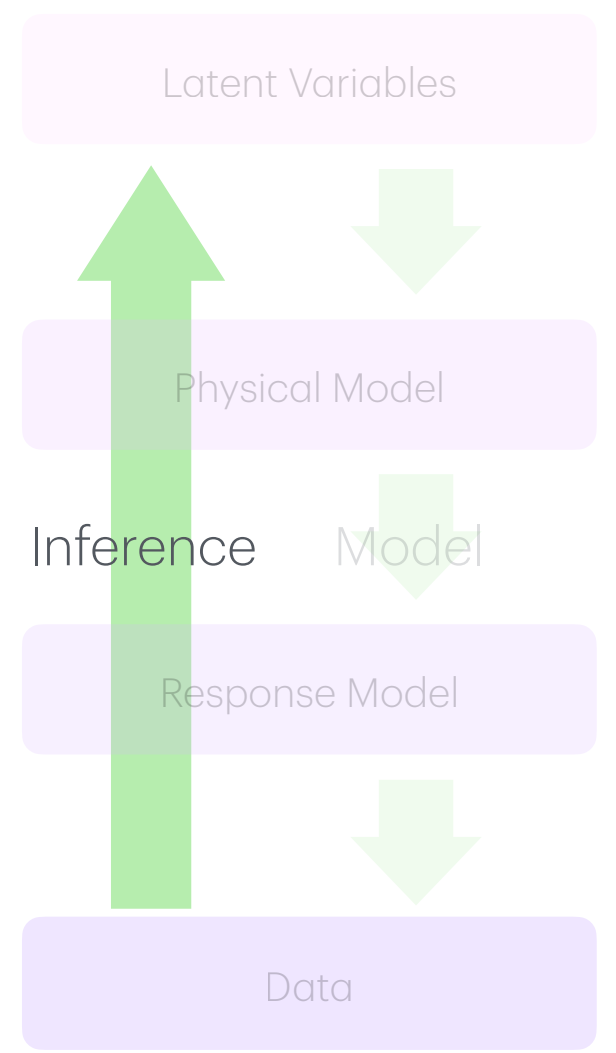
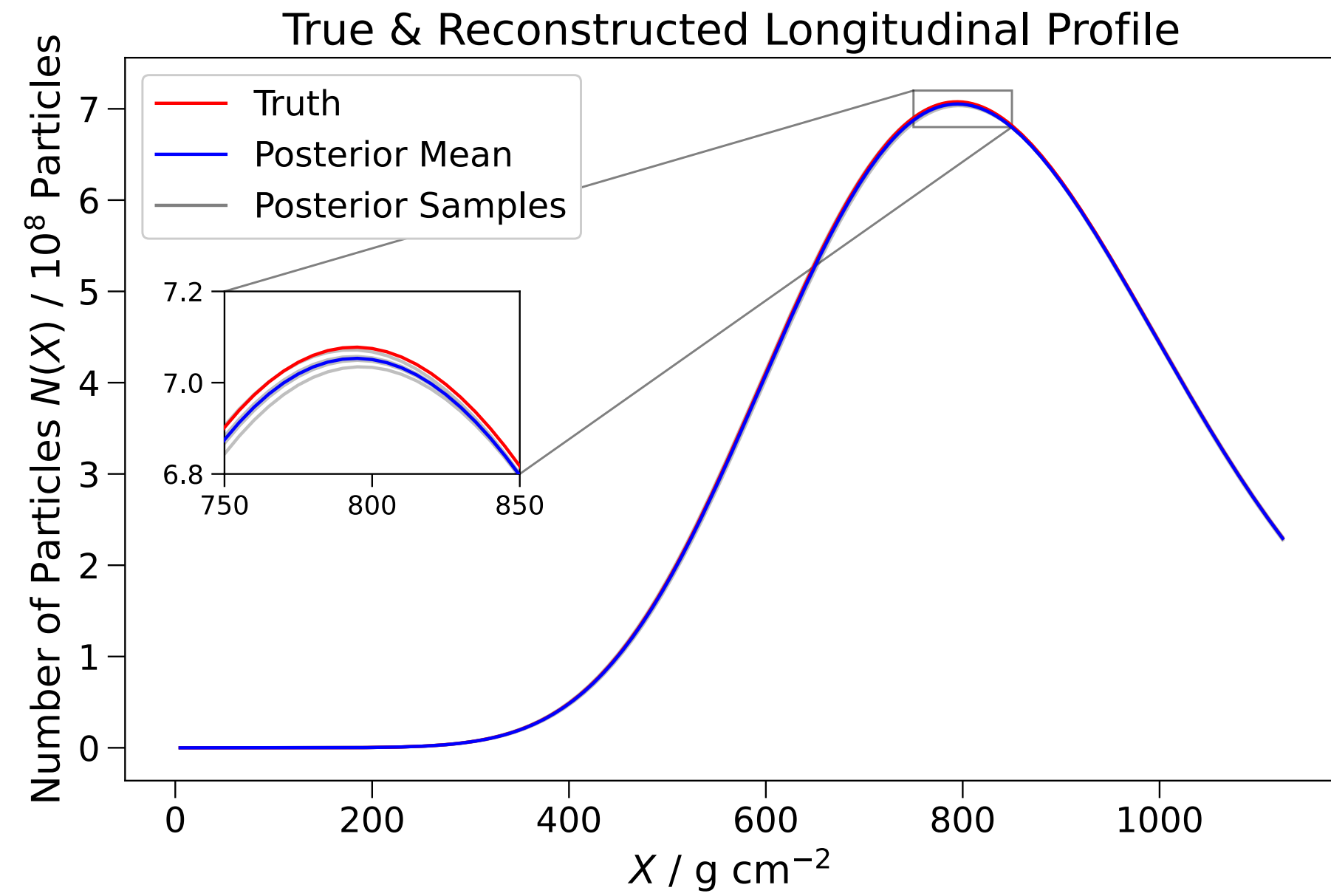
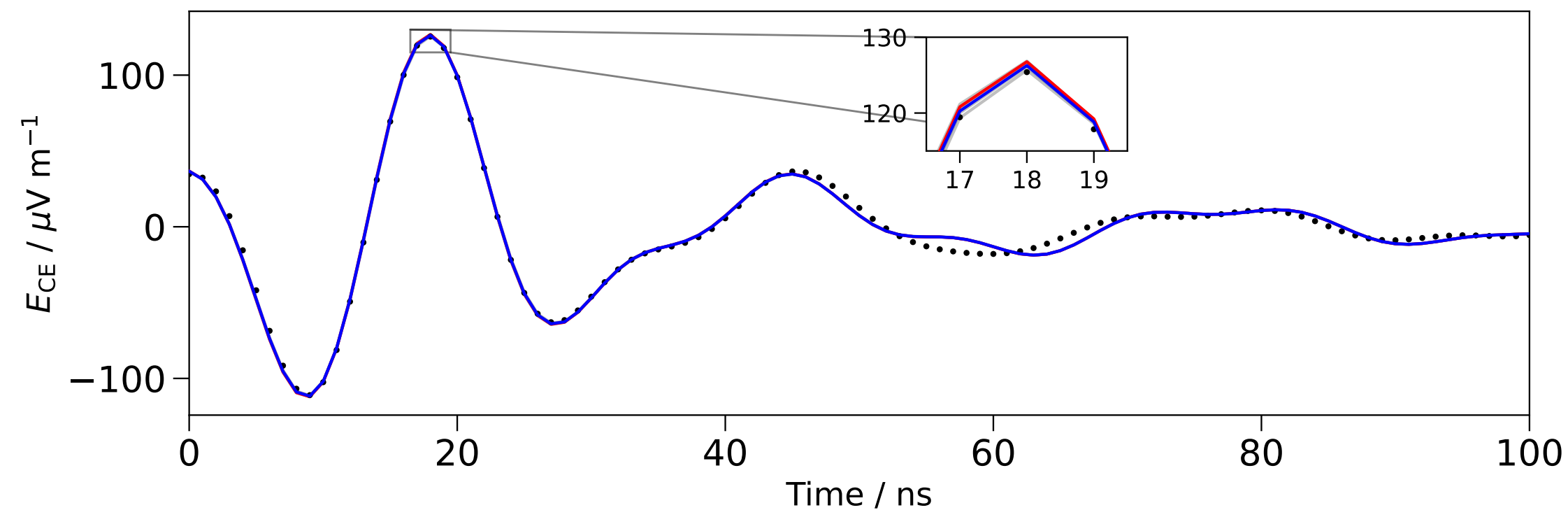
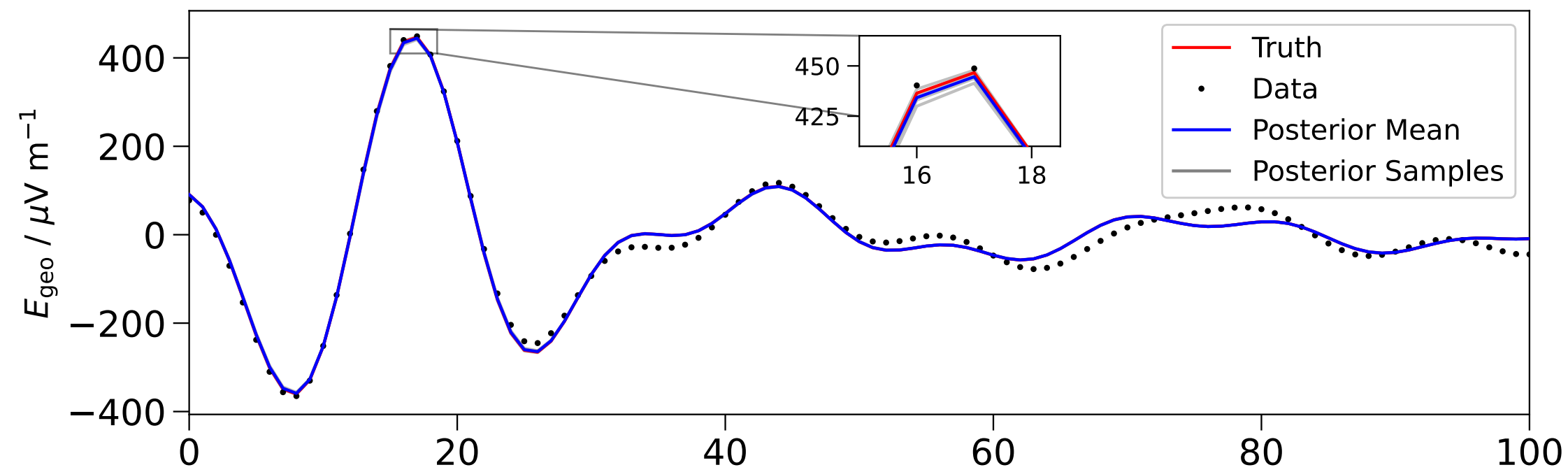


Electric Field Traces of Shower

# Verification with Synthetic Data

- Shower parameters reconstruct well as expected
- Can also reconstruct shower profile / traces from shower parameters

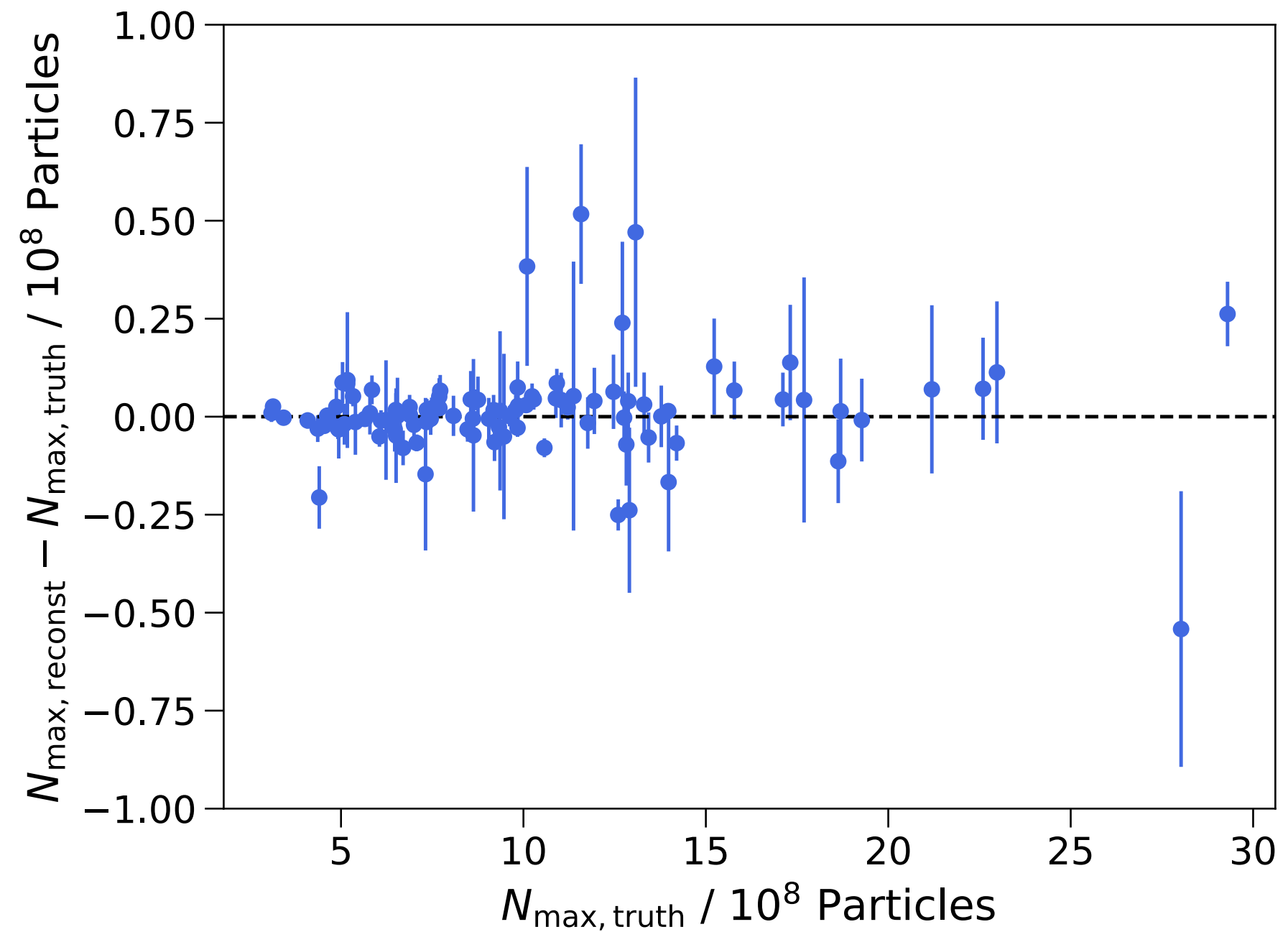
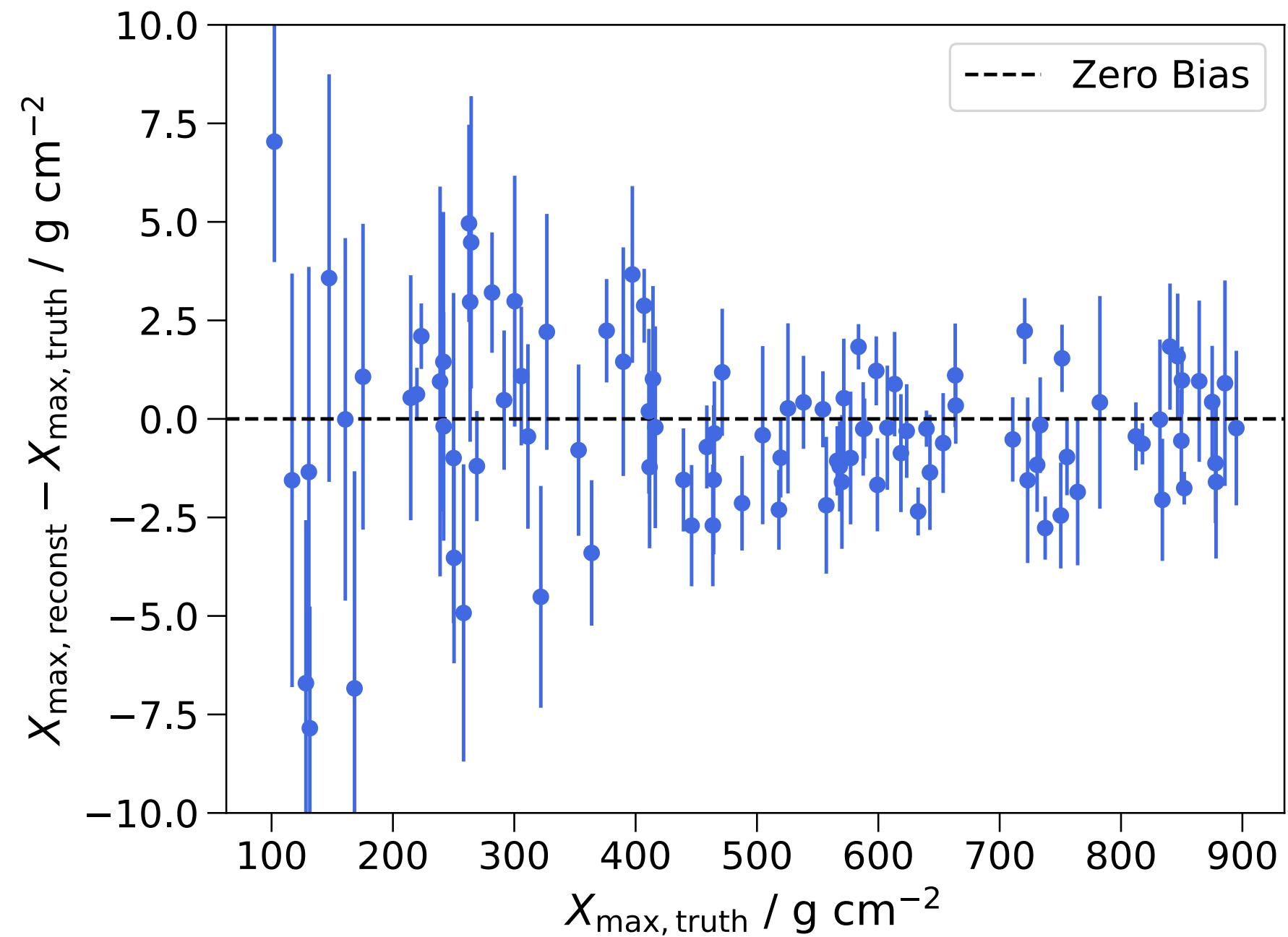
Reconstructed Signal for Antenna with  $d_{\text{core}} = 201.96$  m



	Truth	Reconstructed	$\Delta$
$X_{\text{max}} / \text{g cm}^{-2}$	794.2	$794.6 \pm 1.4$	-0.38
$N_{\text{max}} / 10^8$	7.078	$7.056 \pm 0.016$	0.025

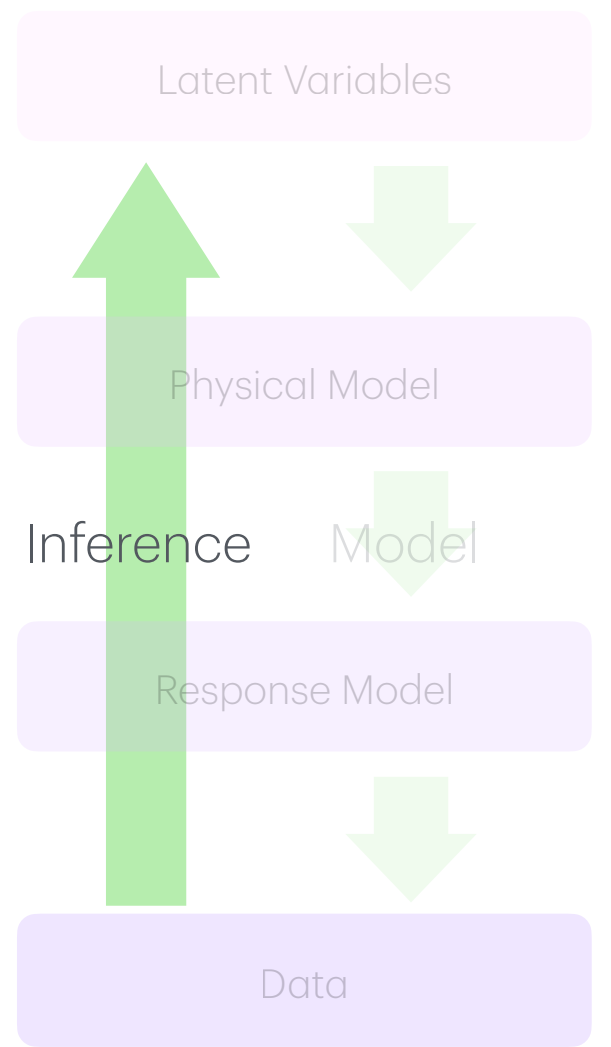
# Verification with Synthetic Data

- Testing reconstruction bias with 100 synthetically generated showers



$X_{\max}$  reconstruction bias of  $\lesssim 8 \text{ g cm}^{-2}$ , comparable with classical reconstruction methods

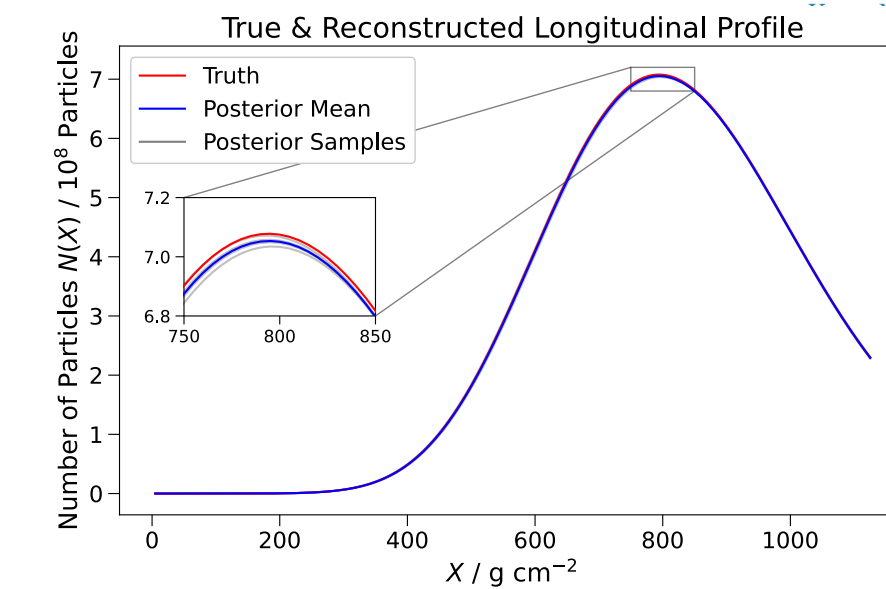
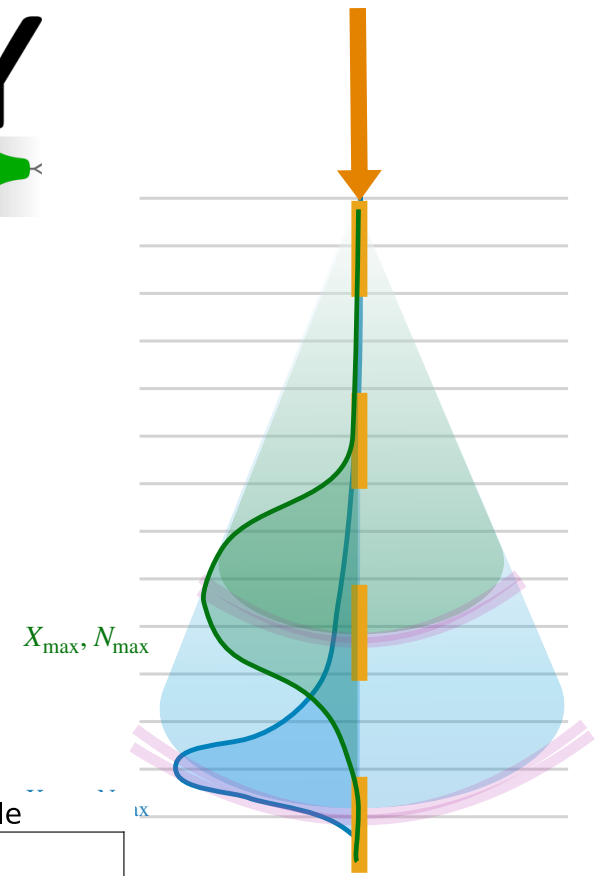
$\implies$  but need to include antenna response & realistic noise model for further interpretation (see K. Terveer's talk)



# Conclusion & Outlook

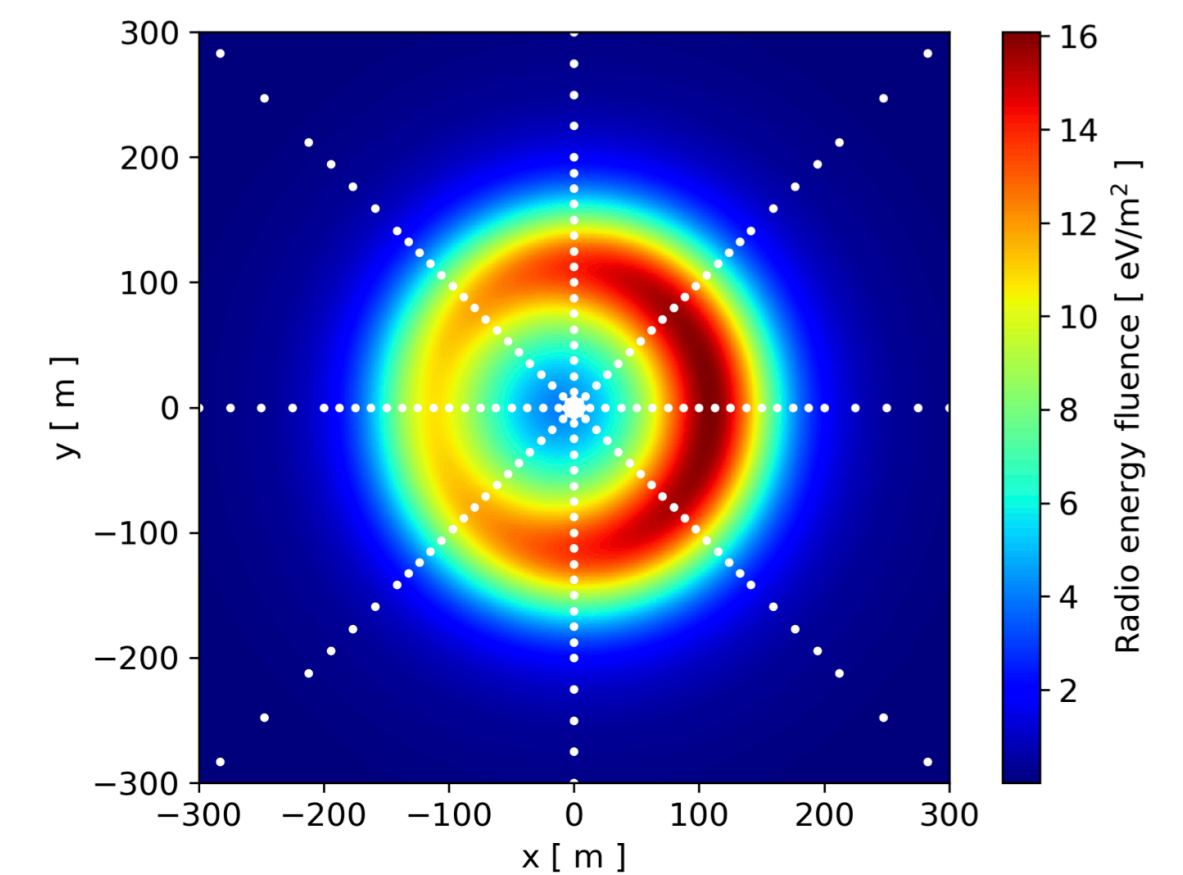
- **Goal:** use **Information Field Theory** for reconstruction of shower profile
- Utilised fast-forward model for radio emission: **template synthesis**
- Preliminary results show accurate reconstruction of  $X_{\max}$  and  $N_{\max}$

**NIFTY**



## Outlook

- Generalise for arbitrary antenna positions (Fourier interpolation)
- Include antenna response & realistic noise model
- Apply to realistic simulated data & to LOFAR data
- Reconstruct full shower profile instead of shower parameters



A. Corstanje et al. 2023 JINST 18 P09005

Backup Slides



# Square Kilometre Array

Reconstruction of **full air shower profile** possible with Square Kilometre Array (SKA)

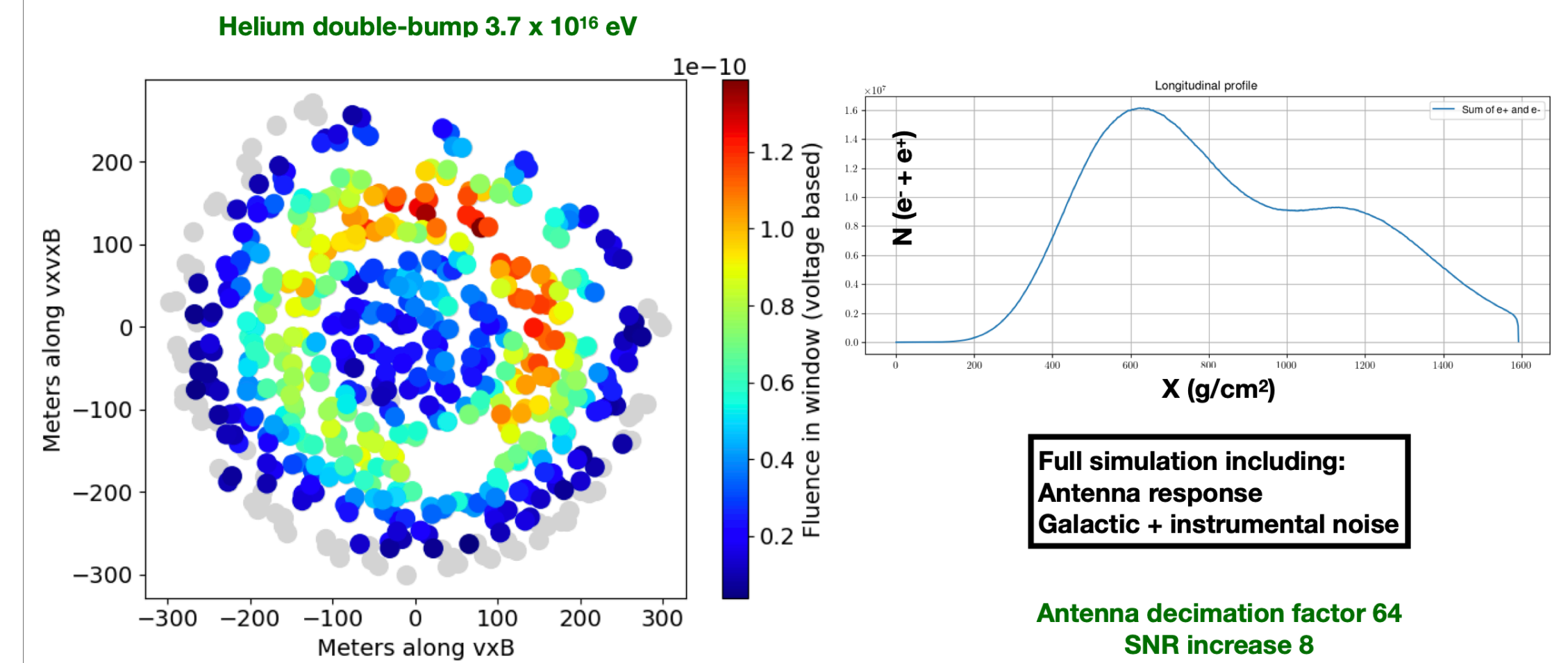
- ~ **60,000** antennas planned within ~ 1 km<sup>2</sup>
- Planned bandwidth from **50 - 350 MHz**
- $X_{\max}$  reconstruction with SKA simulations show resolution of **6-8 g cm<sup>-2</sup>** (LOFAR: 20 g cm<sup>-2</sup>)
- Also possible to reconstruct L, R parameters, double-bump showers & possibly PeV gamma-rays



The first 2 complete stations with 512 antennas, deployed at Murchison Radio-astronomy Observatory

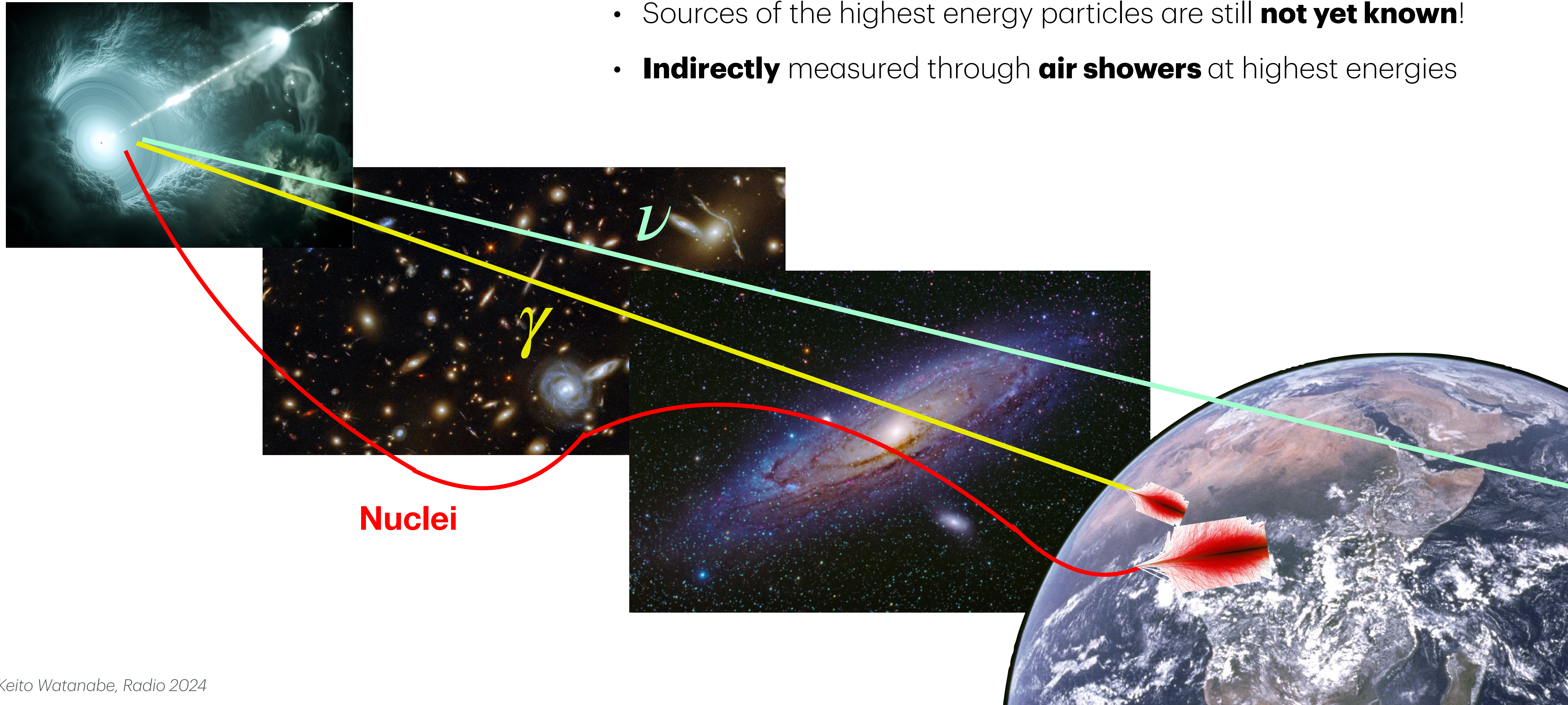


SKALA : SKA log-periodic antenna



# Cosmic Rays

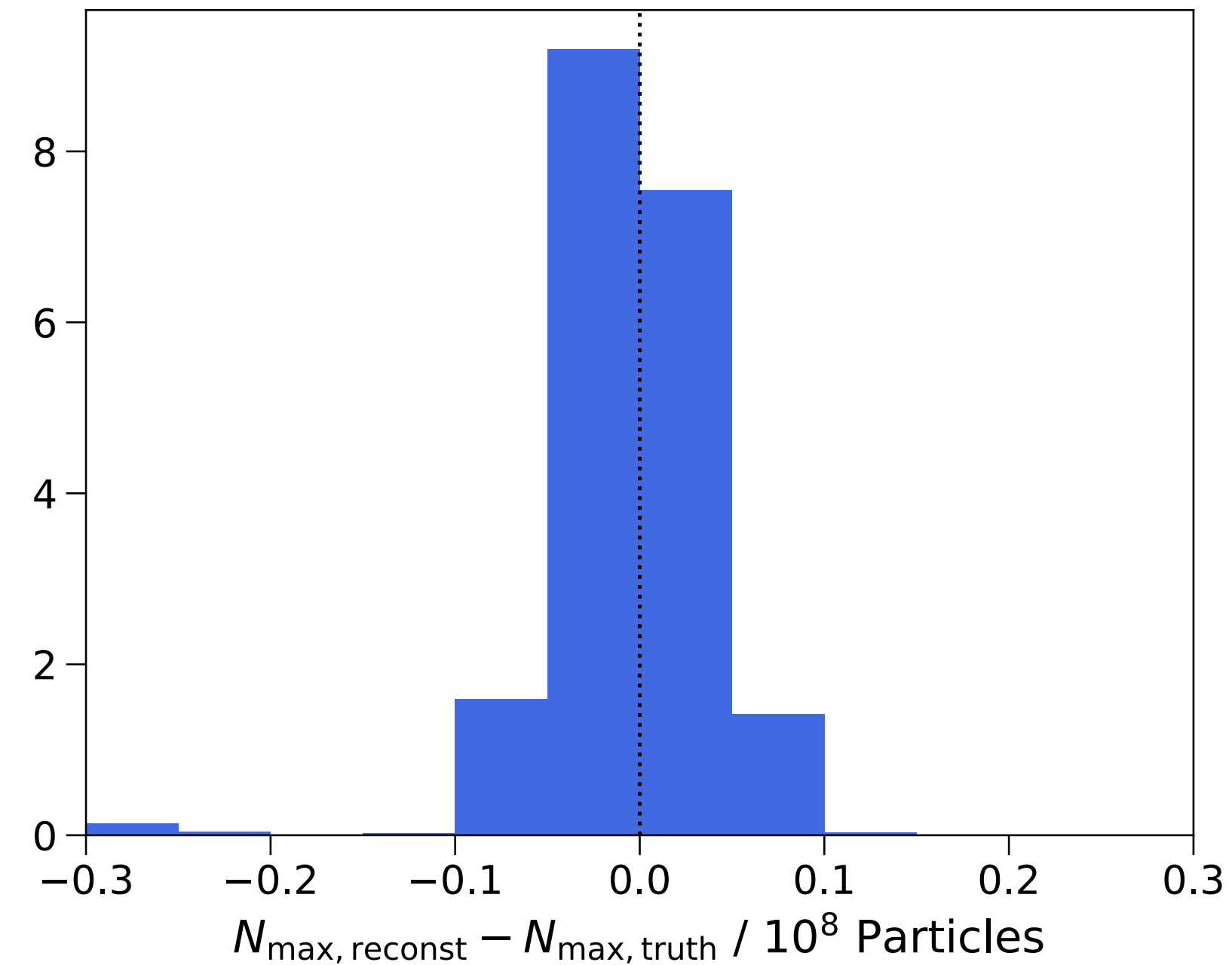
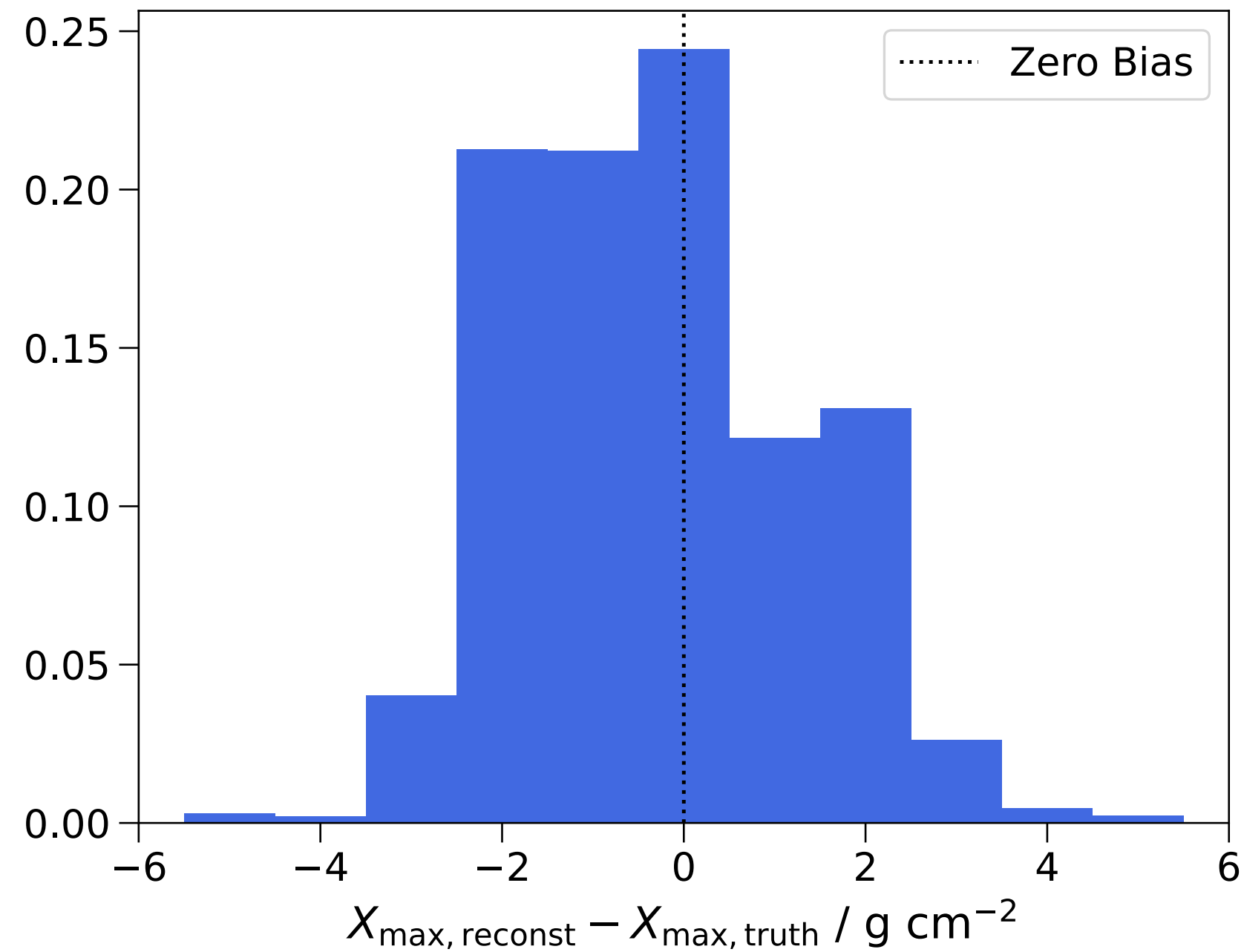
- **Highly energetic particles** (nuclei,  $\gamma$ -rays, neutrinos) that are from astrophysical origin
- Sources of the highest energy particles are still **not yet known!**
- **Indirectly** measured through **air showers** at highest energies



**Nuclei**

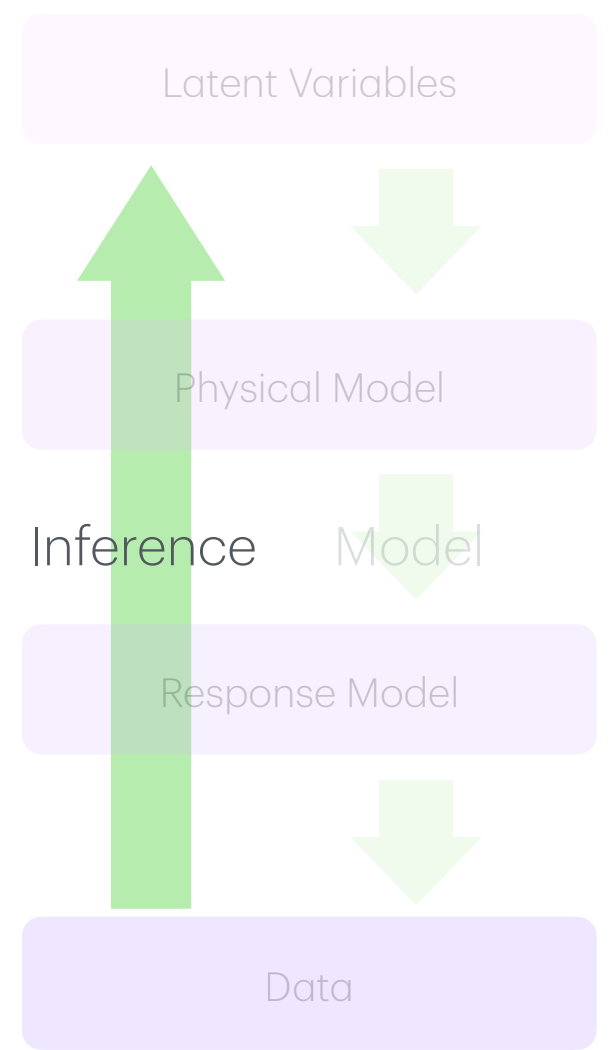
# Verification with Synthetic Data

- Testing reconstruction bias with 100 synthetically generated showers



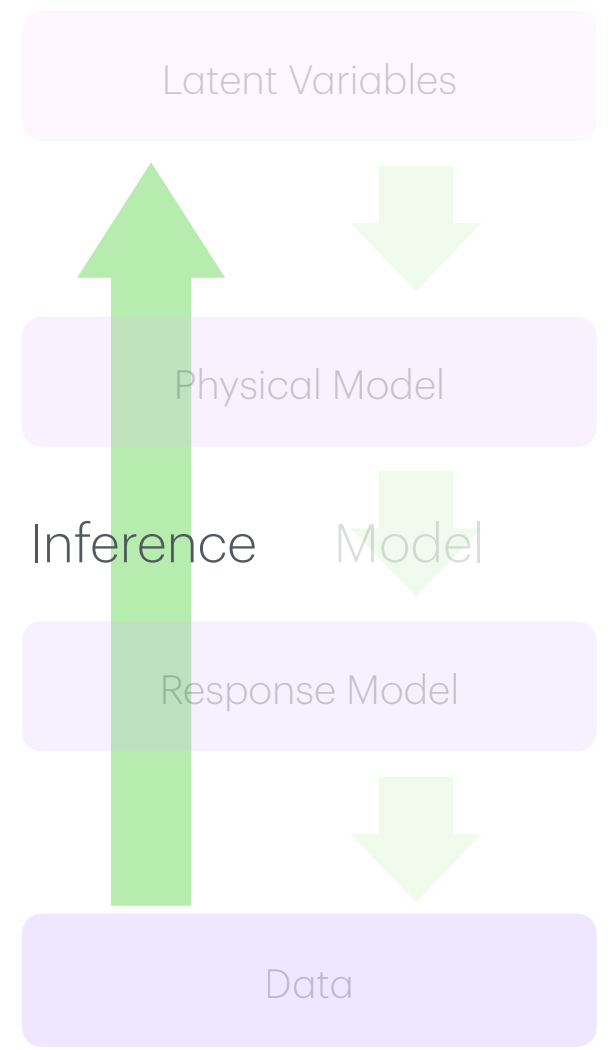
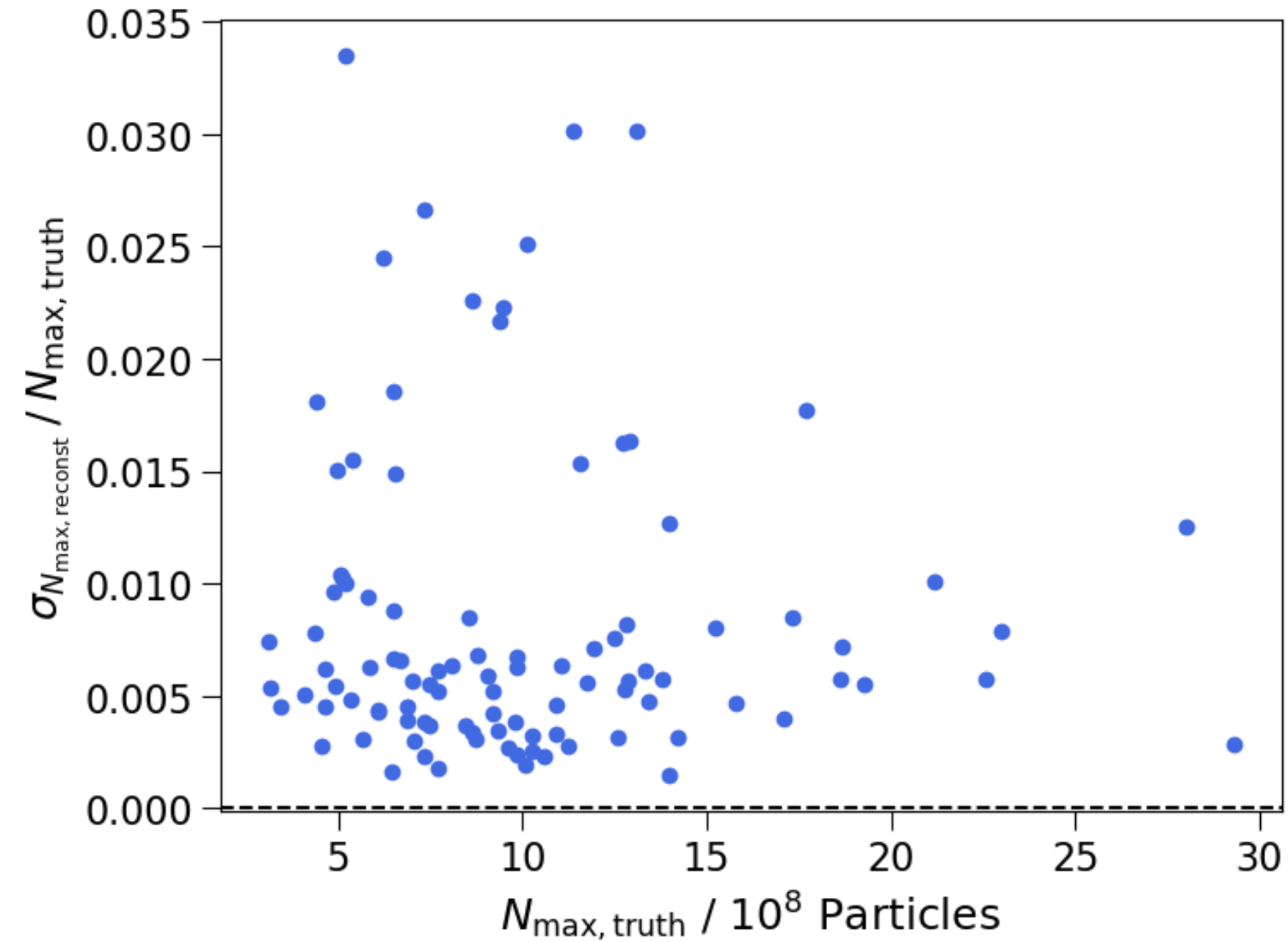
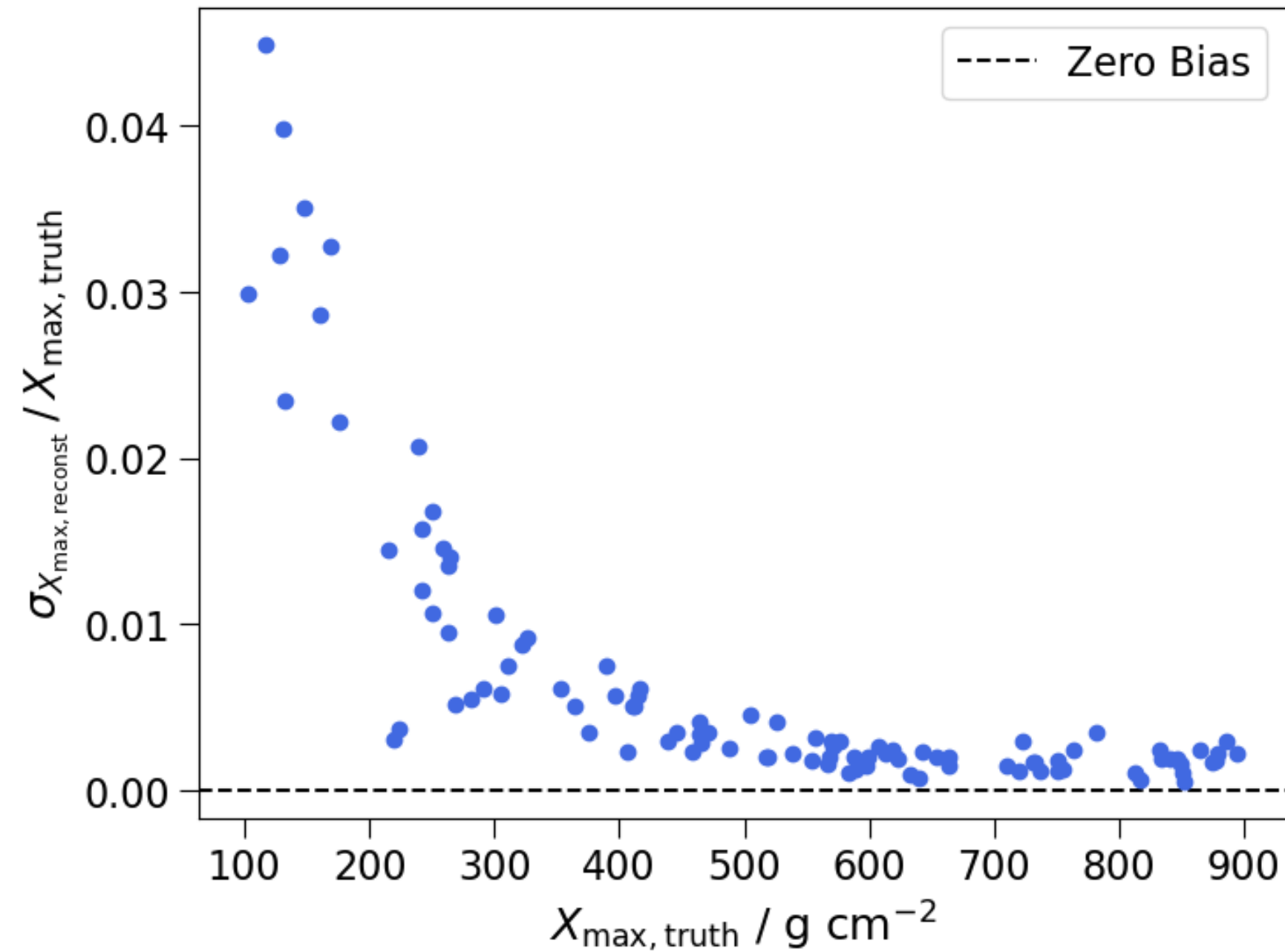
$X_{\max}$  reconstruction bias of  $\lesssim 8 \text{ g cm}^{-2}$ , comparable with classical reconstruction methods

$\implies$  but need to include antenna response & realistic noise model for further interpretation!



# Verification with Synthetic Data

- Reconstruction Efficiency with 100 synthetically generated showers



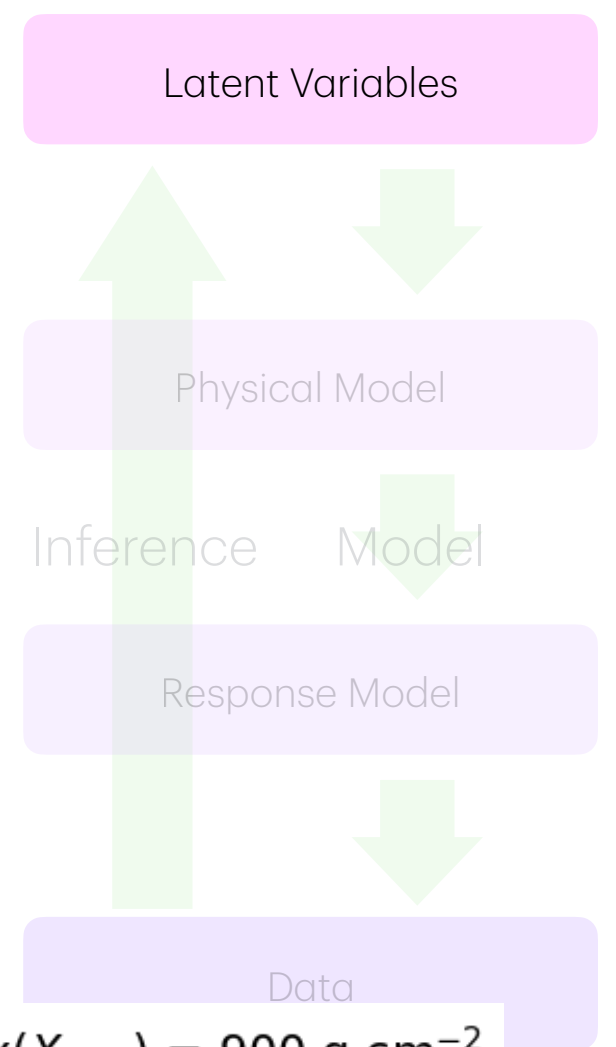
$X_{\max}$  reconstruction efficiency increases with lower  $X_{\max}$ , but still  $< 4\%$

$\implies$  but need to include antenna response & realistic noise model for further interpretation!

# Prior Model

- Distribution to sample physical observables for reconstruction

- Sample each latent parameter  $\xi$  as unit Gaussian  $\rightarrow$  transform to  $X_{\max}, N_{\max}$



$$\xi_{X_{\max}} \sim \mathcal{N}(0,1)$$

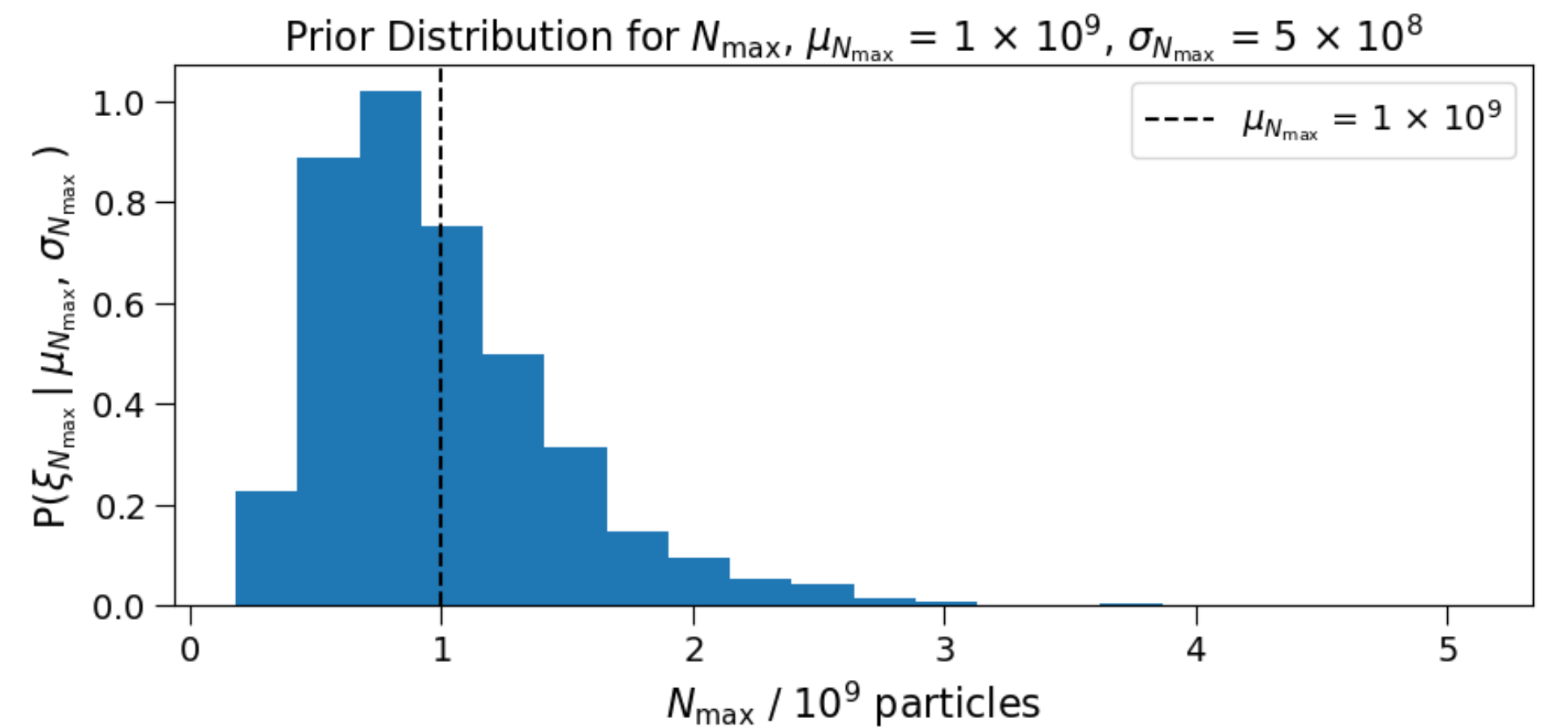
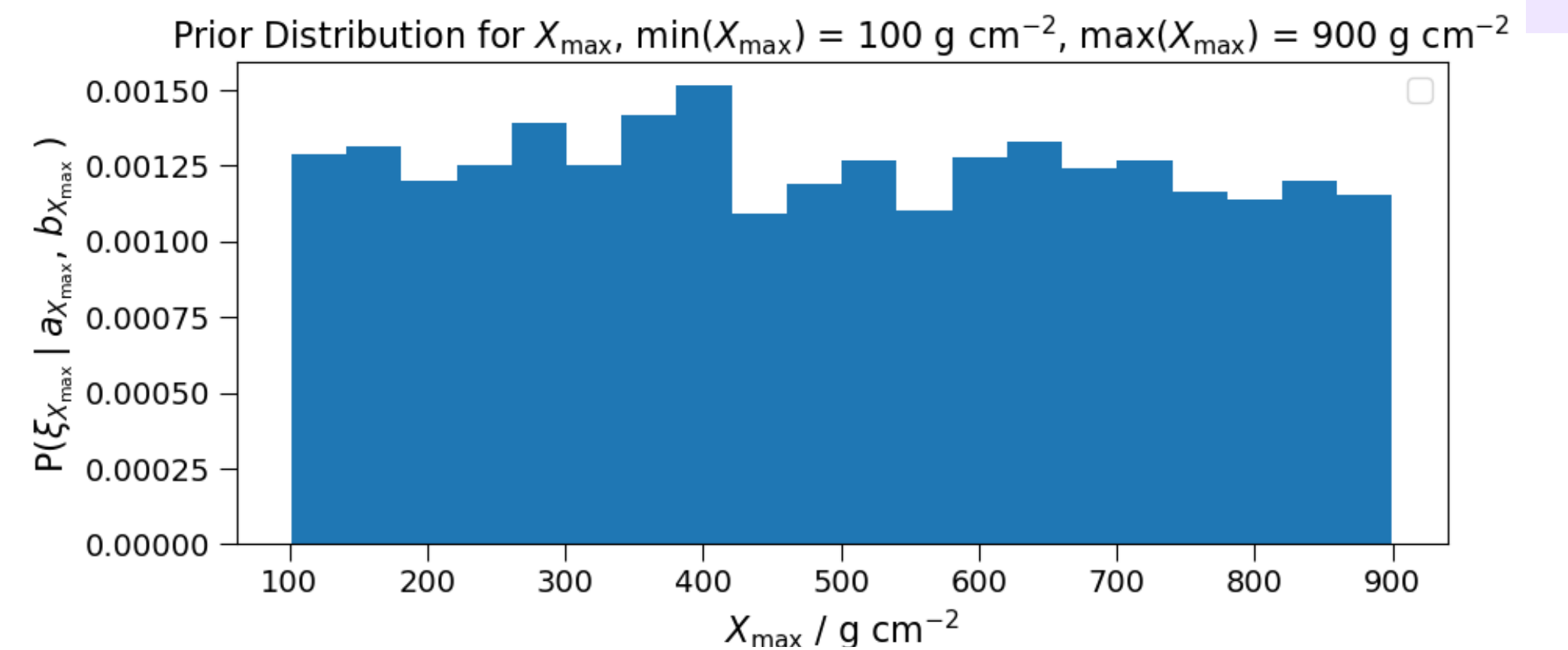
$$X_{\max} \sim P(\xi_{X_{\max}} \mid \min(X_{\max}), \max(X_{\max}))$$

$$\xi_{N_{\max}} \sim \mathcal{N}(0,1)$$

$$N_{\max} \sim P(\xi_{N_{\max}} \mid \mu_{N_{\max}}, \sigma_{N_{\max}})$$

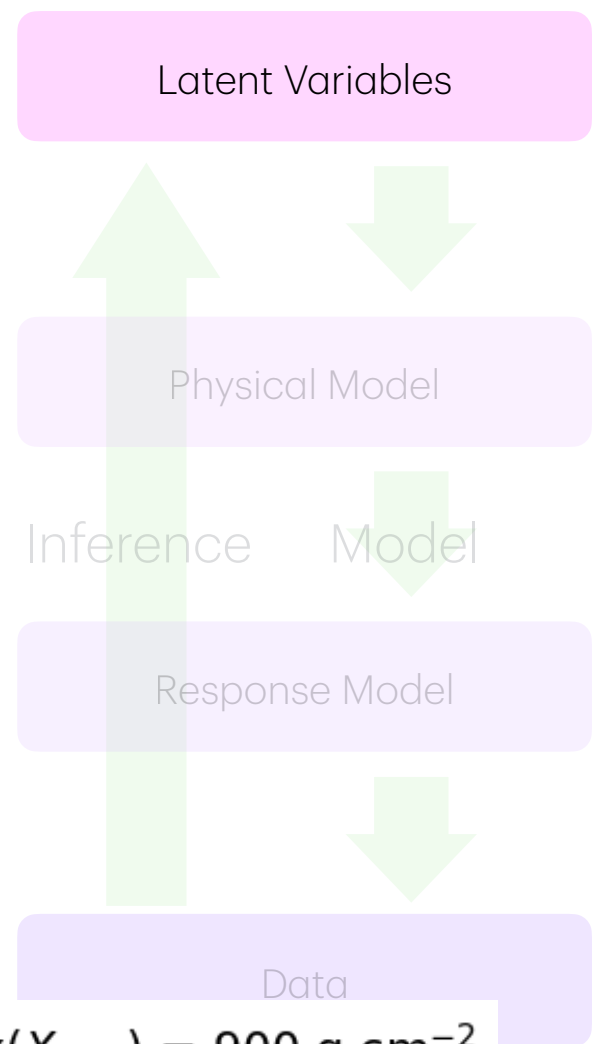
$X_{\max}$  : atmospheric depth at shower maximum

$N_{\max}$  : number of particles at  $X_{\max}$



# Prior Model

- Distribution to sample physical observables for reconstruction
- Sample each latent parameter  $\xi$  as unit Gaussian  $\rightarrow$  transform to  $X_{\max}, N_{\max}$



$$\xi_{X_{\max}} \sim \mathcal{N}(0,1)$$

$$X_{\max} \sim P(\xi_{X_{\max}} \mid \min(X_{\max}), \max(X_{\max}))$$

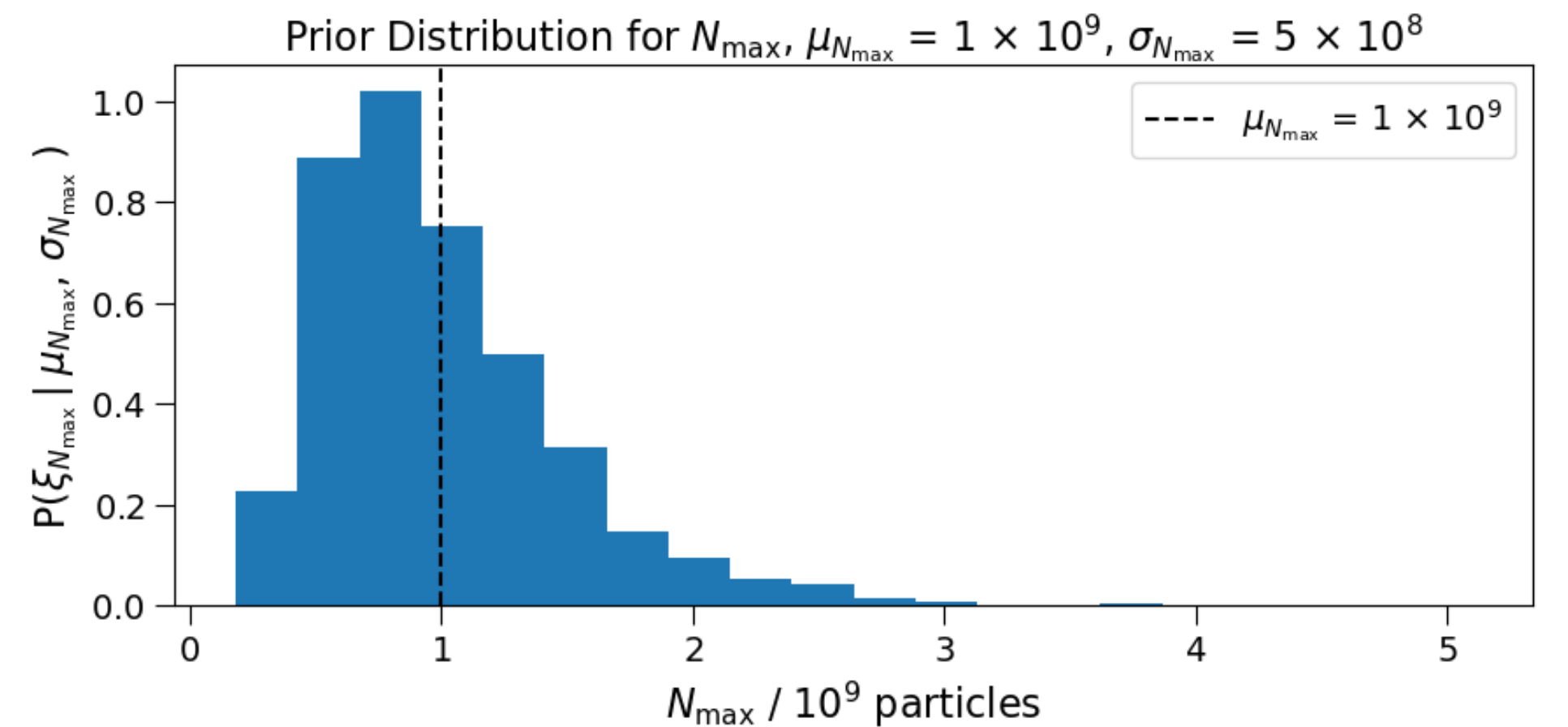
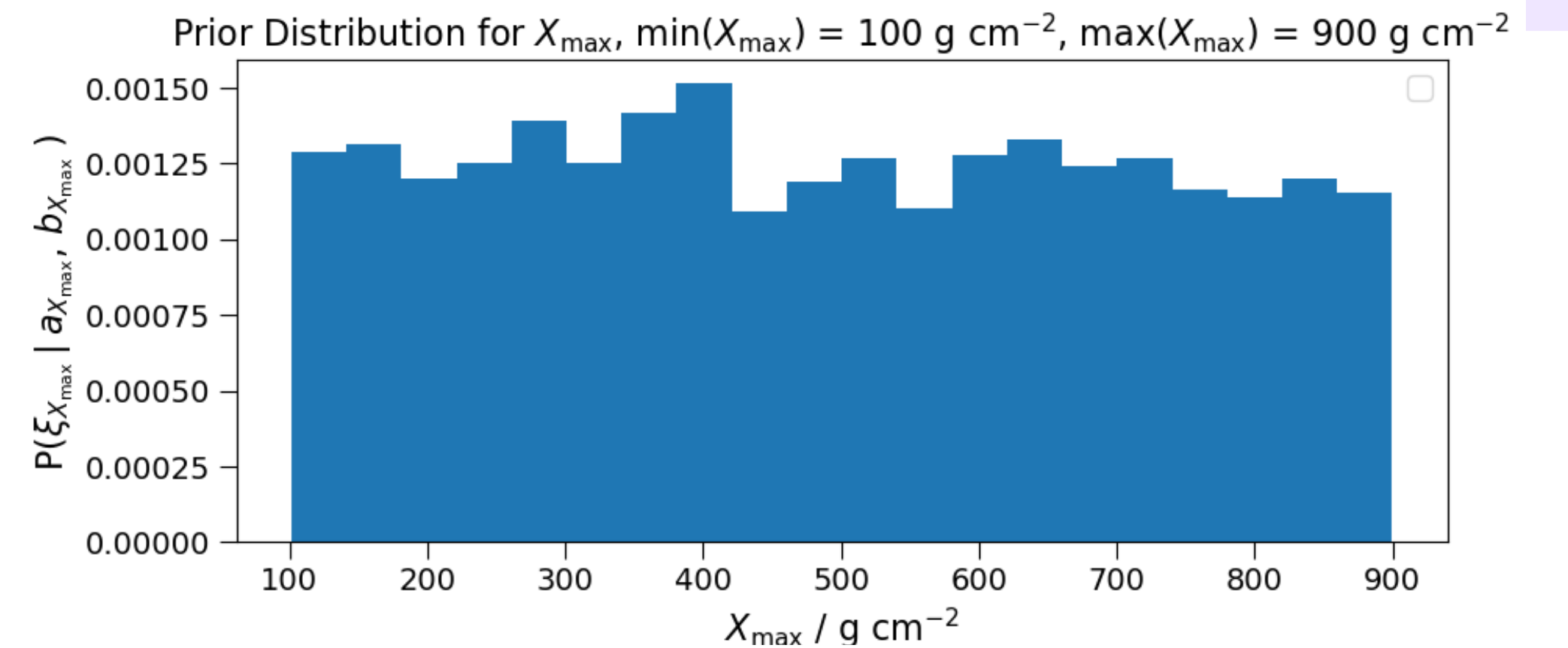


$$\xi_{N_{\max}} \sim \mathcal{N}(0,1)$$

$$N_{\max} \sim P(\xi_{N_{\max}} \mid \mu_{N_{\max}}, \sigma_{N_{\max}})$$

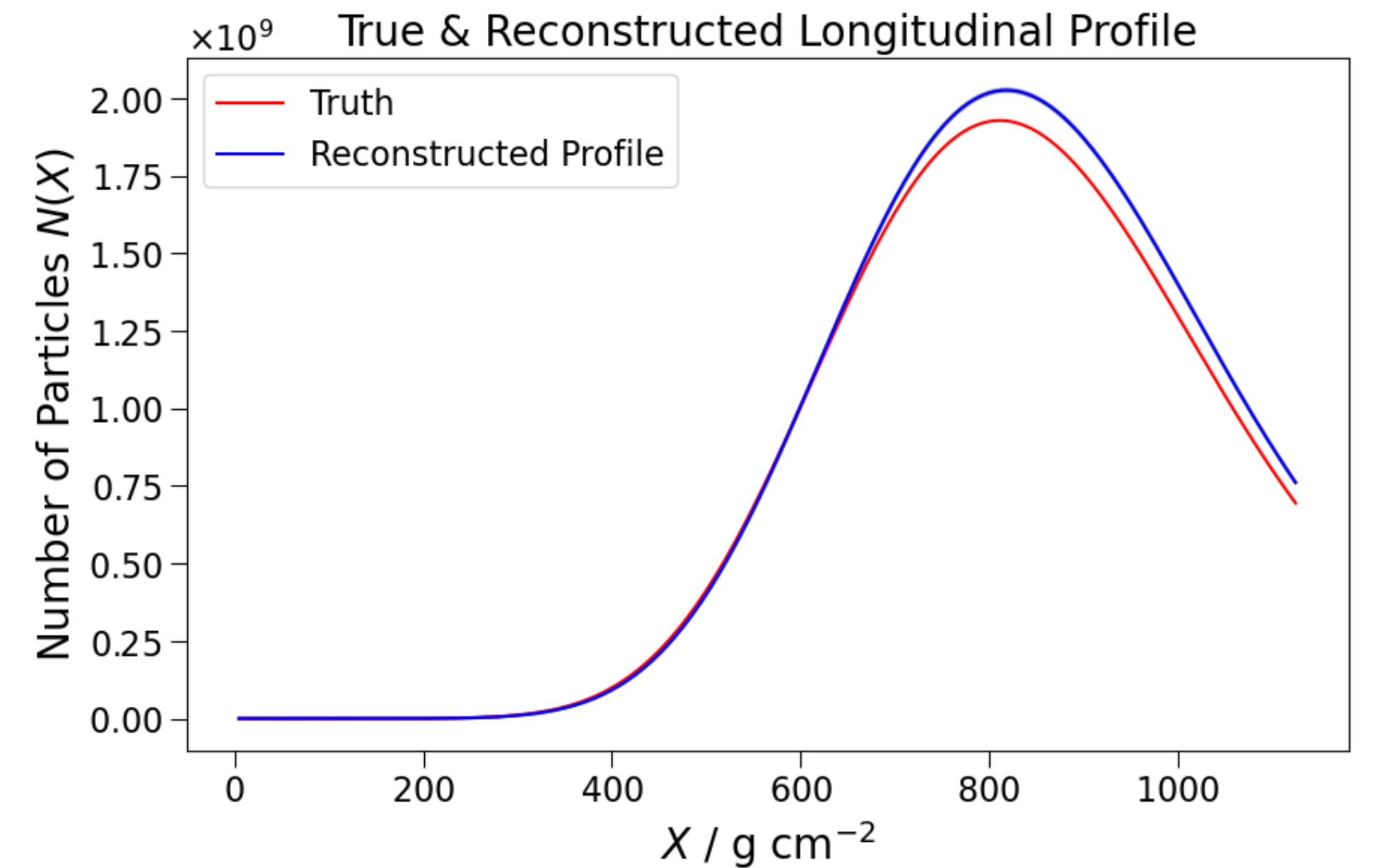
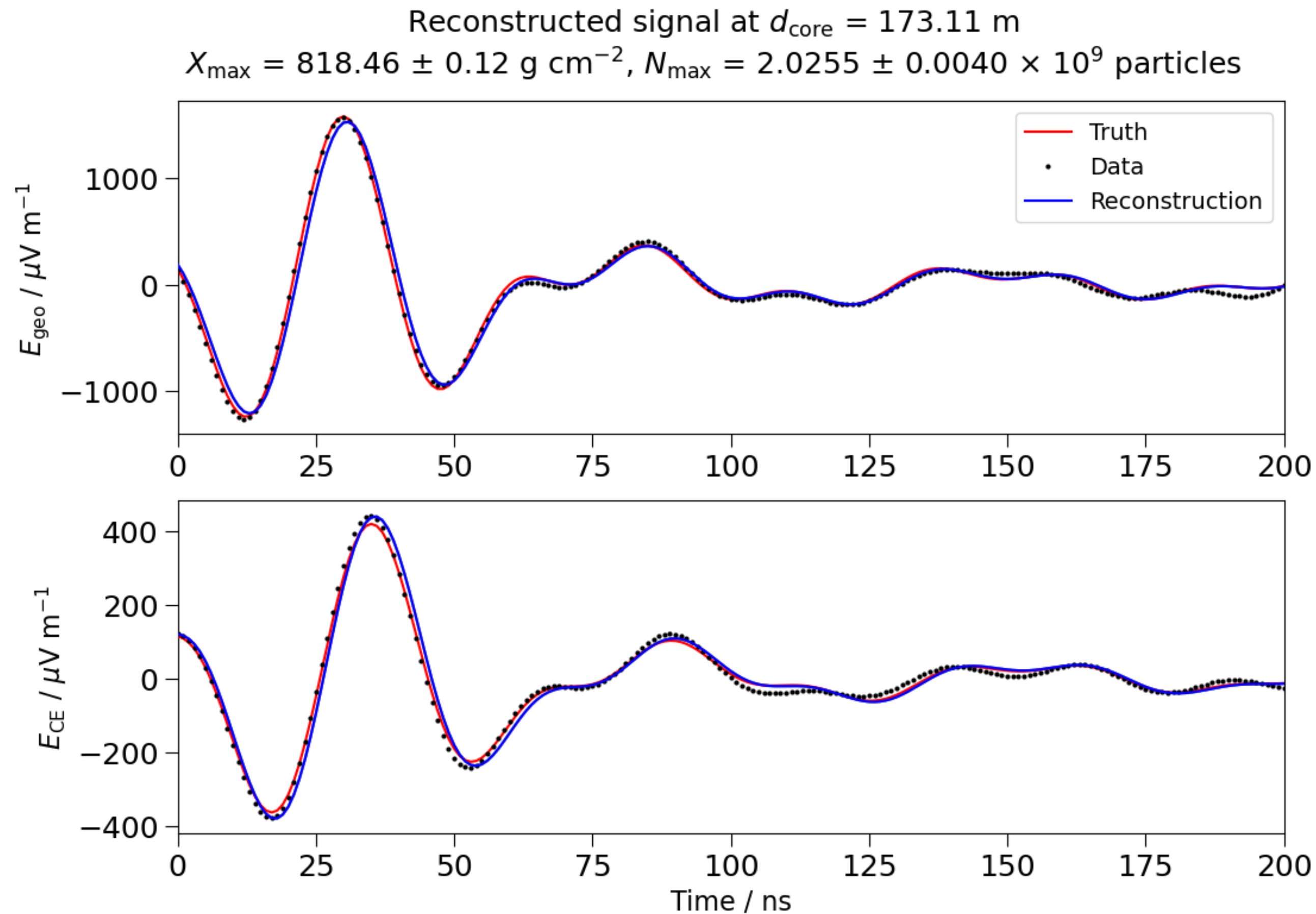
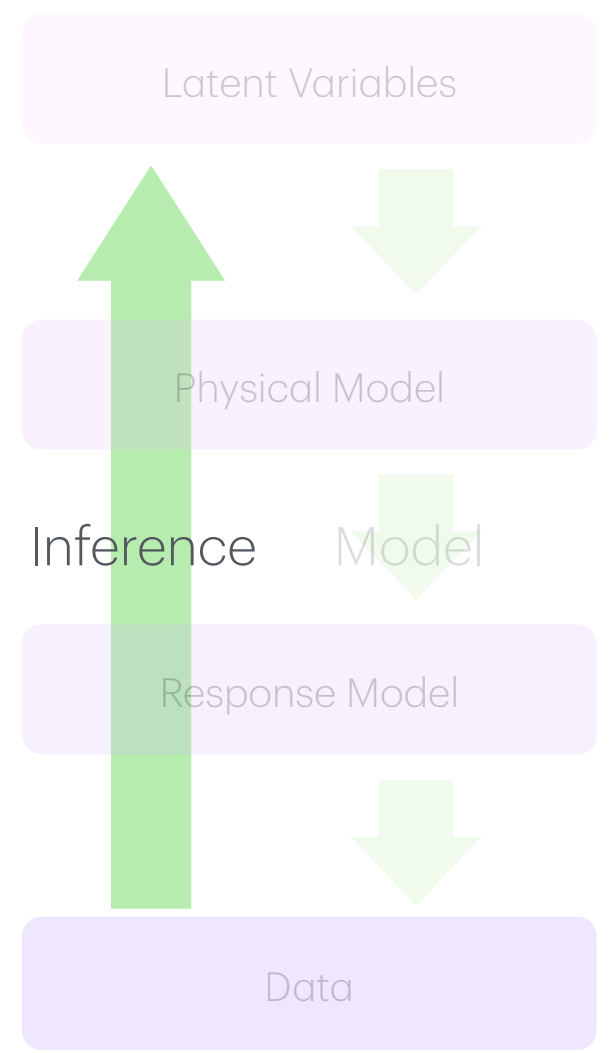
$X_{\max}$  : atmospheric depth at shower maximum

$N_{\max}$  : number of particles at  $X_{\max}$



# Application to Simulated Data

- **Simulated Data** using coREAS simulations
- Accurate  $X_{\max}$  reconstruction with bias of  $< 10 \text{ g cm}^{-2}$

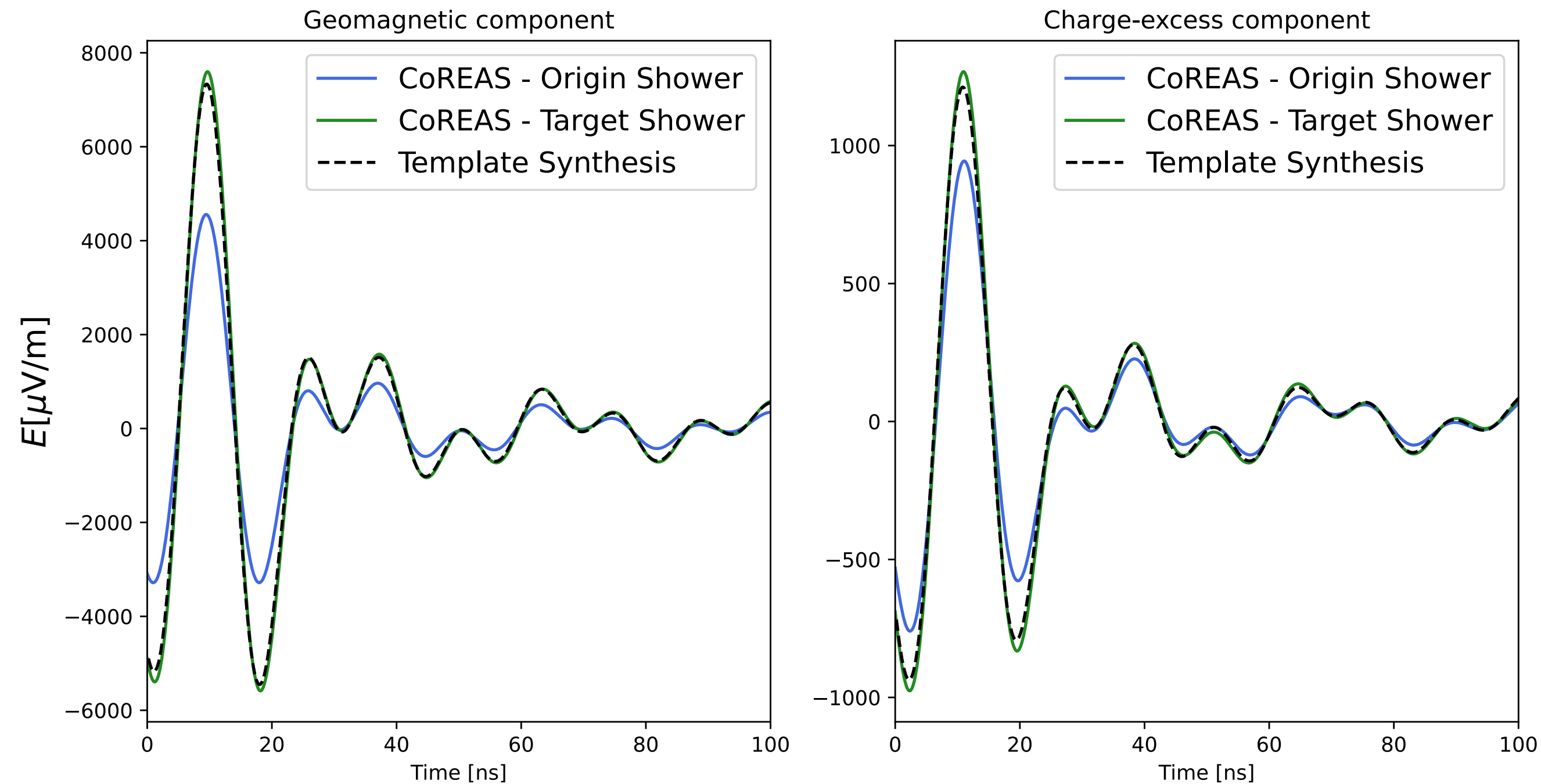


# Template Synthesis

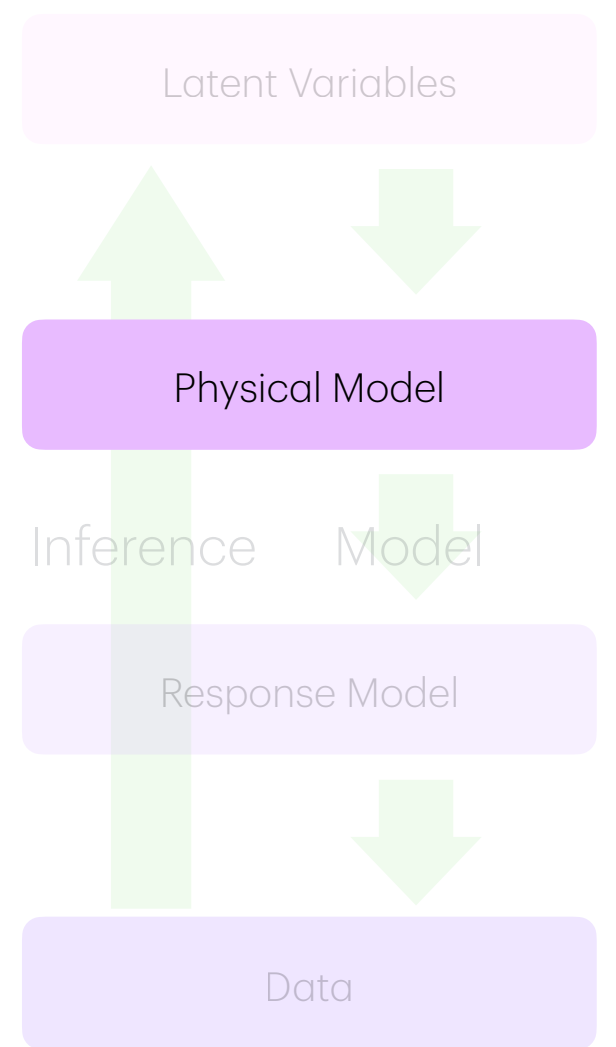
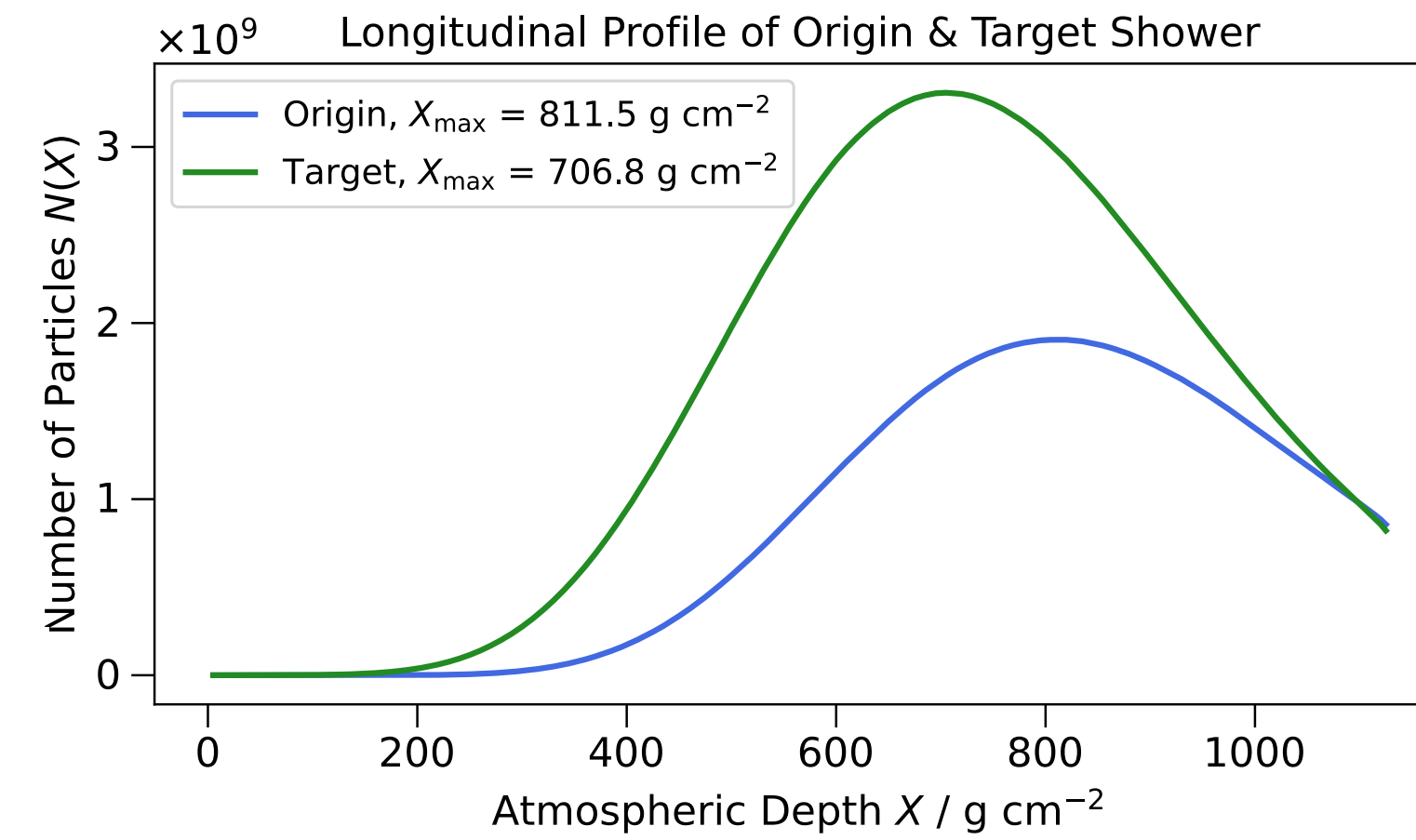
## Verification

Signals for antenna 14\_069 with  $d=69.2$  m from core

$$\chi_{\max}^{\text{origin}} = 811.5 \text{ g/cm}^2 - \chi_{\max}^{\text{target}} = 706.8 \text{ g/cm}^2$$



Electric field trace at single antenna from all slices for **simulated target shower** and synthesised target shower

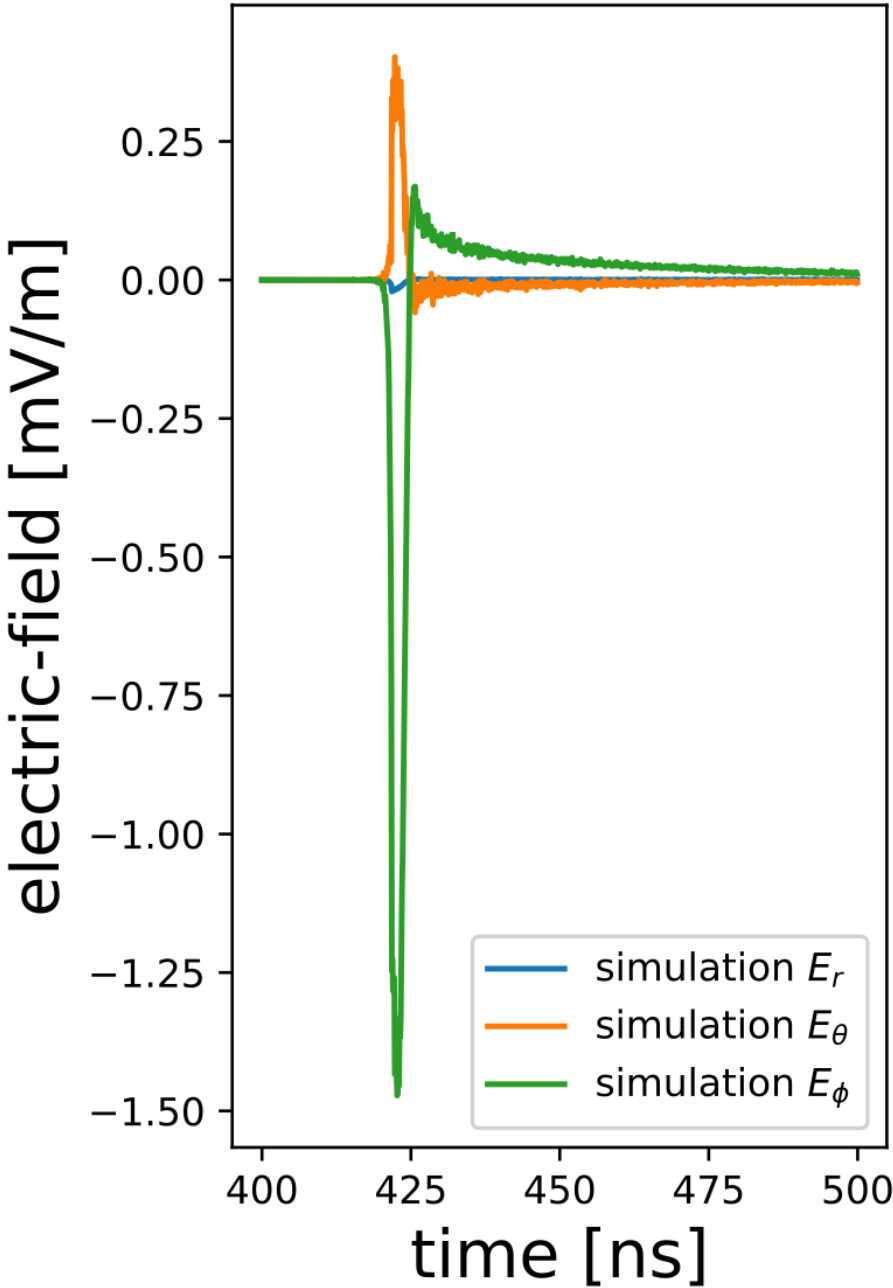


- Frequency band of 30 - 80 MHz
- Template synthesis match simulated results  $\lesssim 5\%$ !
- **<1s** per synthesis  $\rightarrow$  viable physical model for IFT reconstruction

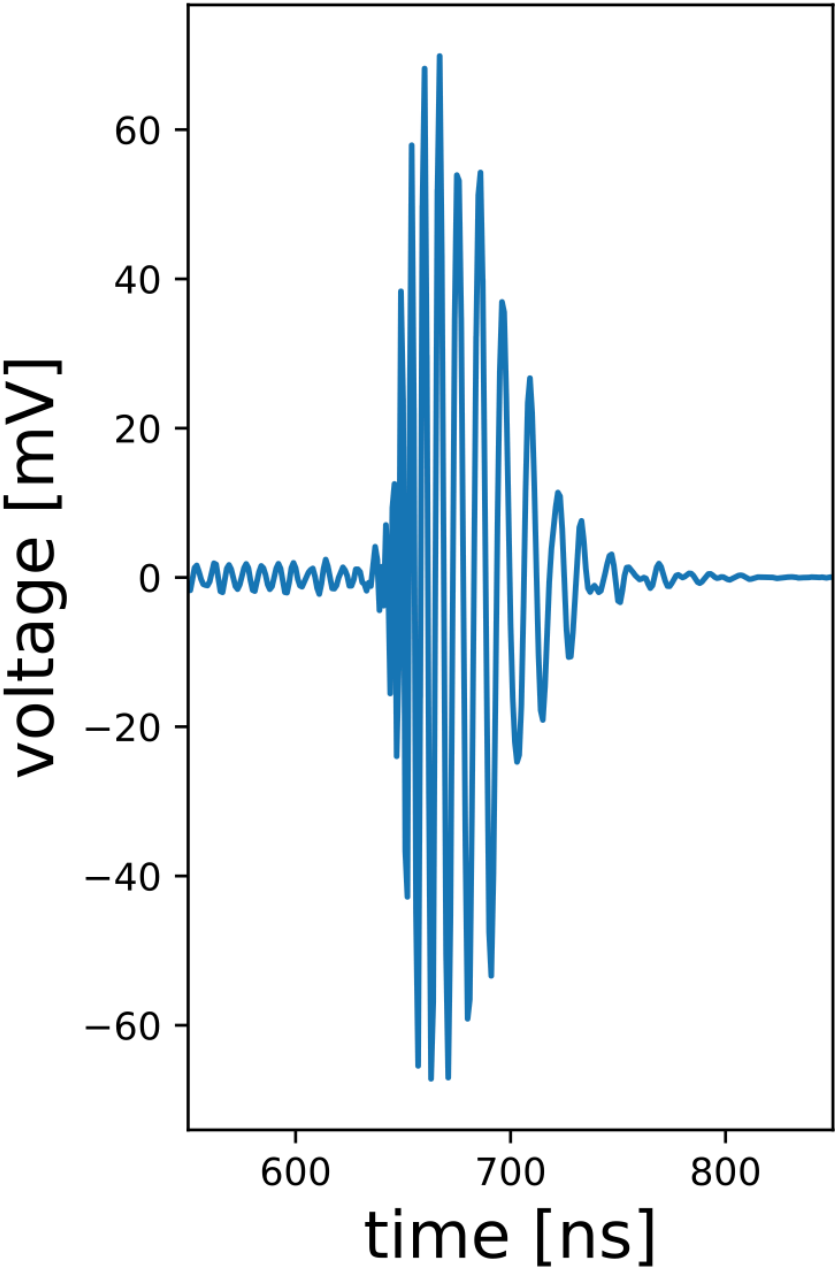
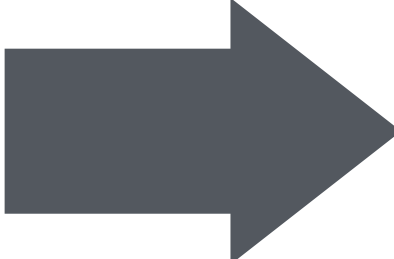


# Instrumental Response

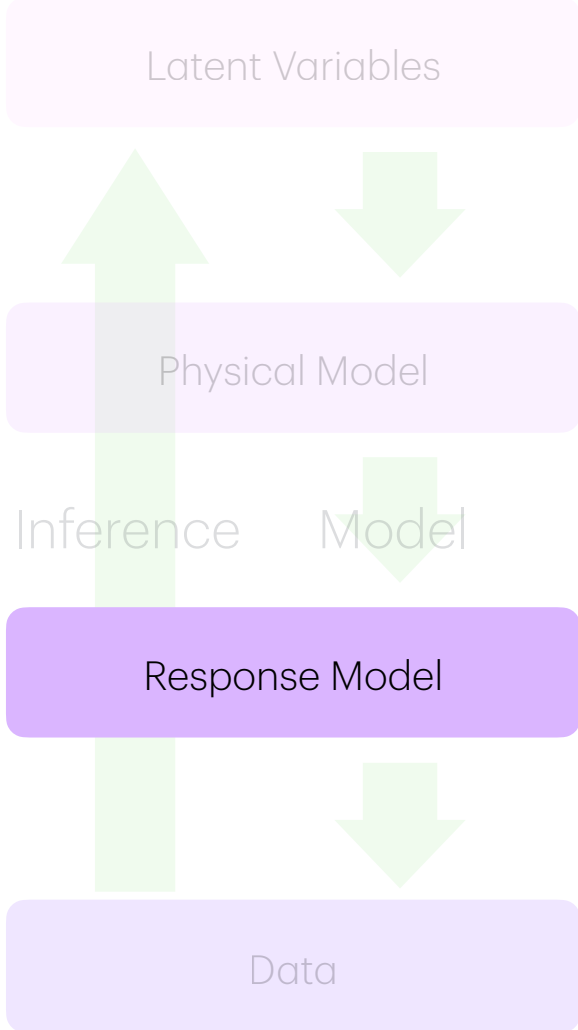
Idea: Transform electric field trace  $\rightarrow$  voltage trace through antenna response



Antenna Response



Glaser et al., Eur. Phys.Jour. C (2019) 79: 464



Currently not implemented!  $\rightarrow$  use electric field traces for now

# Reconstruction of Longitudinal Profile

- Use the whole profile as a prior instead of using Xmax

