

<http://deeplearningphysics.org>

← Tutorial web page

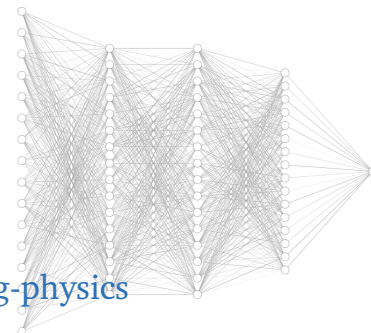
Deep Learning for Physics Research



Exercise class:

- fully-connected networks
- convolutional neural networks

<https://github.com/DeepLearningForPhysicsResearchBook/deep-learning-physics>

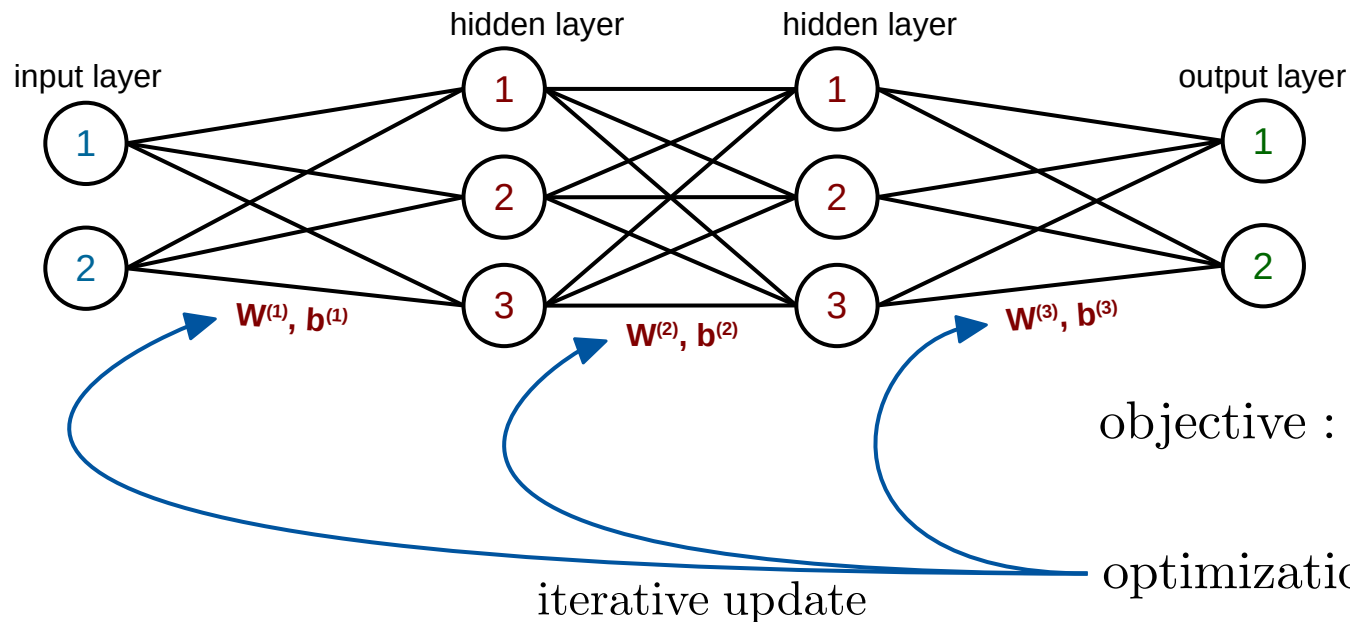


Deep Neural Networks

Feature Hierarchy: each new layer extract more abstract information of the data.

Probabilistic Mapping: learns to combine the extracted features

Train model (to find $\theta = \{W_i, b_i\}$ that minimizes objective) is automatic process.



$$y = \sigma(\mathbf{W}\mathbf{x} + \mathbf{b})$$

output activation input

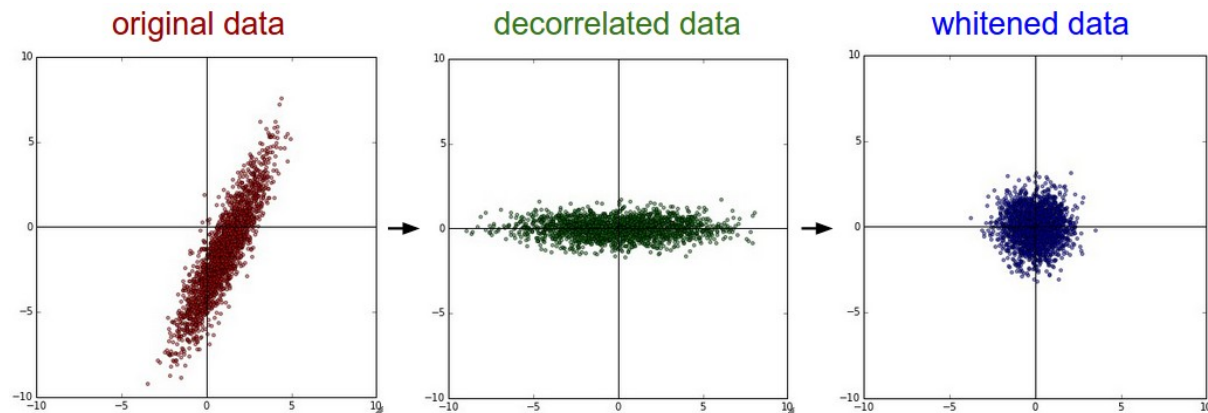
adaptive parameters

$$\text{objective : } J(\theta) = \sum_i [y_m(x_i, \theta) - y_i]^2$$

$$\text{optimization : } \frac{dJ}{d\theta} \rightarrow 0$$
$$\tilde{\theta} \rightarrow \theta - \alpha \frac{dJ}{d\theta}$$

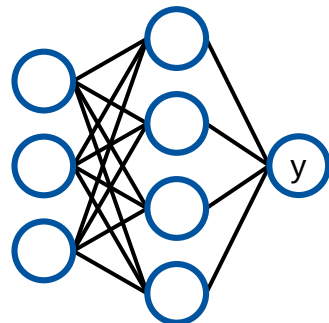
Data Preprocessing

- Input features of data set should be on same scale
 - ♦ Prevent particular sensitivity to few features
- Common normalization strategies
 - ♦ Limit range between $[0, 1]$ or $[-1, 1]$
 - ♦ Standard normalization: $\mu(x_i) = 0$ & $\sigma(x_i) = 1$
 - ♦ Whitening: standard normalization + decorrelation

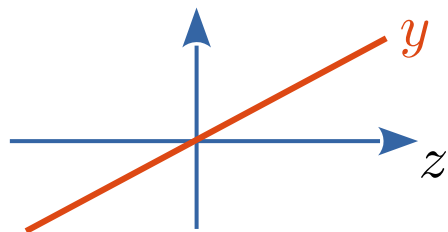


Classification vs. Regression

Regression



Linear

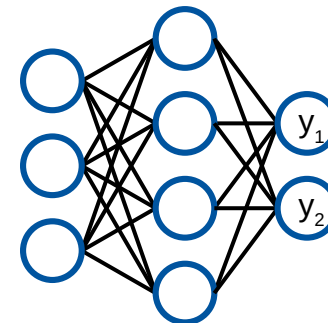


no activation function

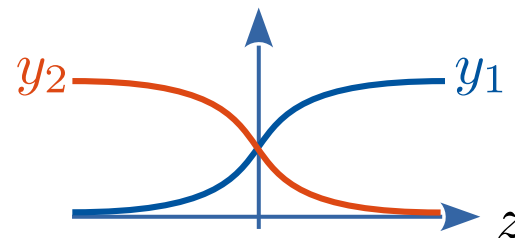
Minimize mean-squared-error

$$J(\theta) = \frac{1}{n} \sum_i [y_i - y_m(x_i)]^2$$

Classification



Softmax



Minimize cross entropy

$$J(\theta) = -\frac{1}{n} \sum_i y_i \log[y_m(x_i)]$$

$$y_j(z) = \frac{e^{z_j}}{\sum_i e^{z_i}}$$

Clarifying frequent misunderstandings



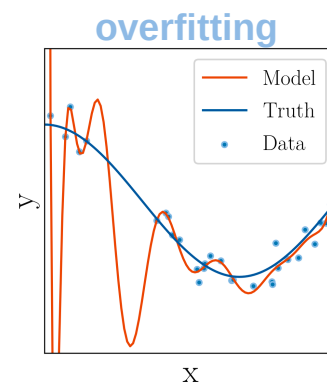
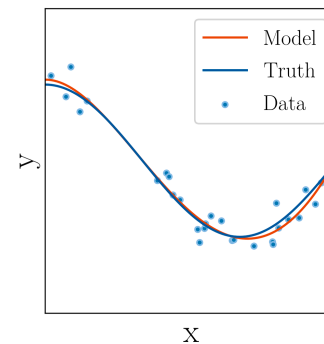
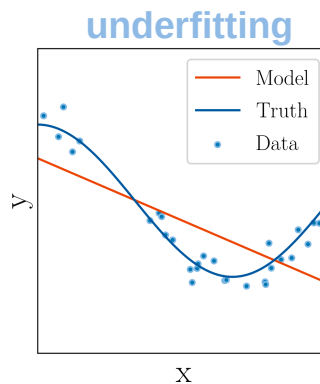
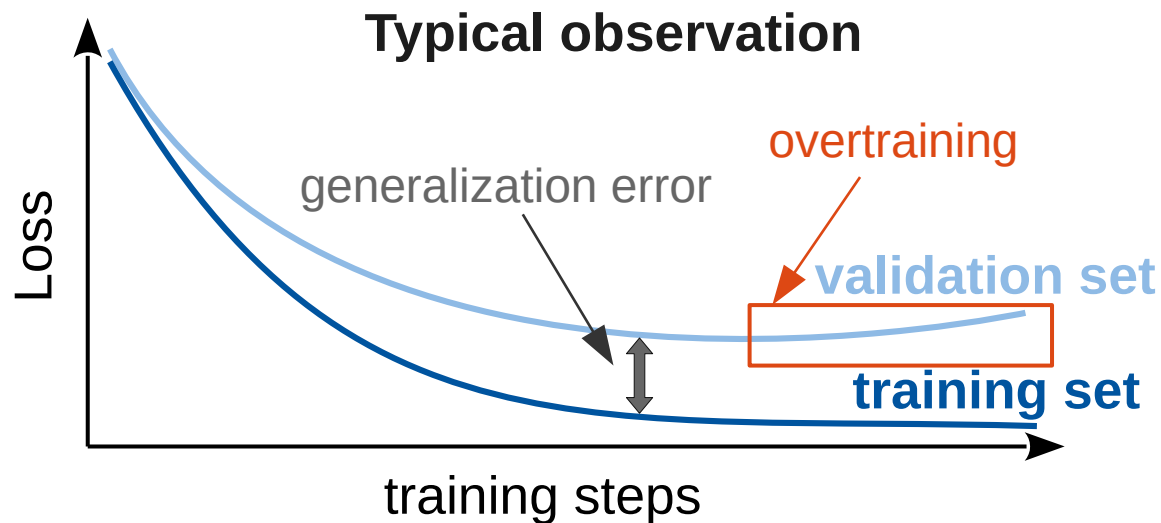
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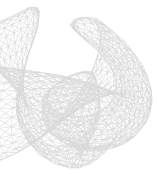


- **Use of activation functions** - layer without activation is usually meaningless
 - ♦ sigmoid **only** @ last layer in classification / regression @ last layer **no** activation
- **Universal approximation theorem is only a theoretic statement**
 - ♦ even such models exists → you have to find its design & **train** it → not easy!
- **Test and validation data are different**
 - ♦ validation: tune your DNN, e.g. train 10 DNNs & compare, monitor overtraining
 - ♦ test: check after you decide for one of the 10 models → ONCE!
- **Training networks is not random** → extract features out of patterns in data
 - ♦ retraining gives slightly different DNN → its feature sensitive to same patterns!
- **DNNs are not the holy grail** → simple fits can outperform DNNs
 - ♦ lots of data needed, challenge has to be complex and multi-dimensional

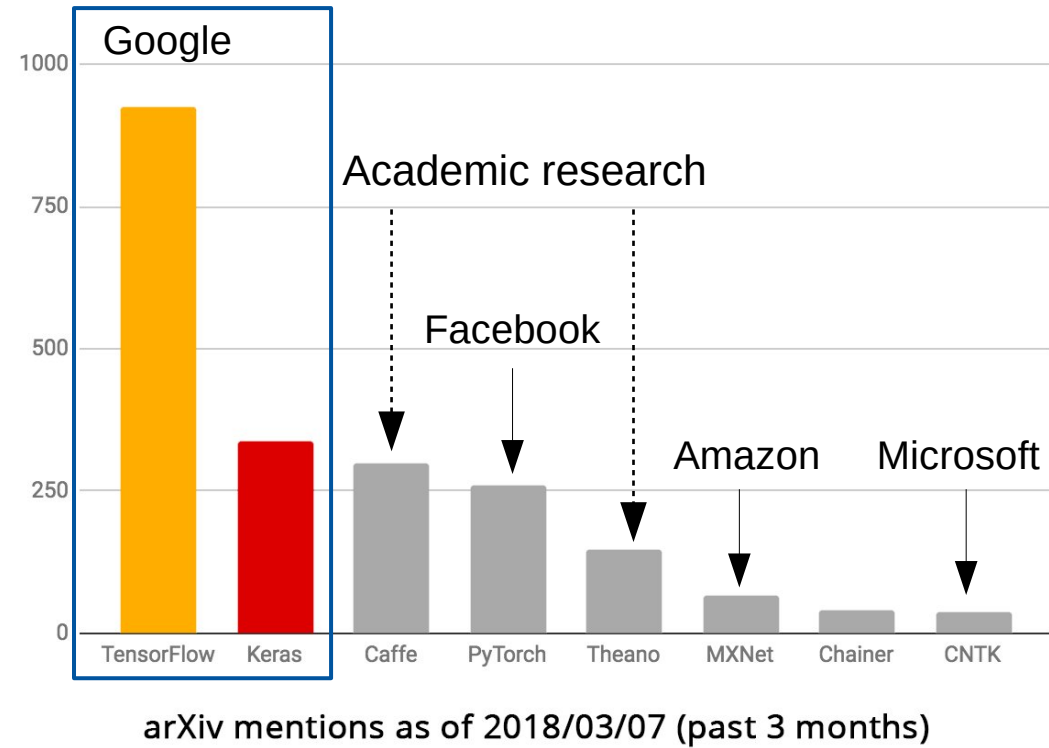
Recap: Under- and Overtraining

- Split data into 3 sets
 - ♦ training
 - ♦ test
 - ♦ validation
- What is a reasonably split?
- During training monitor the loss separately for training and validation set
 - ♦ check for overtraining!
 - ♦ if loss stops decreasing
 - reduce learning rate
 - stop training





Practice I



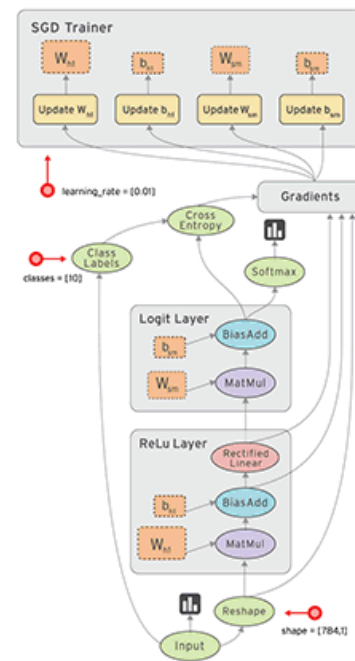
TensorFlow

“Open source software library for numerical computation using data flowing graphs”

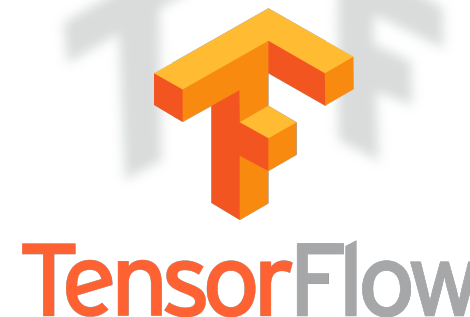
- **Nodes** represent mathematical operations
- **Graph edges** represent multi dimensional data arrays (**tensors**) which **flow** through the graph
- Supports:
 - ♦ CPUs and **GPUs**
 - ♦ Desktops and mobile devices
- Released 2015, stable since Feb. 2017
- Developer: Google Brain



TensorFlow



- Will use keras in this tutorial (TensorFlow backend) - <https://keras.io>
- High-level neural networks API, written in Python
- Concise syntax with many reasonable default settings
- Useful callbacks / metrics for monitoring the training procedure
- Nice Documentation & many examples and tutorials
- Comes with TensorFlow



How to train your Model?

I. Define Model

- Add layers, nodes, regularization, activation functions,)

II. Compile Model

- Set Loss, optimizer settings and useful metrics

III. Fit Model

- Set number of iterations and train model on given data

```
from tensorflow import keras
```

```
layers = keras.layers
```

```
models = keras.models
```

```
# setup and train a 3-layer regression network with Keras
```

```
model = models.Sequential()
```

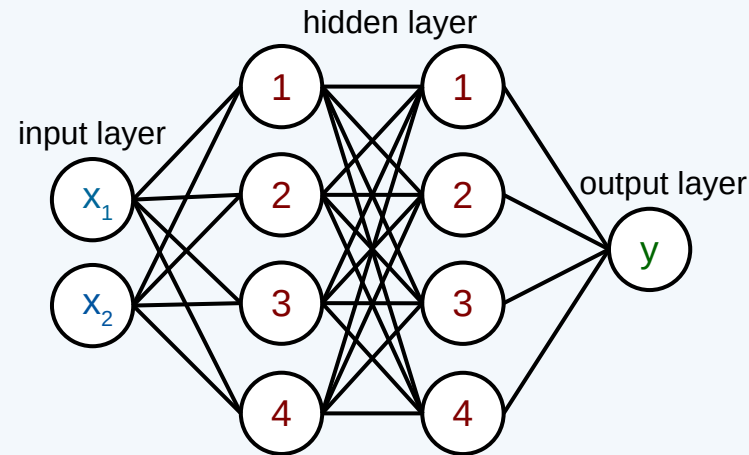
```
model.add(layers.Dense(4, activation='relu', input_dim=2))
```

```
model.add(layers.Dense(4, activation='relu'))
```

```
model.add(layers.Dense(1, activation='linear'))
```

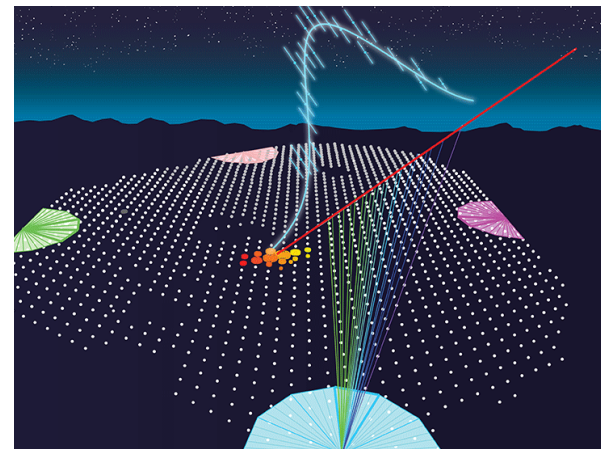
```
model.compile(loss='MSE', optimizer='SGD')
```

```
model.fit(xdata, ydata, epochs=200)
```



Air Shower Reconstruction

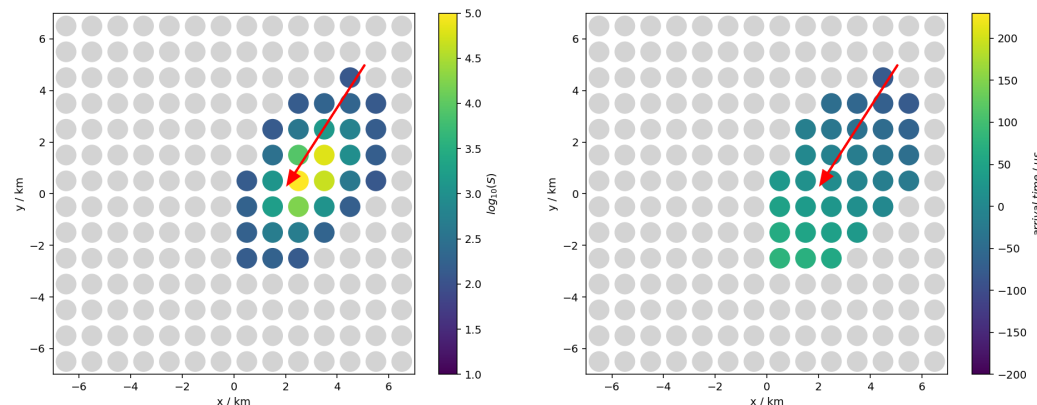
- Cosmic-ray-induced air showers
 - ♦ 14 x 14 particle detectors, arranged in a Cartesian grid at a height of 1400 m
 - ♦ stations measure arrival time of the shower and the deposited energy



$E = 11.4 \text{ EeV}$, $\theta = 56.1^\circ$, $\phi = 57.2^\circ$

Task

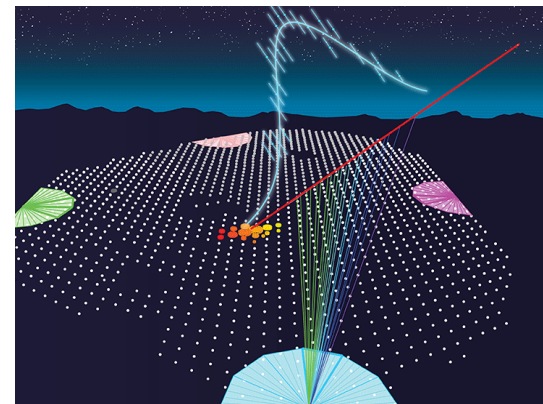
- Create Google Account
- Reconstruct energy of the shower
 - ♦ footprint is 2D image
 - ♦ cannot directly be used as input
 - reshape to a vector with length $(14 \times 14 \times 2 = 392)$



Air Shower Reconstruction - FCN

Now: OPEN tutorial at:

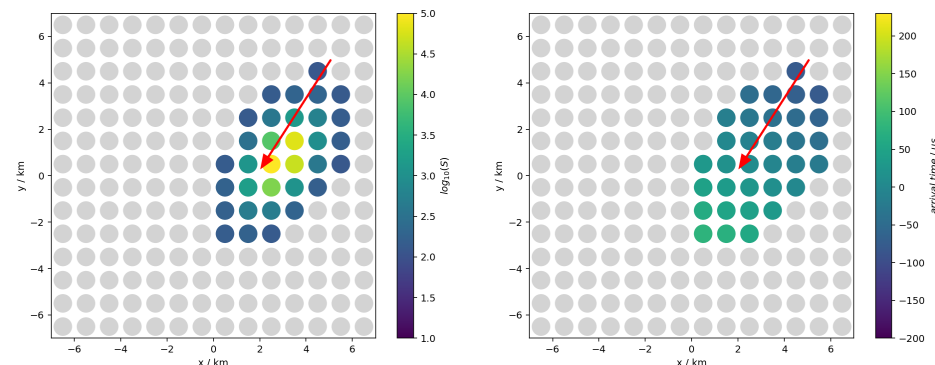
- www.deeplearningphysics.org/ and open Exercise 7.2
- or click and login



$E = 11.4 \text{ EeV}$, $\theta = 56.1^\circ$, $\phi = 57.2^\circ$

Task

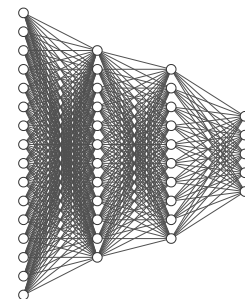
- Reconstruct energy of the shower
 - ♦ footprint is 2D image
 - ♦ cannot directly be used as input
 - reshape to a vector with length $(14 \times 14 \times 2 = 392)$
 - ♦ Try to reach a resolution better than 3.6 EeV



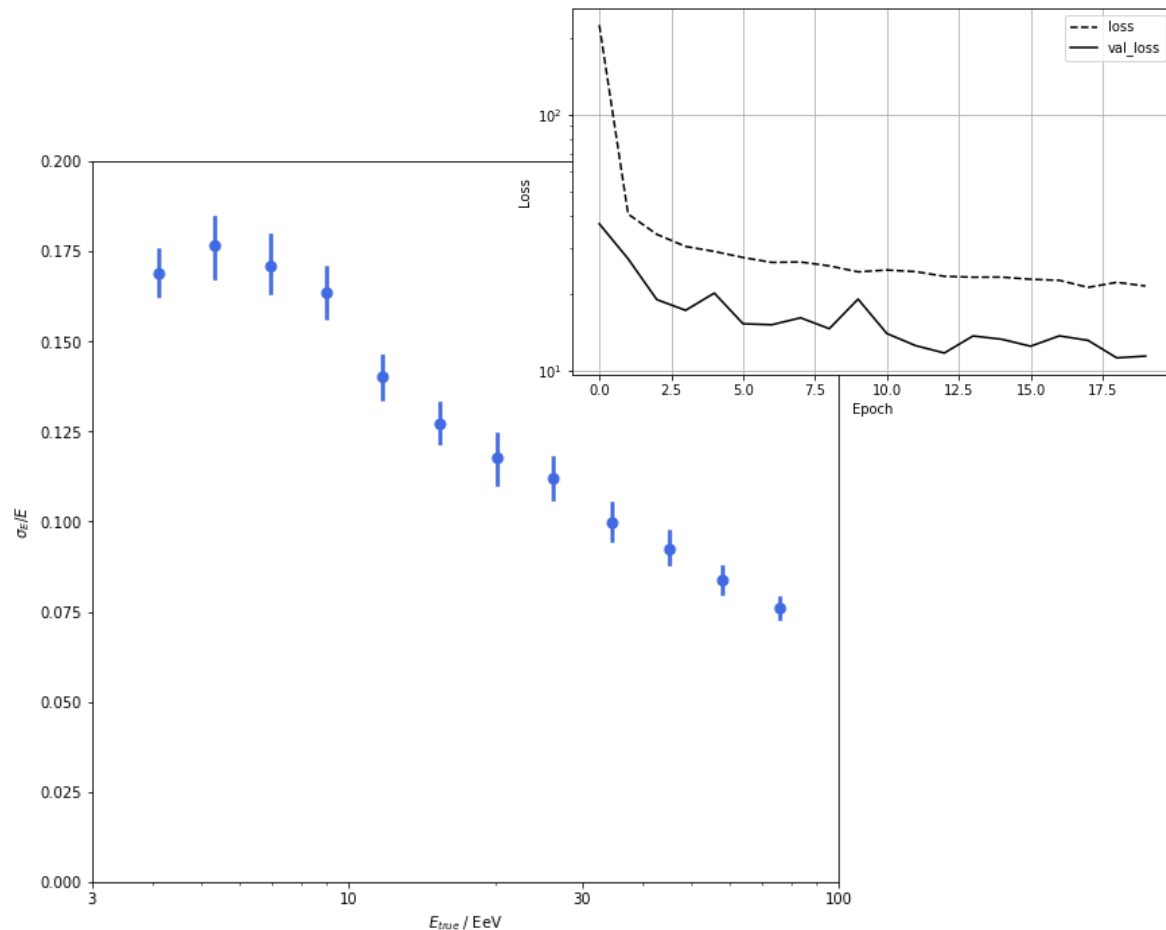
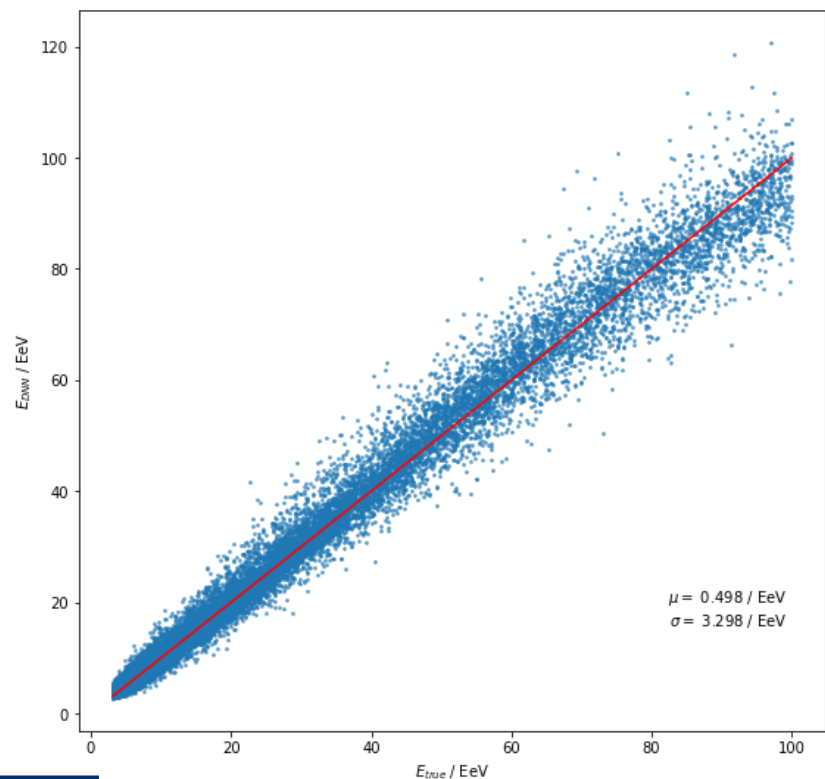
Results I

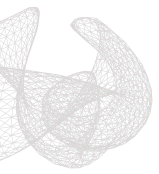
- Train fully-connected network as benchmark
- Model – **add**:
 - ♦ additional layers
 - ♦ more nodes
 - ♦ regularization (Dropout)

```
model = keras.models.Sequential()  
model.add(layers.Flatten(input_shape=X_train.shape[1:]))  
model.add(layers.Dense(100, activation="elu"))  
model.add(layers.Dense(100, activation="elu"))  
model.add(layers.Dense(100, activation="elu"))  
model.add(layers.Dense(100, activation="elu"))  
model.add(layers.Dropout(0.3))  
model.add(layers.Dense(1))
```

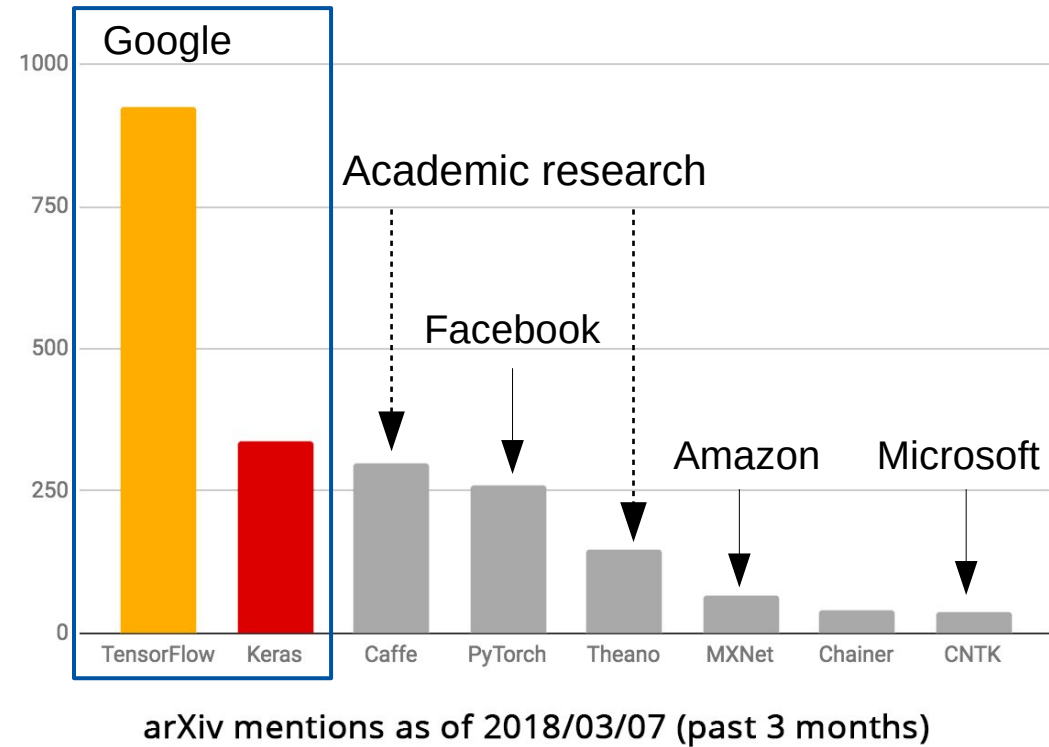


Results II





Practice II



Clarifying frequent misunderstandings



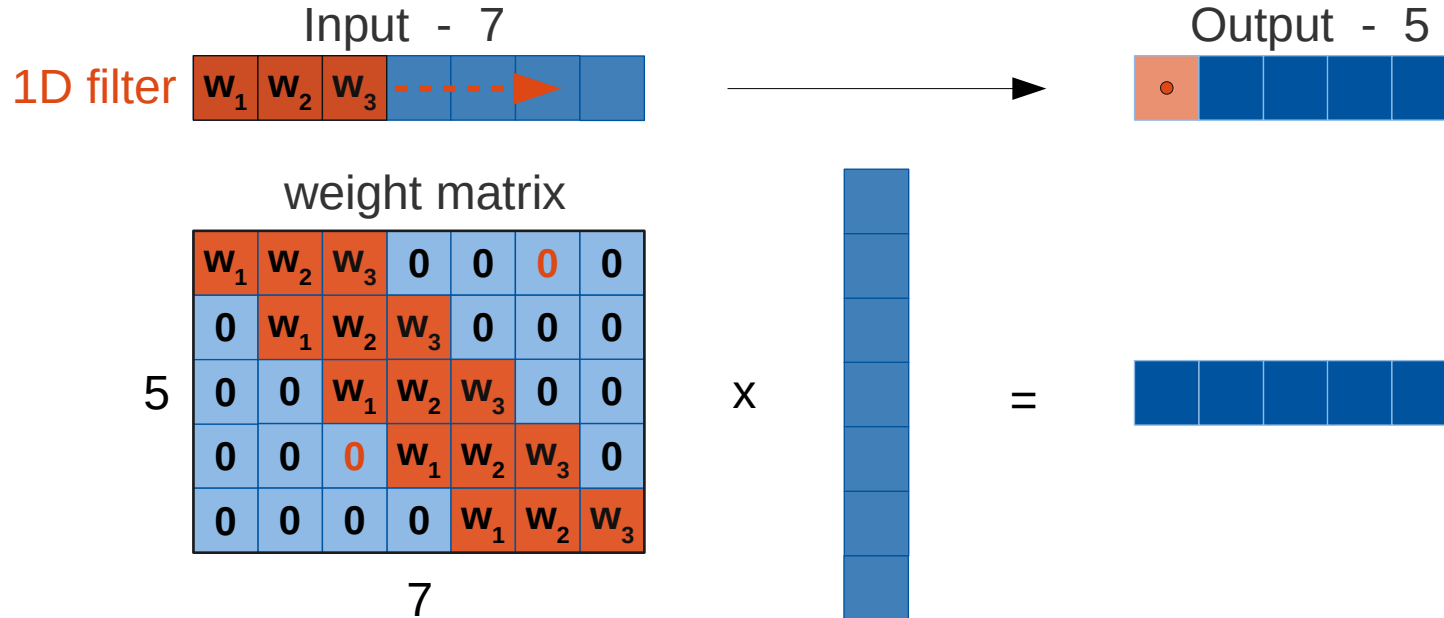
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- The **filters are no pre-defined** by the user → just width and depth and number
 - ♦ filters are adapted / learned by the CNN during training
- **Number of filters define number of new feature maps**
 - ♦ ten 3x3 filter applied to RGB image → 10 feature maps
- **Filter has the depth of the input image** (e.g. depth 3 for RGB images)
 - ♦ two 3x3 filter applied to RGB image → 2 feature maps, i.e. 2 channels
→ number of adaptive parameters = $3 \times 3 \times 3 \times 2 + 2 = 56$
- **After each convolutional operation an activation is applied!** (usually)
- **CNN part is followed by a fully-connected part** (in most cases)
 - output is reshaped (flattened) to a vector → apply vanilla NN layer

Convolutional Operation

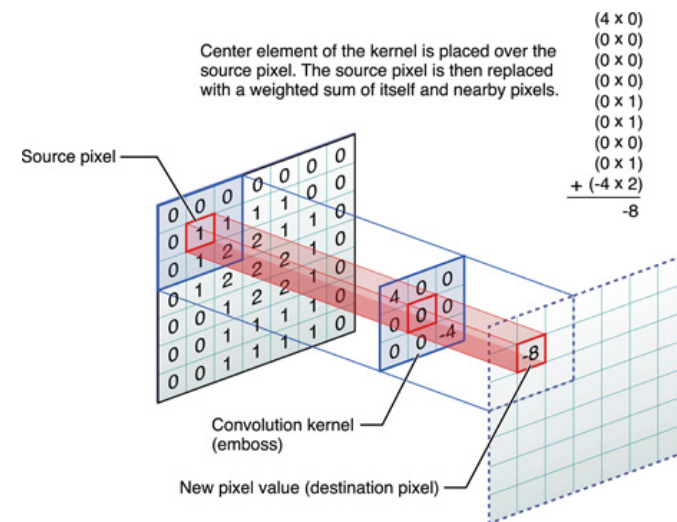
- Fully connected layers are special case of convolutional layers



- Parameters greatly reduced due to **sparsity** and **weight sharing**
- Strong prior on **local correlation** and **translational invariance**

Summary

- 2D Convolution acts on 3D input (width x height x depth)
- Slide small filter over input and make linear transformation (dot product + bias)
- Hyperparameter:
 - Size of filter, typically (1 x 1), (3 x 3), (5 x 5) or (7 x 7)
 - Number of filters (feature maps)
 - **Padding** (maintain spatial extent)
 - **Striding** or **pooling** (reduce spatial extent)
- Reduction of parameters using symmetry in data:
 - Prior on **local correlations** (use small filters)
 - **Translational invariance** (weight sharing)



Convolutional Layers - Keras

- Same Syntax as for fully connected layers

```
layers.Convolution2D(32, kernel_size=(5, 5), padding='same', activation='relu', strides=(2, 2))
```

- layer with 32 filters, size of filter 5x5 pixels, stride of 2 in both directions, and ReLU
- Use padding='same' to keep spatial dimension (else padding='valid')

Pooling and transition to fully-connected networks

- Pooling layer with pooling size of 2x2 pixels and a stride of 2 in both dimensions

```
layers.MaxPooling2D((2,2), strides=(2, 2)) // layers.AveragePooling2D((2,2), strides=(2, 2))
```

- Layer flattens output to vector → allows use of Dense layers after Convolutions

```
layers.Flatten()
```

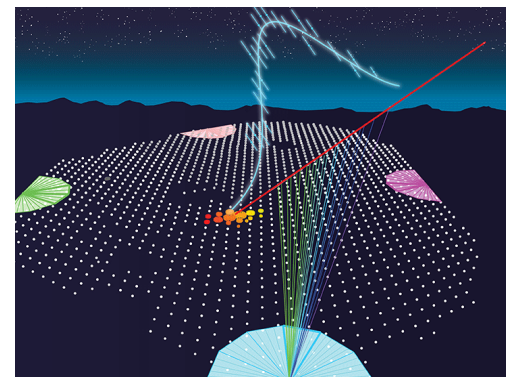
- Pooling operation on complete feature map → (remove all pixel dimensions + Flatten)

```
layers.GlobalMaxPooling2D() // layers.GlobalAveragePooling2D()
```

Air Shower Reconstruction - CNN

Now: OPEN tutorial at:

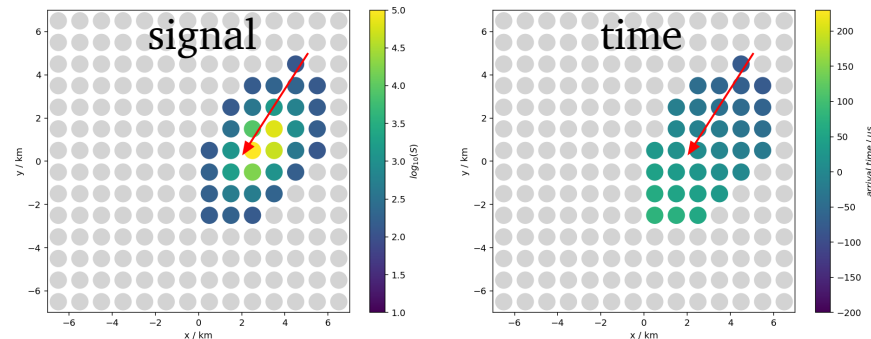
- www.deeplearningphysics.org/ and open Exercise 8.2
- or click and login



$E = 11.4 \text{ EeV}$, $\theta = 56.1^\circ$, $\phi = 57.2^\circ$

Task

- Reconstruct energy of the shower
 - ♦ Footprint is 2D image
 - ♦ **can** directly be used as input
 - input shape: $14 \times 14 \times 2$
 - ♦ Try to reach a resolution better than 1.9 EeV! (try, e.g., CNN pyramid!)



Results I

Model – add:

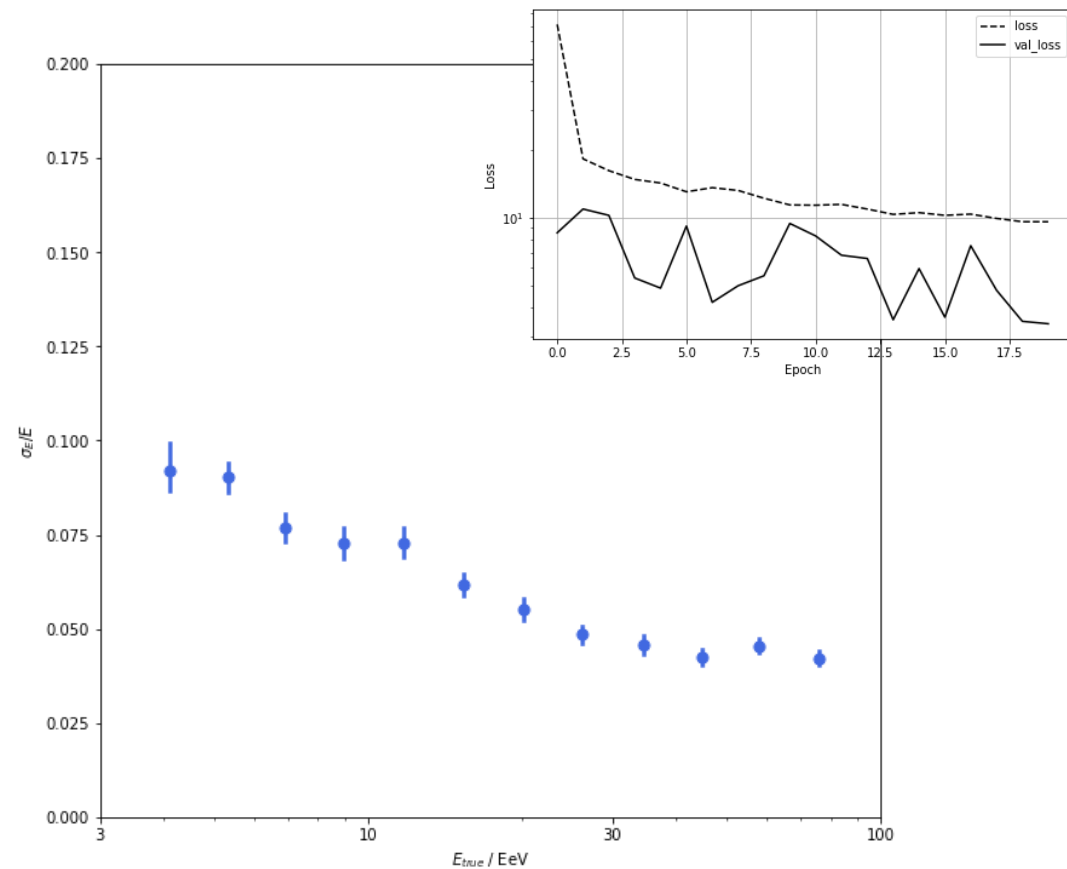
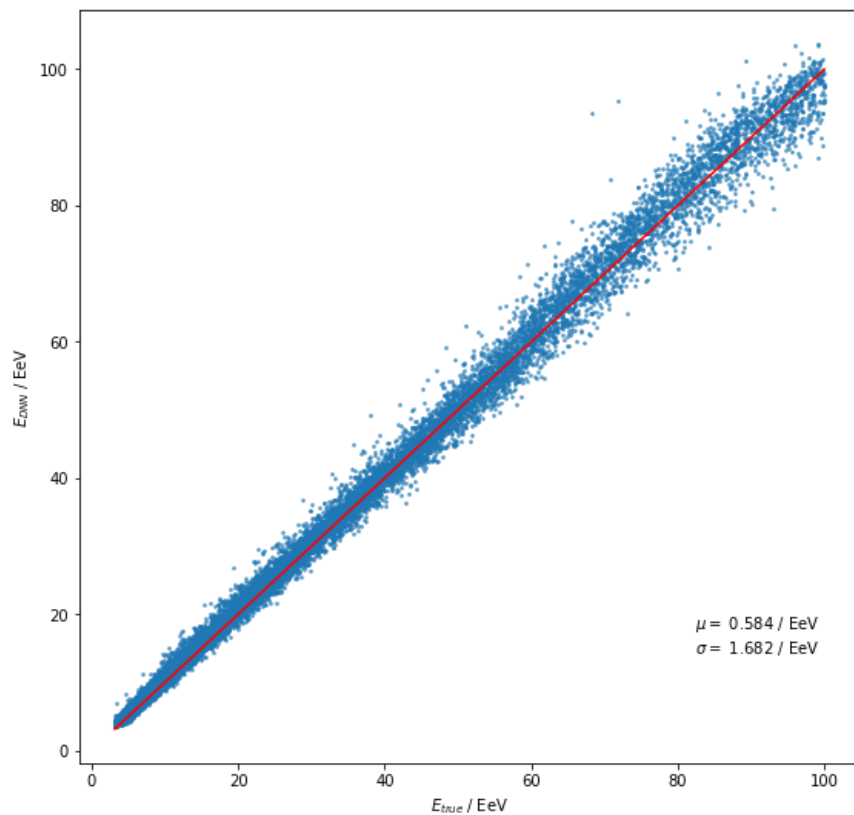
- Conv. layers and filters
- Pooling, Dense (FC) layers
- Regularization (after Flatten)

Model – modify:

- Batch size, epochs
- Kernel size, strides
- Optimizer, learning rate

```
kwargs = dict(activation='elu', padding='same',)
model = models.Sequential()
model.add(layers.Conv2D(32, (3, 3),
input_shape=X_train.shape[1:], **kwargs))
model.add(layers.Conv2D(32, (3, 3), **kwargs))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(64, (3, 3), **kwargs))
model.add(layers.Conv2D(64, (3, 3), **kwargs))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(128, (3, 3), **kwargs))
model.add(layers.Conv2D(128, (3, 3), **kwargs))
model.add(layers.GlobalMaxPooling2D())
model.add(layers.Dropout(0.3))
model.add(layers.Dense(1))
```

Results II

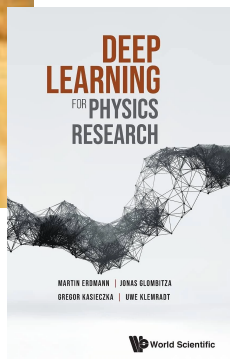


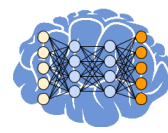
Tryout Deep Learning Yourself!

Find many physics examples at:
<http://www.deeplearningphysics.org/>

For example:

- CNNs, RNNs, GCNs
- GANs and WGANs
- Anomaly detection, Denosing AEs
- Visualization & introspection and more



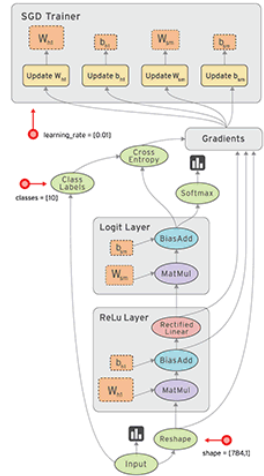


Graphs in TensorFlow 2.x

- Training of models is done using computational graphs!
 - Allows for high performance

TF2.0: graph \leftrightarrow function (input generates output)

- Simply add **@tf.function** decorator \rightarrow compiles function to TF graph
 - Note, only main function (training step) needs the decorator
all following function calls will be transformed also!



```
a = tf.Variable(1.0)
```

```
@tf.function # this is all you have to do
```

```
def f(x, a):
```

```
    return a.assign_add(a * x)
```

```
print(f(1.0, a))
```


Variables & Datasets

- **Variables** can be modified → Use for network **weights** and **biases**

```
W = tf.Variable([1., 2.])  
--> <tf.Variable 'Variable:0' shape=(2,) dtype=float32, numpy=array([1, 2], dtype=float32)>
```

- Use tf.datasets or numpy arrays to build input pipelines!
 - Used to pass data (x, y) through the graph

```
dataset = tf.data.Dataset.from_tensor_slices(([8., 3., 0., 8., 2., 1.], [16., 6., 0., 16., 8., 2.])) # input, output  
model = Model() # build the model
```

```
for x, y in dataset: # loop over dataset
```

```
    current_loss = (y - model(x))**2 # calculate loss (forward pass)
```

```
    ...
```

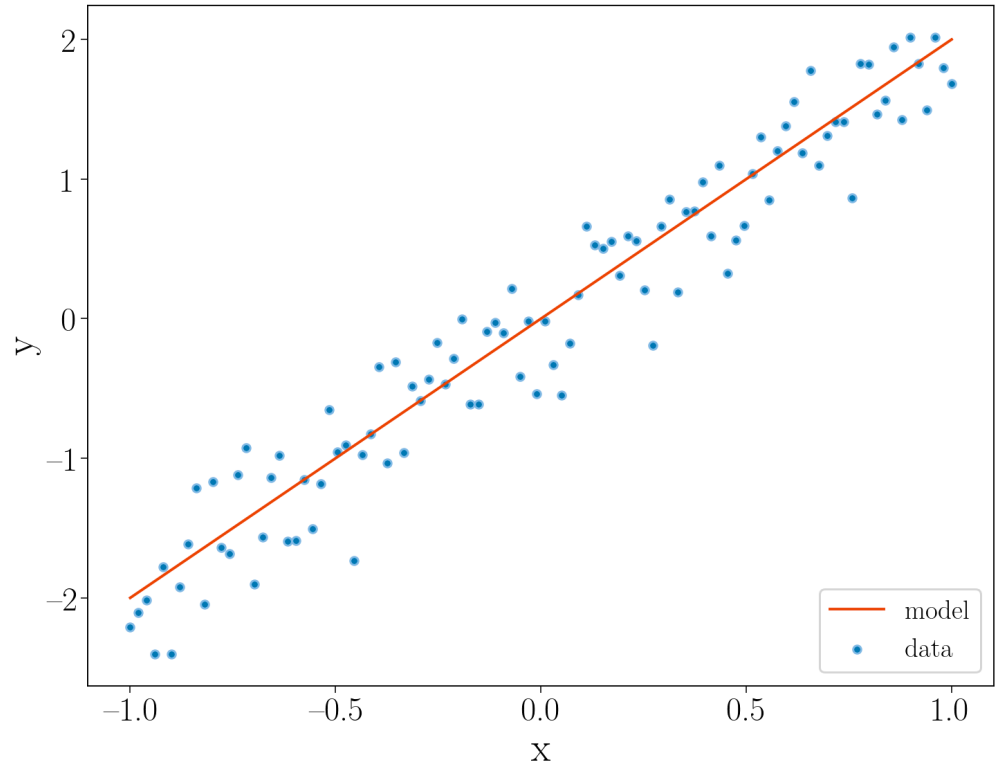
Example 1: Linear Regression

Linear model with slope = 2 and some noise

- Generate some data:

```
xdata = np.linspace(-1, 1, 100)
ydata = 2 * xdata + np.random.randn(100) * 0.3
```

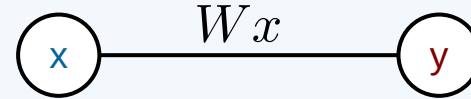
- Fit linear model using TensorFlow



Example 1: Linear Regression

- Define TensorFlow model as Class! Owning an initialization and a call function.
 - ♦ Parameters belong to respective class

```
class Model(object):  
    def __init__(self):  
        # Initialize the slope to `0.1`  
        self.W = tf.Variable(.1)  
  
    def __call__(self, x):  
        return self.W * x  
  
    # define optimization procedure  
    def objective(x, y):  
        return tf.reduce_mean(tf.square(y - x))
```



$$J(\theta) = \frac{1}{N} \sum_{i=1}^N [y_m(x_i) - y_i]^2$$

Example 1: Linear Regression

```
linear_model = Model() # build model

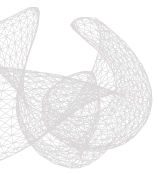
for i in range(100):

    with tf.GradientTape() as tape:

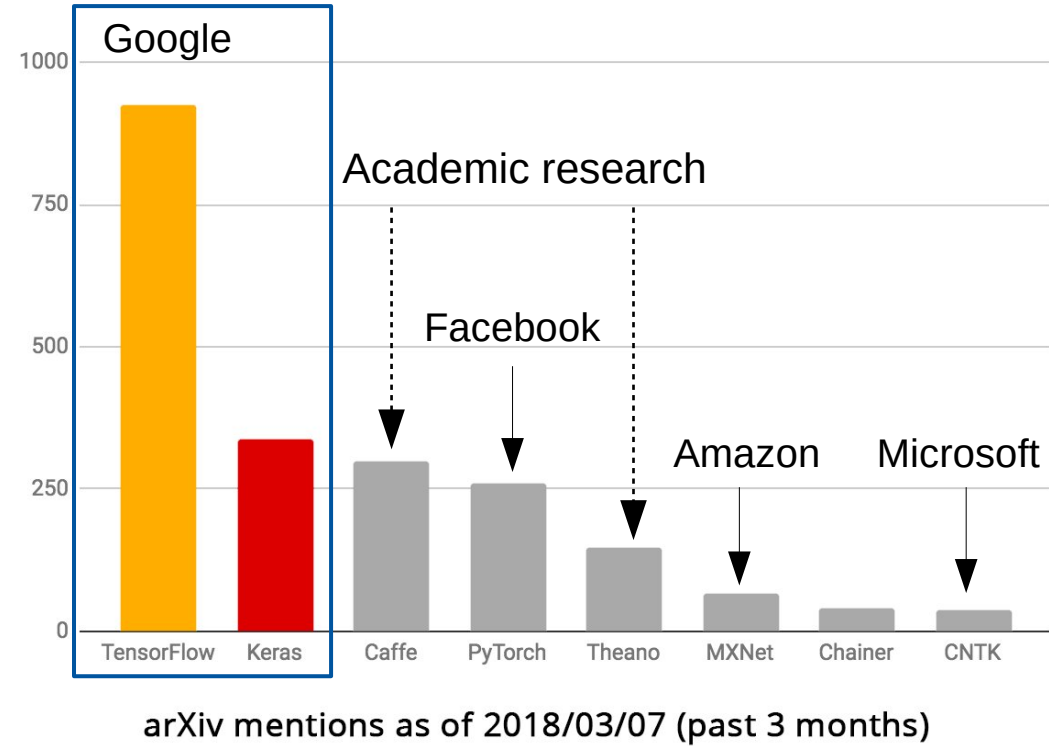
        # Forward pass
        current_loss = objective(y, linear_model(x))
        experiment.log_metric("loss", current_loss) # log metric to comet

        # Backward pass
        dW = tape.gradient(current_loss, linear_model.W) # calculate gradient
        # update model parameters assign_sub --> W -= lr * dW (gradient descent)
        linear_model.W.assign_sub(lr * dW)
```

- Update parameters of your linear model 100 times using gradient descent!

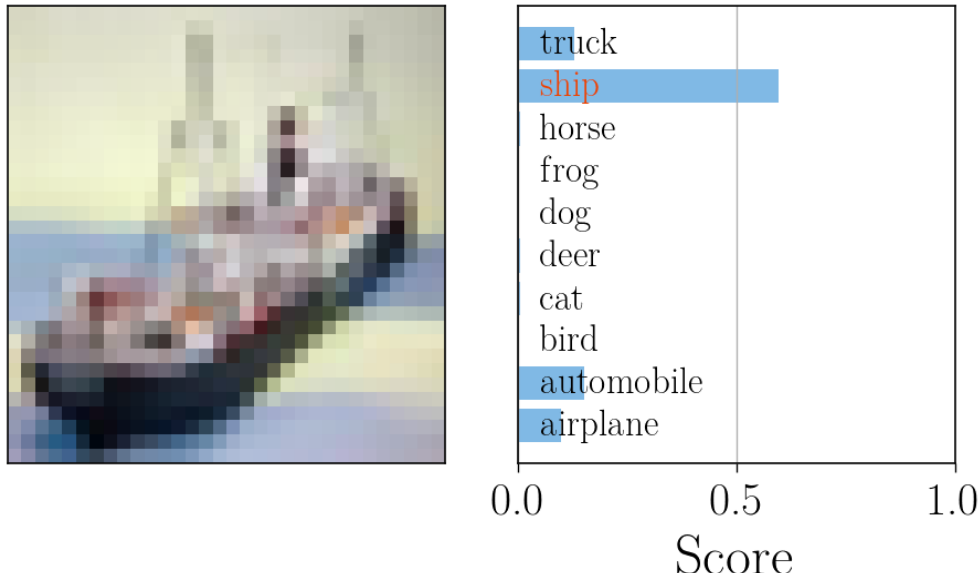


Bonus CIFAR-10



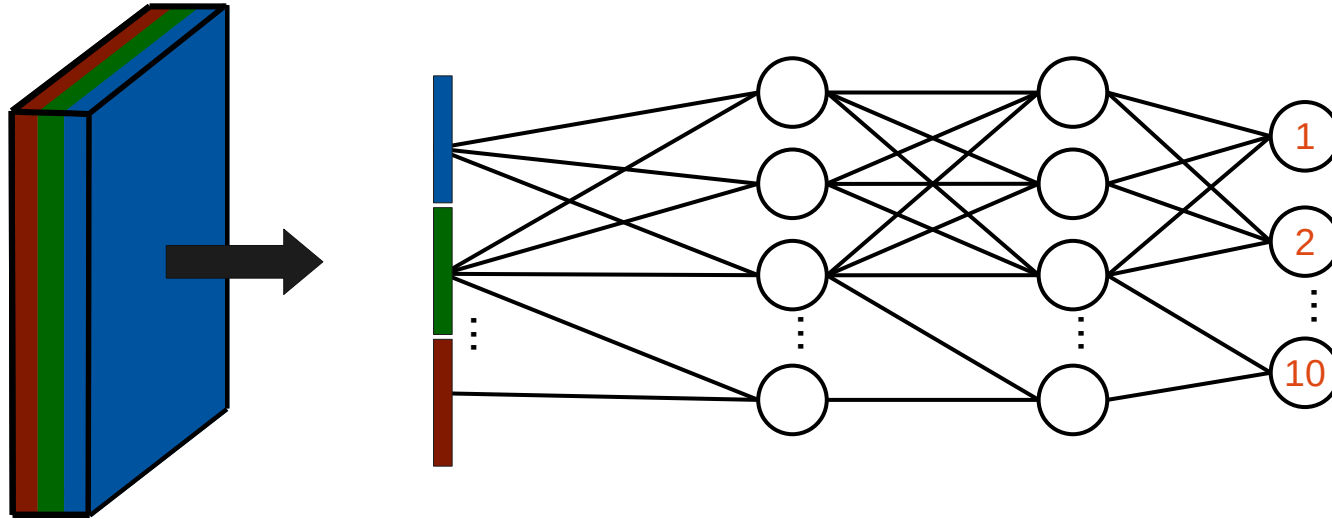
CIFAR-10 Classification Task

- 60,000 images with 10 classes
- Input $\mathbf{x} = (x_1, x_2, \dots, x_{3072})$, for $32 \times 32 \times 3 = 3072$ input features
- Output $\mathbf{y} = (y_1, y_2, \dots, y_{10})$, one for each class (one-hot encoded)
 - ♦ frog, airplane, automobile, bird, cat, deer, dog, horse, ship, truck



- Model should learn to estimate the conditional probability distribution
 - outputs probability for each class
$$\mathbf{y}_m(x_i|\theta) = (p_{\text{cat}}, p_{\text{dog}}, \dots)$$
- Take highest p_j as prediction
 - Value of p_j states certainty

Fully Connected Network



- Input layer: Flatten image to $32 \times 32 \times 3 = 3072$ vector
- Use fully connected network with some hidden layers, ReLU and dropout
- Output layer: 10 layer output with softmax
- Measure performance with independent **validation set**

Exercise II

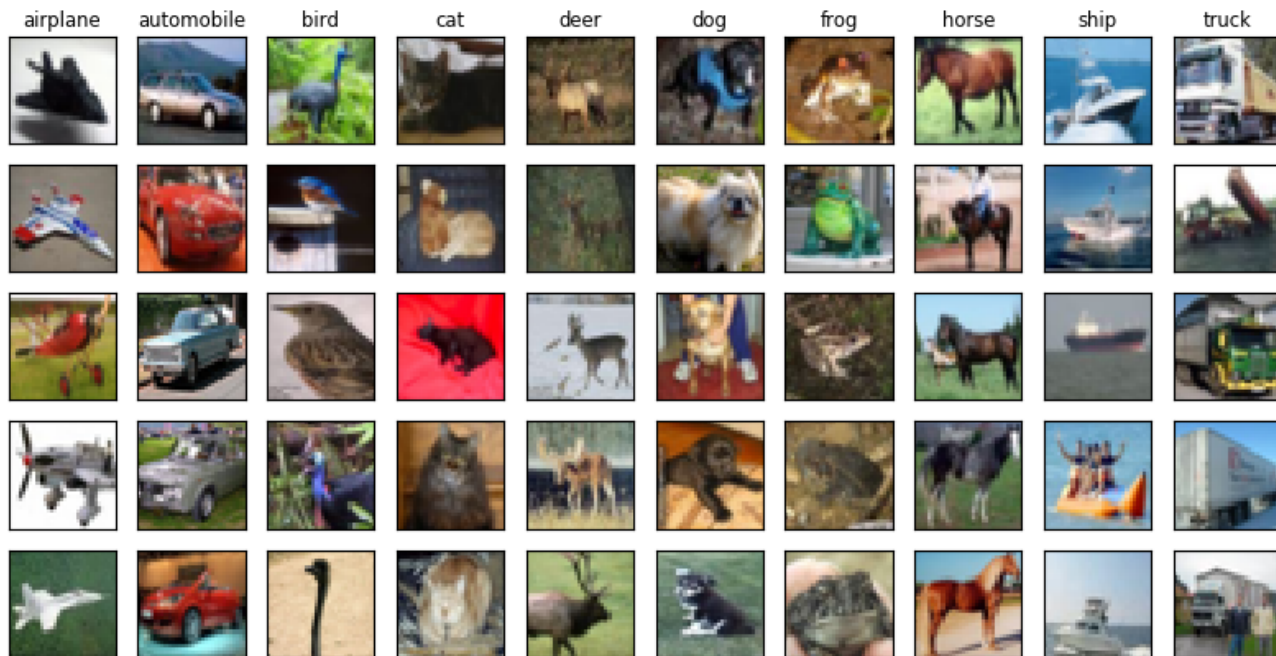
- 60,000 images with 10 classes
- Input $\mathbf{x} = (x_1, x_2, \dots, x_{3072})$, for $32 \times 32 \times 3 = 3072$ input features
- Output $\mathbf{y} = (y_1, y_2, \dots, y_{10})$, one for each class (one-hot encoded)
 - ♦ frog, airplane, automobile, bird, cat, deer, dog, horse, ship, truck



Open in Colab

Try to reach close to 50%
validation accuracy!

https://github.com/jglombitza/cifar_tutorial



CIFAR 10 – Convolutional Networks



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Model – add:

- Conv. layers and filters
- Pooling, Dense (FC) layers
- Regularization (after Flatten)

Model – modify:

- Batch size, epochs
- Kernel size, strides
- Optimizer, learning rate

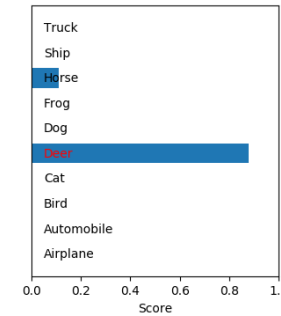
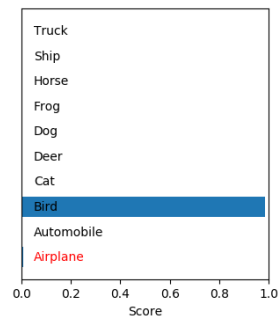
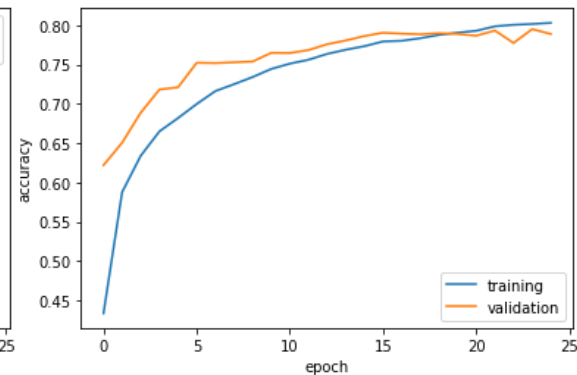
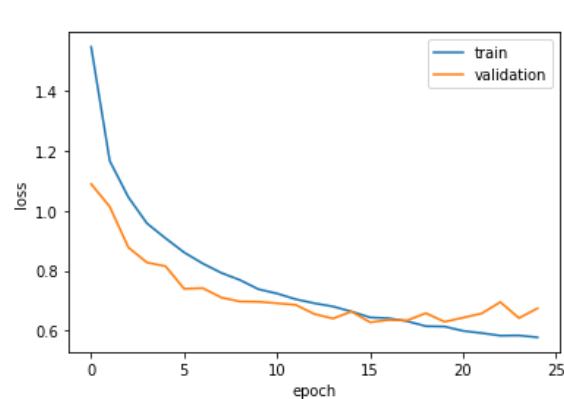
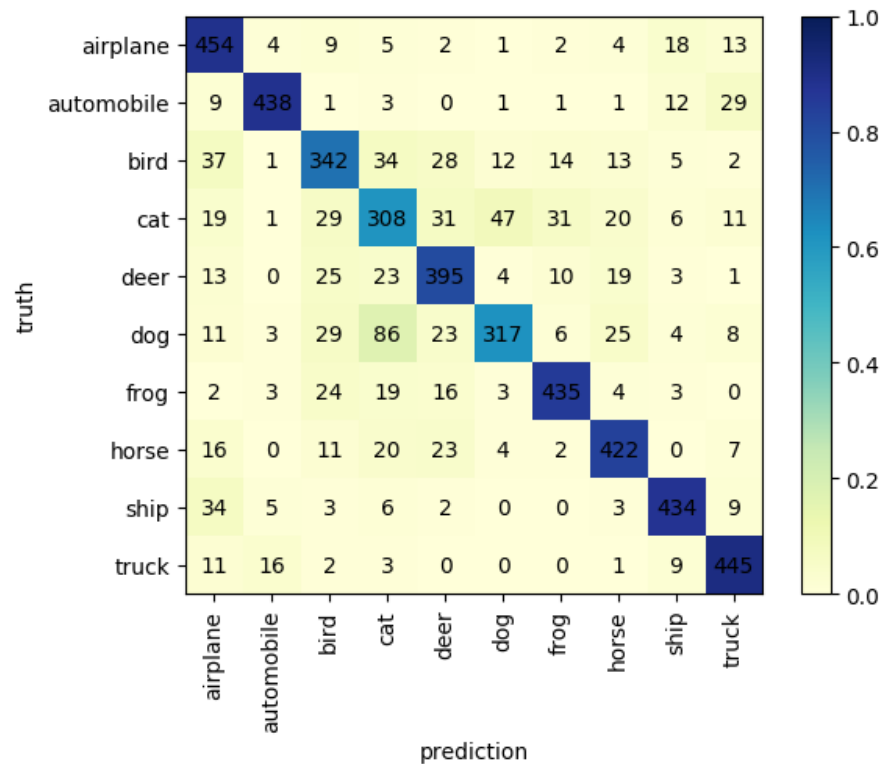
```
model = models.Sequential([
    layers.Convolution2D(32, kernel_size=(5, 5), padding='same',
                        activation='relu', input_shape=(32, 32, 3)),
    layers.MaxPooling2D((2, 2)),
    layers.Convolution2D(64, kernel_size=(3, 3), padding='same',
                        strides=(2, 2), activation='relu'),
    layers.Flatten(),
    layers.Dropout(0.3),
    layers.Dense(10, activation='softmax')
])
```

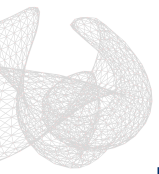


➤ **Can you achieve >75% validation accuracy?**

```
model = models.Sequential([
    layers.Convolution2D(16, kernel_size=(3, 3), padding='same', activation='elu',
                        input_shape=(32, 32, 3)),
    layers.Convolution2D(32, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.Convolution2D(32, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.MaxPooling2D((2, 2)),
    layers.Convolution2D(32, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.Convolution2D(64, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.Convolution2D(64, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.MaxPooling2D((2, 2)),
    layers.Convolution2D(64, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.Convolution2D(128, kernel_size=(3, 3), padding='same', activation='elu'),
    layers.GlobalMaxPooling2D(),
    layers.Dropout(0.5),
    layers.Dense(10, activation='softmax')])
```

Results





Tryout Deep Learning Yourself!

Find many physics examples at:
<http://www.deeplearningphysics.org/>

For example:

- CNNs, RNNs, GCNs
- GANs and WGANs
- Anomaly detection, Denosing AEs
- Visualization & introspection and more

