







# Dark Matter in the multi-messenger era

#### Workshop on High-energy astrophysics in the multimessenger era

#### May 2023 Erlangen - Germany

#### <u>Aion Viana</u> Instituto de Física de São Carlos - USP

#### 1. Indirect detection of dark matter: basic principles

- 2. Indirect searches for dark matter with gamma-rays (and neutrinos): instruments and recent results
- 3. Indirect searches for dark matter with neutrinos: instruments and recent results
- 4. Indirect searches for dark matter with charged cosmic-rays: instruments and recent results

Disclaimer: Very large topic. Here I present a personal selection of recent results

# Introduction

#### **Two hypothesis:**

#### 1. Dark matter does exist



Most **gravitational mass** of galaxies and galaxy clusters (Zwicky 1937)





Pratically **non-collisional**: Bullet Cluster (Clowe+ 2006)



**Non-barionic**: Big bang nucleosynthesis, barionic accoustic oscillations, WMAP(2010), Planck(2015)

## Introduction

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## Introduction

#### **Two hypothesis:**

- 1. Dark matter does exist
- 2. Dark matter is a particle that couples non-gravitationally to Standard Model particles



Annihilation or decay of DM leads to the production of stable particles of Standard Model

# Relic density and WIMP miracle

#### Standard Cosmology Model: ACDM



 $Ω_b = 0.048 \pm 0.001$   $Ω_{cdm} = 0.258 \pm 0.006$  $Ω_\Lambda = 0.691 \pm 0.006$ 

# Relic density and WIMP miracle

#### Standard Cosmology Model: ACDM

Boltzman equation in comoving volume  $\frac{dn_{\chi}}{dt} + 3Hn_{\chi} = -\langle \sigma v \rangle \left[ n_{\chi}^2 - (n_{\chi}^{eq})^2 \right]$ 



# Relic density and WIMP miracle

#### Standard Cosmology Model: ACDM

Boltzman equation in comoving volume  $\frac{dn_{\chi}}{dt} + 3Hn_{\chi} = -\langle \sigma v \rangle \left[ n_{\chi}^2 - (n_{\chi}^{eq})^2 \right]$ 



# Dark matter particle candidates

#### A question of pespective: plausible mass scale

thermal

#### Weakly Interacting Massive Particles (WIMPs)

- weak scale mass (10 GeV 1 TeV)
- weak interaction  $\langle \sigma v \rangle \sim 3x10^{-26} \text{ cm}^3 \text{s}^{-1}$
- produces the observed thermal relic density

# particles

weak scale (1 TeV)

## Dark matter particle candidates

#### A question of pespective: plausible mass scale



"only" 90 orders of magnitude!

Lots of Beyond Standard Model theories predict the existence of one of more WIMPs, and other dark matter particle candidates





DM = Dark Matter SM = Standard Model (of Particle Physics)



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## **This talk!**



DM = Dark Matter SM = Standard Model (of Particle Physics)

# Dark matter messengers in the Galaxy



## Dark matter messengers in the Galaxy



# Dark matter messengers in the Galaxy



=> Spectral and spatial signatures

## Dark Matter searches with gamma rays

## The extreme electromagnetic universe











## Fermi telescope: 2008 - Present

- Energy range: 20 MeV 300 GeV
- Effective area ~ 0.9 m<sup>2</sup>
- Energy resolution ~ 10%
- Angular resolution ~0.15° (GeV)
- Pair conversion detector:





## The current IACT world

#### VERITAS Arizona, USA 1275m a.s.l. 4 telescopes, Ø12m Stereoscopy >2007



#### MAGIC Canary Island, Spair

La Palma, 2225m a.s.l. 2 telescopes, Ø17m >2009

H.E.S.S. Namibia

1800m a.s.l. 4 telescopes, Ø12m stereoscopy >2003 HESS 2 : 4+ 1 (Ø28m) telescopes, 2012

## The future IACT world: Cherenkov Telescope Array

- Two arrays: North in La Palma (Spain), South in Paranal (Chile)
- Factor 10 better flux sensitivity
- Larger energy coverage, field of view and twice better angular and energy resolution

## The future IACT world: Cherenkov Telescope Array



CTA is a global effort with more than 1,350 scientists and engineers from 210 institutes in 32 countries involved in directing CTA's science goals and array design.

#### Brazilian participation:

- Centro Brasileiro de Pesquisas Físicas
- Centro de Ciências Naturais e Humanas Universidade Federal do ABC
- Departamento de Engenharias e Exatas, Universidade Federal do Parana
- Escola de Artes, Ciências e Humanidades, Universidade de São Paulo
- Escola de Engenharia de Lorena, Universidade de São Paulo
- Instituto de Astronomia, Geofísico, e Ciências Atmosféricas
- Instituto de Física de São Carlos, Universidade de São Paulo
- Instituto de Física Universidade de São Paulo
- International Centre for Theoretical Physics, Universidade Estadual Paulista
- Nucleo de Astrofisica Teorica, Universidade Cruzeiro do Sul
- Núcleo de Formação de Professores Universidade Federal de São Carlos



#### Southern Wide-field Gamma-ray Observatory (SWGO)





## The SWGO collaboration

- R&D collaboration founded on July 1st 2019 by 54 partner institutes in 12 countries + supporting scientists from 11 more countries
- Aims of the collaboration: development, over the next three years, of a detailed proposal for the implementation of such an observatory, including site selection and technology choice



#### Countries in SWGO Institutes

Argentina\*, Brazil, Chile, Czech Republic, Germany\*, Italy, Mexico, Peru, Portugal, South Korea, United Kingdom, United States\*

#### Supporting scientists

Australia, Bolivia, Costa Rica, France, Japan, Poland, Slovenia, Spain, Switzerland, Turkey

\*also supporting scientists

# A straw man design for SWGO

- Based on established performances (e.g. HAWC)
- CORSIKA + simple detecctors; altitude of 5000m; larger + denser array











where

$$\overline{J}(\Delta\Omega) = \frac{1}{\Delta\Omega} \int_{\Delta\Omega} d\Omega \int_{\text{l.o.s.}} \rho^2[r(s)] ds$$

- Line of sight integral
- Density profile model is needed
- Dependence dark matter halo modeling

# **Dark Matter halo modeling**



Observation of galaxies dynamics => Cored profile



- The parameters are found from observation of some tracer dynamics(luminous density, star velocity dispersion, velocity anisotropy...)
- The DM density at small scale is poorly known
  - necessity to take in account both class of models
### **Dark Matter halo modeling**

- Cosmological N-body numerical simulations => Cusp profile
- Observation of galaxies dynamics => Cored profile



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#### Additional contributions to the DM annihilation flux

#### **From astrophysics:**

• Contribution of the substructures(sub-halos) to the overall density <= flux ~  $\rho^2$ 







### Secondary radiation from DM



#### Dark matter targets



#### Galactic Centre

- Proximity (~8kpc)
- High (possibly) central DM concentration :

DM profile : core? cusp?

High astrophysical background in gammarays

#### Dwarf galaxies of the Milky Way

- □ Many of them within the 100 kpc from Sun
- Extremely DM-dominated environment
- Potential low astrophysical

background



#### Galaxy clusters

- ☐ High DM annihilation luminosity
- □ Substructures contribution to the overall DM flux
- Astrophysical background may be important





#### Local Group Galaxies

- Relatively close
- □ Large DM mass
- Secondary radiation may be important

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### Dwarf galaxies of the Milky Way



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## Combined Dark Matter Searches with gamma-ray observatories

#### Twenty dwarf spheroidal galaxies observed by Fermi-LAT, HAWC, H.E.S.S., MAGIC, and VERITAS

Source name	Experiments	Distance
		(kpc)
Bootes I	Fermi-LAT, HAWC, VERITAS	66
Canes Venatici I	<i>Fermi</i> -LAT	218
Canes Venatici II	Fermi-LAT, HAWC	160
Carina	Fermi-LAT, H.E.S.S.	105
Coma Berenices	Fermi-LAT, HAWC, H.E.S.S., MAGIC	44
Draco	Fermi-LAT, HAWC, MAGIC, VERITAS	76
Fornax	Fermi-LAT, H.E.S.S.	147
Hercules	Fermi-LAT, HAWC	132
Leo I	Fermi-LAT, HAWC	254
Leo II	Fermi-LAT, HAWC	233
Leo IV	Fermi-LAT, HAWC	154
Leo T	Fermi-LAT	417
Leo V	<i>Fermi</i> -LAT	178
Sculptor	Fermi-LAT, H.E.S.S.	86
Segue I	Fermi-LAT, HAWC, MAGIC, VERITAS	23
Segue II	<i>Fermi</i> -LAT	35
Sextans	Fermi-LAT, HAWC	86
Ursa Major I	Fermi-LAT, HAWC	97
Ursa Major II	Fermi-LAT, HAWC, MAGIC	32
Ursa Minor	Fermi-LAT, VERITAS	76

#### • Armand et al arXiv:2108.13646

## In the case of no signal detection -> Joint likelihood analysis

 $\succ$  Limits on the plane  $\langle \sigma v \rangle \propto m_{DM}$ 

#### **Combined Dark Matter Searches with gamma-ray** observatories

 $\succ$  Three channels bb, W<sup>+</sup>W<sup>-</sup>,  $\tau$ + $\tau$ -, using the J factors from Geringer Sameth et al.



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Combined upper limits are up to 3 times more constraining, depending on the annihilation channel and the mass

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- Below ~2 30 TeV DM limits largely dominated by Fermi-LAT
- Above ~2 30 TeV IACTs and HAWC take over

#### Future prospects on dSphs



- Recent deep observations with wide-field optical imaging surveys have already discovered 33 new ultra-faint Milky Way satellites
- The next generation of surveys (i.e., The Rubin Observatory) should complete our census of the ultra-faint dwarfs out to the virial radius of the Milky Way.
- Legacy data from Fermi-LAT at these locations could easily and immediately be analysed when new dSphs are found.

#### Future prospects on dSphs



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### H.E.S.S. Inner Galaxy Survey

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- Analysis method : 2D likelihood analysis with spectral and spatial information of signal and background



#### Dark Matter distribution in the GC





- > We assumed an Einasto profile
- The spatial morphology can be used to discriminate between a DM gamma-ray signal and the residual isotropic hadronc background

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#### > Search for signal in the inner 1° (CTA) and 10° (SWGO) of the Galaxy



- Search for signal in the inner 1° (CTA) and 10° (SWGO) of the Galaxy
- Exclusion of +-0.3° band in latitude to avoid strong astrophysical background
- > 2D likelihood analysis with spectral and spatial information of signal and background





- For  $\tau^+\tau^-$  channel: SWGO more sensitive than CTA for masses > 600 GeV
- Combined (LAT,CTA,SWGO) future sensitivity smaller than thermal relic cross-section for all masses below 100 TeV



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W<sup>+</sup>W<sup>-</sup> channel SWGO GC Halo 10 yr CTA GC Halo 500 hr AT 15 dSphs 6 vr

bb channel



- For W+W- channel: combined sensitivity smaller than relic-thermal cross- $\triangleright$ section (3×10<sup>-26</sup> cm<sup>-3</sup> s<sup>-1</sup>) for all masses below 80 TeV
- For **bb** channel: combined sensitivity smaller than thermal relic cross-section (3×10<sup>-26</sup> cm<sup>-3</sup> s<sup>-1</sup>) for all masses below 30 TeV

### **Complementarity at the highest energies**



For masses > 10 TeV, SWGO can be complementary to CTA -> confirmation of a spectrum cut-off

### DM decay sensitivity



Gamma-ray flux from decay of a WIMP:

$$\frac{\mathrm{d}\Phi_{\mathrm{Dec}}(\Delta\Omega, E_{\gamma})}{\mathrm{d}E_{\gamma}} = \left(\frac{1}{4\pi} \frac{1}{\tau_{\mathrm{DM}}M_{\mathrm{DM}}} \frac{\mathrm{d}N}{\mathrm{d}E_{\gamma}}\right) \times \left(D(\Delta\Omega)\right)$$

where

$$D(\Delta \Omega) = \int_{\Delta \Omega} \int_{\text{l.o.s.}} d\Omega \, ds \, \rho_{\text{DM}}[r(s,\Omega)]$$

### GC halo: DM decay sensitivity



- SWGO will have unprecedented sensitivity in the TeV mass range
- Better than CTA and Fermi-LAT for all DM particle masses above ~1 TeV
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### Large Magellanic Cloud

- Large dark matter content  $M_{vir} \sim 10^{11} M_{Sun}$
- Proximity to Earth
   D ~ 50 kpc



Credit: David Darling

### Large Magellanic Cloud observed by ASKAP

- Large dark matter content  $M_{vir} \sim 10^{11} M_{Sun}$
- Proximity to Earth
   D ~ 50 kpc



Credit: David Darling

- Australian Square Kilometre Array Pathfinder (ASKAP)
   36 antennas, each 12 m in diameter Commissioning and early science
- Evolutionary Map of the Universe (EMU) Survey of the Southern sky (3 x 10<sup>4</sup> deg<sup>2</sup>) at ~ 1 GHz with ~10" resolution and sensitivity of 30 mJy/beam



#### Limits to DM from LMC by ASKAP



- Very strong bounds
- Thermal cross-section excluded for DM masses below 480 GeV (bb), 358 GeV (W+W-), 192 GeV ( $\tau$ + $\tau$ -) , 164 GeV ( $\mu$ + $\mu$ -)

#### "Galactic Center GeV Excess"



#### **Residual GeV emission in the Galactic Center by Fermi-LAT**

- Initial claims by Goodenough & Hooper (2009) [see also Vitale & Morselli (2009)]
- Controversial discussion in the community for six years
- In 2015, the existence of "GeV excess" finally got the blessing of the Fermi-LAT collaboration
- ➢ Is it a sign of DM?

#### Literature overview

#### Papers that looked at data

- Goodenough & Hooper, arXiv:0910.2998
- Vitale & Morselli, 2009
- Hooper & Goodenough, Phys. Lett. B697 (2011) 412
- Hooper & Linden, Phys. Rev. D84 (2011) 123005
- Boyarsky, Malyshev & Ruchayskiy, Phys. Lett. B705 (2011) 165
- Abazajian & Kaplinghat, PRD 86 (2012) 083511
- Hooper & Slatyer, Phys. Dark Univ. 2 (2013) 118
- Gordon & Macias, Phys. ReV. D88 (2013) 083521
- Macias & Gordon, PRD 89 (2014) 063515
- Abazajian, Canac, Horiuchi, Kaplinghat, Phys. Rev. D90 (2014) 023526
- Cholis, Evoli, Calore, Linden, Weniger, Hooper, JCAP 1512 (2015) 12
- Calore, Cholis & Weniger, JCAP 1503 (2015) 038
- Zhou, Liang, Huang, Li, Fan, Chang, Phys. Rev. D91 (2015) 123010
- Gaggero, Taoso, Urbano, Valli & Ullio, JCAP 1512 (2015) 056
- Daylan, Finkbeiner, Hooper, Linden, Portillo et al., Physics of Dark Universe 12 (2016) 1
- De Boer, Gebauer, Neumann, Biermann, arXiv:1610.08926 (ICRC 2016 proceedings)
- Huang, Ensslin & Selig, JCAP 1604 (2016) 030
- Carlson, Linden, Profumo, Phys. Rev. D94 (2016) 063504
- Bartels, Krishnamurthy, Weniger, Phys. Rev. Lett. 116 (2016) 5
- Macis, Gordon, Crocker, Coleman, Paterson, arXiv:1611.06644
- Lee, Lisanti, Safdi, Slatyer, Xue, Phys. Rev. Lett. 116 (2016) 5
- Ajello et al. 2016, Astrophys. J. 819, 44
- Ackermann et al., 2017, Astrophys. J. 840, 43
- Ajello et al., 2017, arXiv:1705.00009
- Macias, Horiuchi, Kaplinghat, Gordon, Crocker, Nataf, JCAP arXiv:1901.03822
- Leane & Slatyer, PRL arXiv:1904.08430
- Cholis, Zhong, McDermott, Surdutovich PRD arXiv:2112.09706
- Martin Pohl, Macias, Coleman, Gordon, ApJ arXiv:2203.11626

Excess is likely DM Excess is there Excess is likely not DM Excess is not there

+hundreds of DM theory papers+a few papers missed

Slide adapted from C. Weniger

### **High-energy telescopes: past-present-future**



R. K. LEANE

ENERGY

#### What about neutrinos?



### Neutrinos experiments: past-present-future


#### Neutrino constraints to annihilation





#### Neutrino constraints to decay

The IceCube Collaboration arXiv:1804.03848 & arXiv:2107.11527



## Dark matter capture in the Sun



## Neutrinos constraint to scattering cross-section



Limits from IceCube and ANTARES comparable to DM direct detection experiments

## Dark Matter searches with charged cosmic rays

## **Transport equation of charged CRs**

spectrum



Salati, Chardonnay, Barrau, Donato, Taillet, Fornengo, Maurin, Brun... '90s, '00s

$$\frac{\partial f}{\partial t} - K(E) \cdot \nabla^2 f - \frac{\partial}{\partial E} \left( b(E)f \right) + \frac{\partial}{\partial z} (V_c f) = Q_{\text{inj}} - 2h\delta(z)\Gamma_{\text{spall}} f$$
diffusion energy loss convective wind source spallations funcer

# **Illustration of CRs propagation**



Diffusion on magnetic inhomogeneities

**R** <sup>0.6</sup> [excellent review: Lavalle & Salati (2012)]

#### Most relevant assumption:

- Cylindrical symmetry
- Homogeneous diffusion coefficient

#### Most relevant parameters:

- Diffusion zone height, L
- Diffusion constant, D

R

# **Detecting charged CRs at GeV-TeV**

- Cosmic-ray detector at International Space Station: AMS-2
- Taking data since 2011



**Data Signature of Various Particles in Each Detector** 





## Primary production of CRs from dark matter



# Proton/anti-proton ratio



- Shown as excess above the expectations from secondary production (ICRC 2015: "Theoretical prediction based on pre-AMS knowledge of cosmic ray propagation")
- Antiprotons traditionally well modelled by our CR knowledge
- —> Useful to set stringent constraints on DM contribution.

# Proton/anti-proton ratio



- However quite some uncertainty affects the prediction of the astro only antiproton signal.
- Situation: No excess observed above astrophysical background, when all uncertainties are taken into account
- Only upper limits

## **Constraints to annihilation from antiprotons**



### **Positron fraction**



- Anomaly: a rise in the positron fraction for E > 10 GeV
- From CR propagation physics, the ratio is expected to decrease for all propagation models.

### **Positron fraction from DM**

However, dark matter interpretation:

- Only annihilation into leptons ("leptophilic" DM)
- Massive particle (~TeV)
- Too large annihilation cross-section: O(10<sup>-21</sup>-10<sup>-24</sup> cm<sup>-3</sup> s<sup>-1</sup>)



#### **Positron fraction from DM**

- Annihilation into leptons produces inverse compton emission, not seen in gamma -> gamma-ray consraints
- Tension with CMB

Dark matter interpretation of positron fractions seems to be in tension with gammaray observations!







# **Other explanations**

Primary positrons by pair production (e+e-) in pulsars magnetosphere







#### How to discriminate DM from astrophysical emission?

a. Spectrum shape(hard)b. Anisotropy (signal direction)?



Boudaud+ A&A'14

### **Cosmic-ray detectors: past-present-future**





### **Cosmic-ray detectors: past-present-future**

COSMIC-RAY TELESCOPES



# Other new interesting things I didn't mention

#### Dark Matter In Extreme Astrophysical Environments: arXiv:2203.07984



DM mass (eV)

# Thank you!

#### GC halo: DM decay sensitivity

#### W<sup>+</sup>W<sup>-</sup> channel

bb channel



- Unprecedented sensitivity in the TeV mass range
- Better than CTA and Fermi-LAT for all DM particle masses above  $\sim 1$  TeV
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# Complementarity to direct detection and

#### accelerators

- Particle model dependent: in Simplified DM models it depends on the mediators
- Indirect detection is most sensitive for pseudoscalar DM at >200 GeV
- For a complete understanding of the nature of dark matter these different techniques are complementary and essential



Table: Summary of suppression effects		
OPERATOR	ID	DD
SCALAR	$v^2$	1
PSEUDO SCALAR	1	$(ec{s}_\chi\cdotec{q})(ec{s}_N\cdotec{q})$
VECTOR	1	1
AXIAL VECTOR	$m_q^2, v^2$	$ec{s}_{\chi} \cdot ec{s}_{ec{N}}_{M.\ Meyer}$

