## How do particles escape from accelerators?



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#### Plan of the lecture

- [1] Supernova remnants are spherical
- [2] Dynamical evolution of SNRs
- [3] Cosmic ray escape from SNRs (naive)

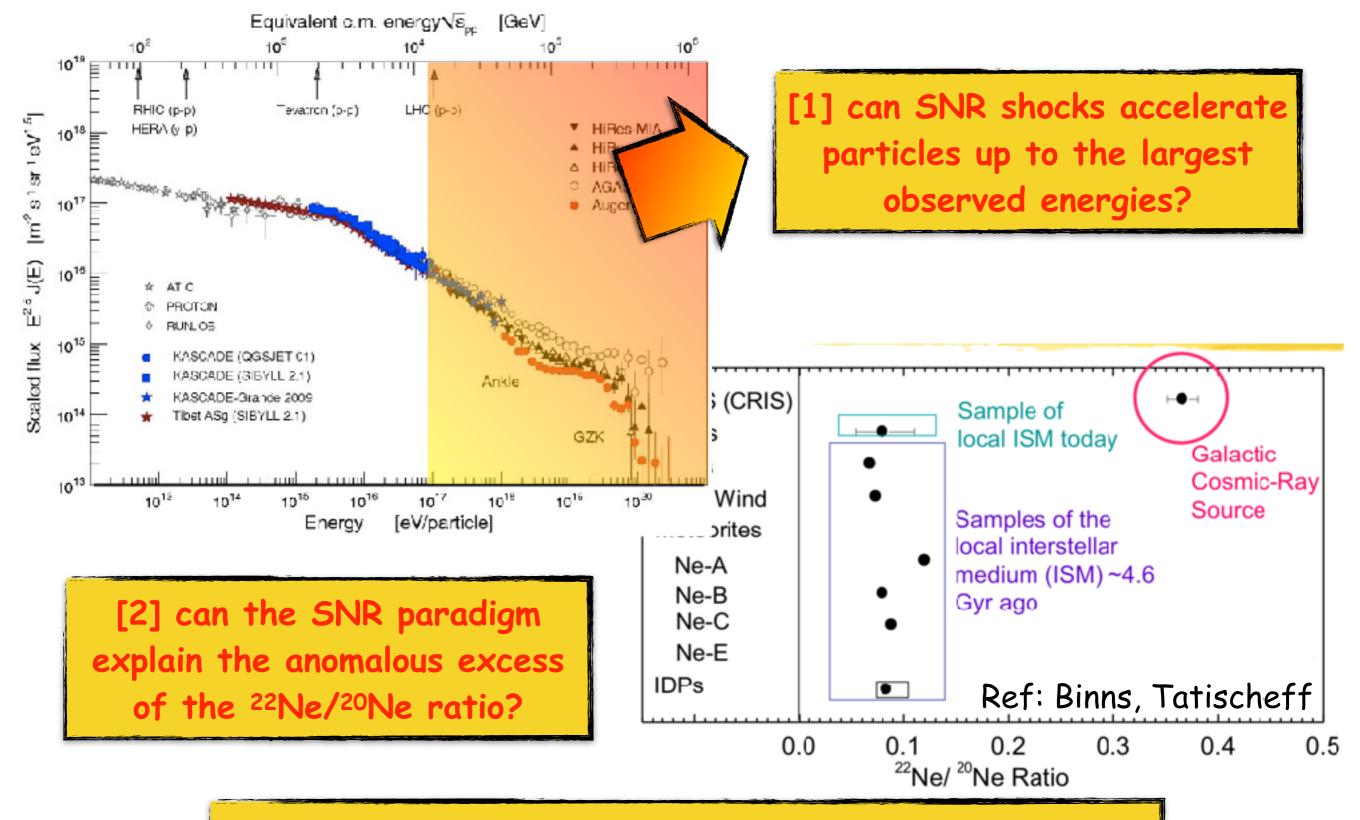
Supernova remnants

CR escape from sources

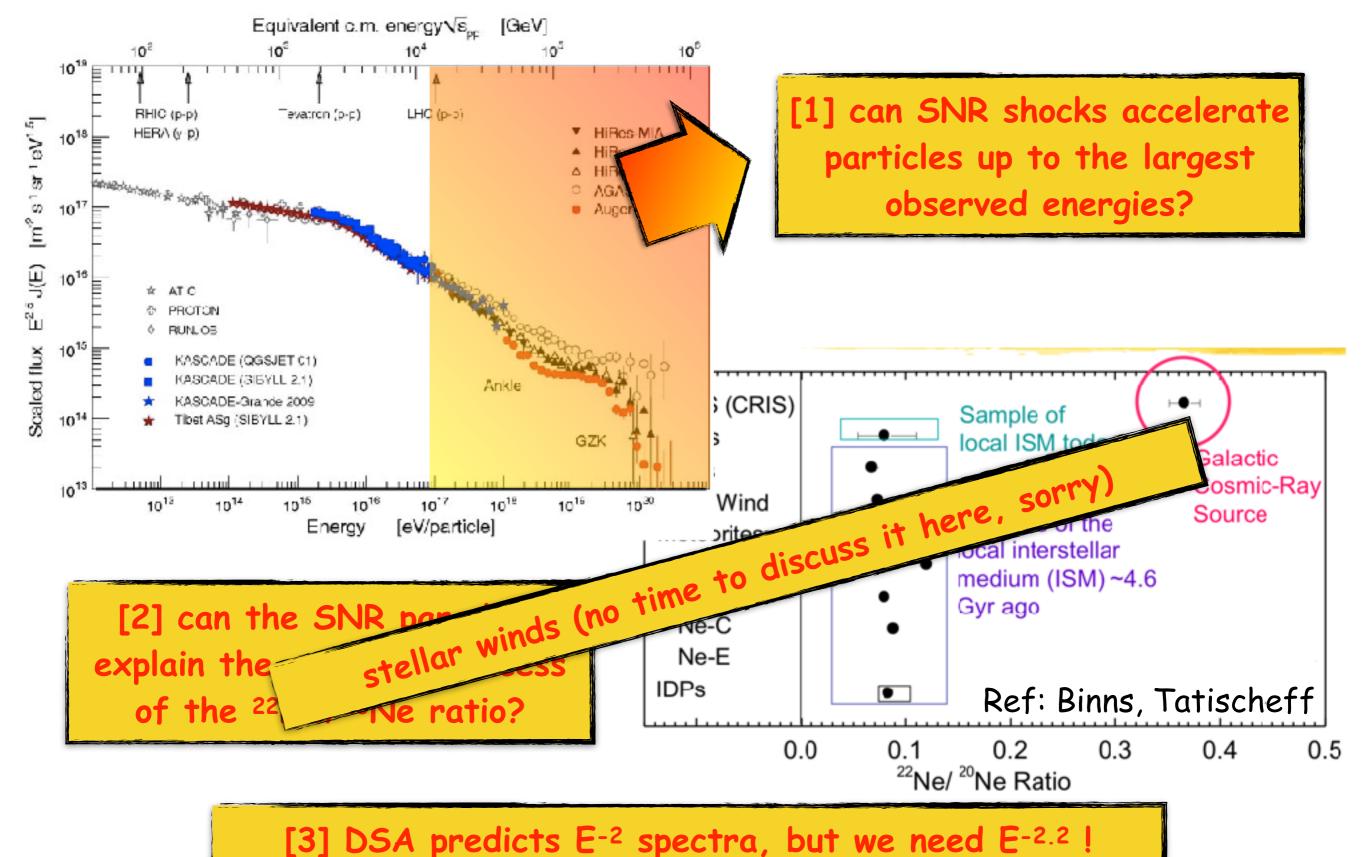
- [5] CR escape from SNRs (a bit more formal, but still quite hand wavy...)
- [6] maximum energy of accelerated CRs
- [7] spectrum of escaping CRs

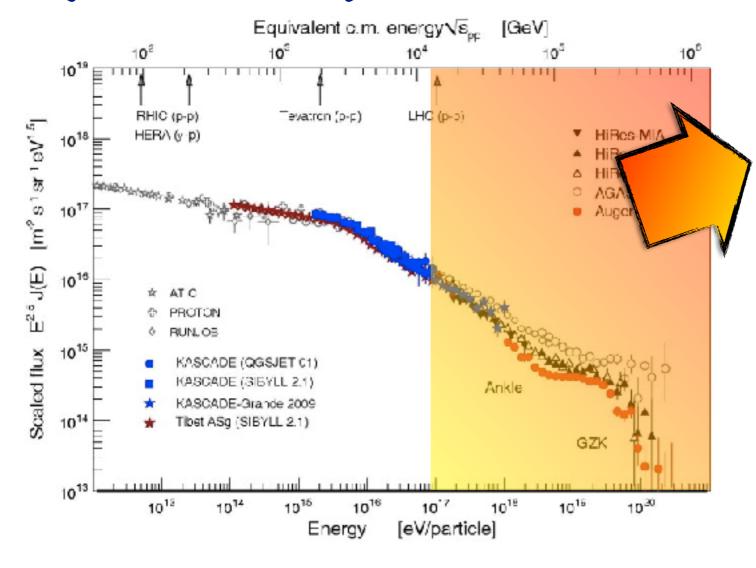
Conclusions

## Supernova remnants

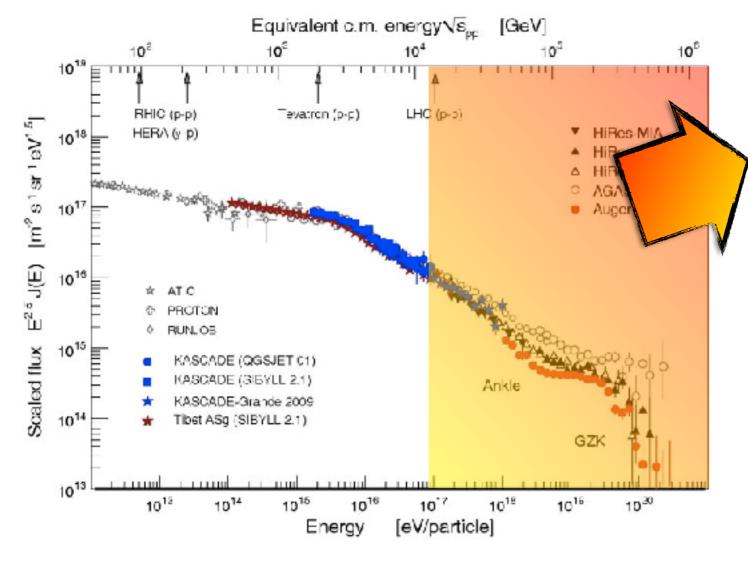


[3] DSA predicts E-2 spectra, but we need E-2.2!





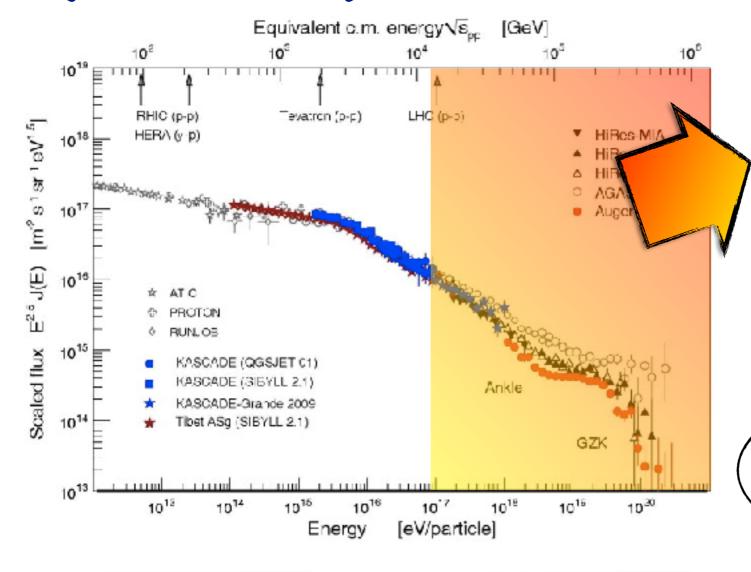
[1] can SNR shocks accelerate particles up to the largest observed energies?



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to answer this one needs to understand particle escape from the accelerator

[3] DSA predicts E-2 spectra, but we need E-2.2!



[1] can SNR shocks accelerate particles up to the largest observed energies?

think about the extreme case where particles NEVER escape the accelerator...

to answer this one needs to understand particle escape from the accelerator

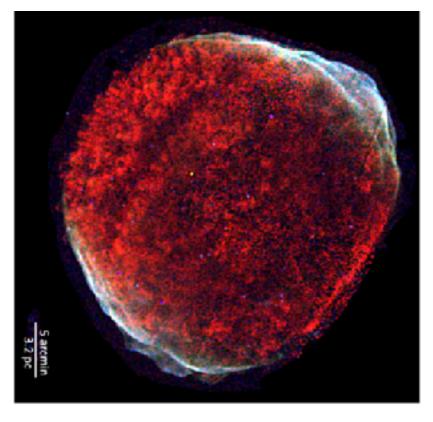
[3] DSA predicts E-2 spectra, but we need E-2.2!

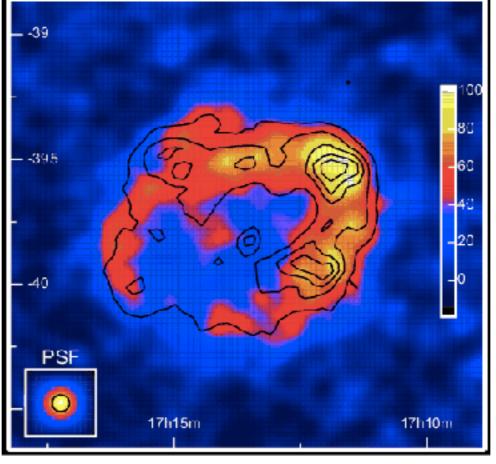
#### A small detail...

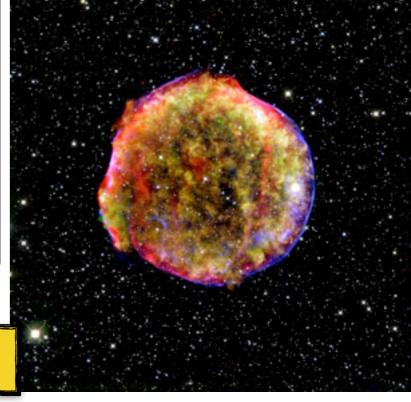
DSA: we considered a plane and infinite shock moving at constant speed

#### A small detail...

DSA: we considered a plane and infinite shock moving at constant speed







... SNRs are roughy spherical and the shock decelerates

interstellar medium

 $\begin{array}{cc} \text{pressure} \\ P & \varrho \end{array}$ 



massive star

interstellar medium

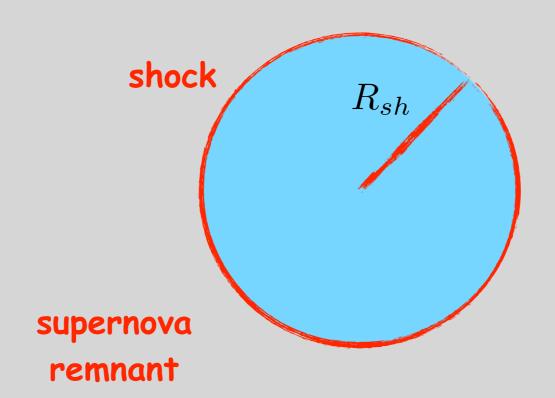
mass of the ejecta explosion energy

 $M_{ej}$   $E_{SN}$  P  $\varrho$ 



interstellar medium

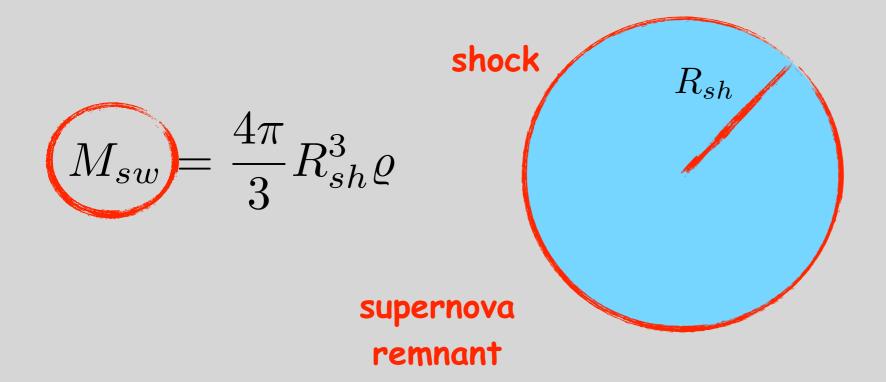
 $M_{ej}$   $E_{SN}$  P  $\varrho$ 



$$M_{ej}$$
  $E_{SN}$   $P$   $\varrho$ 

$$M_{sw} = \frac{4\pi}{3} R_{sh}^3 \varrho$$
 supernova remnant

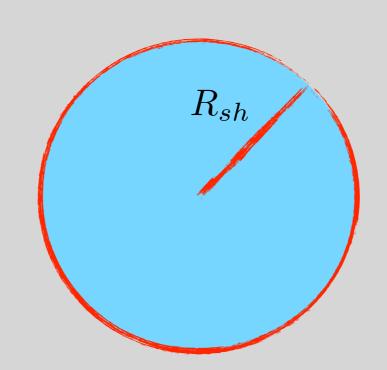




$$M_{ej} \gg M_{sw}$$

$$M_{ej}$$
  $E_{SN}$   $P$   $\varrho$ 

$$M_{sw} = \frac{4\pi}{3} R_{sh}^3 \varrho$$



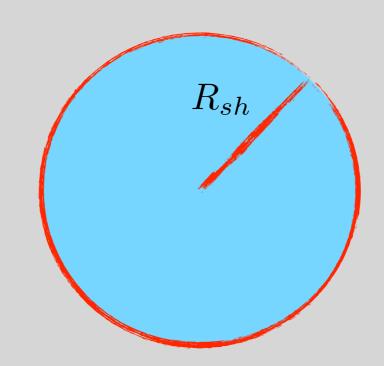
$$M_{ej}\gg M_{sw}$$

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  $E_{SN}$   $\nearrow$ 





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#### interstellar medium

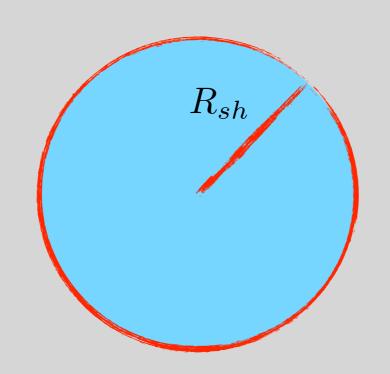
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 $M_{ej}$   $E_{SN}$  R





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free expansion (constant speed)

$$E_{SN} = \frac{1}{2} M_{ej} v_{sh}^2$$

#### interstellar medium

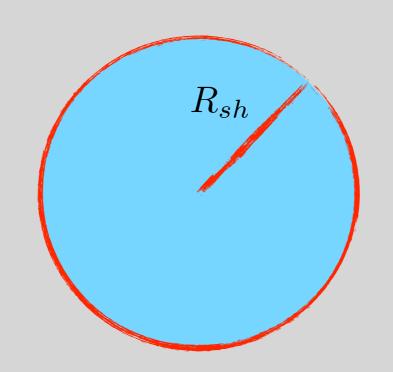
$$M_{ej}\gg M_{sw}$$

 $M_{ej}$   $E_{SN}$  ightharpoonup (





$$M_{sw} = \frac{4\pi}{3} R_{sh}^3 \varrho$$



free expansion (constant speed)

$$E_{SN} = \frac{1}{2} M_{ej} v_{sh}^2 \longrightarrow v_{sh} = \sqrt{\frac{2E_{SN}}{M_{ej}}} \sim 10000 \left(\frac{M_{ej}}{M_{\odot}}\right)^{-1/2} \text{km/s}$$

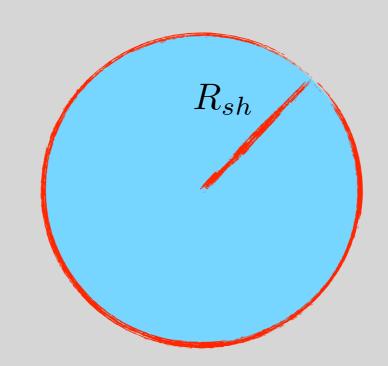
$$M_{ej} = M_{sw}$$

$$M_{ej}$$
  $E_{SN}$   $\nearrow$ 





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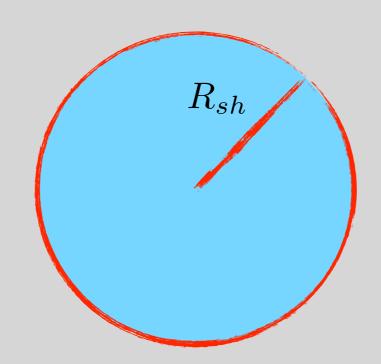
$$M_{ej}=M_{sw}$$
  $M_{ej}$   $E_{SN}$ 

$$M_{ej}$$
  $E_{SN}$ 





$$M_{sw} = \frac{4\pi}{3} R_{sh}^3 \varrho$$



$$R_* = \left(\frac{3M_{ej}}{4\pi\varrho}\right)^{1/3} \sim 2\left(\frac{M_{ej}}{M_{\odot}}\right)^{1/3} \left(\frac{n}{\text{cm}^{-3}}\right)^{-1/3} \text{pc}$$

#### interstellar medium

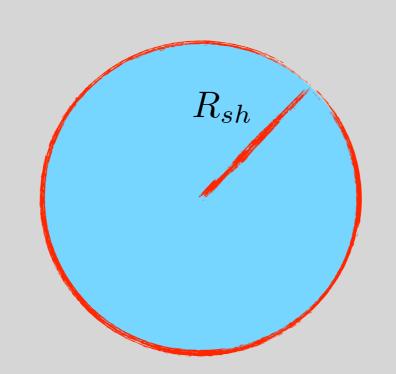
$$M_{ej}=M_{sw}$$
  $M_{ej}$   $E_{SN}$ 

$$M_{ej}$$
  $E_{S}$ 



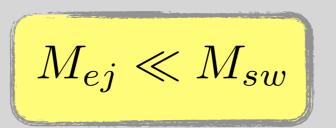


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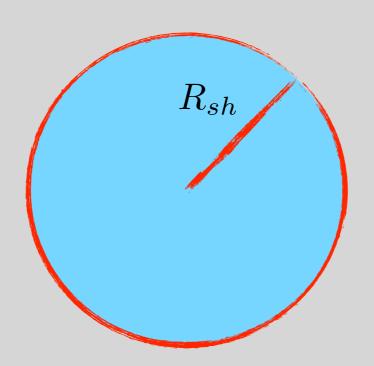


it takes few centuries to reach this moment

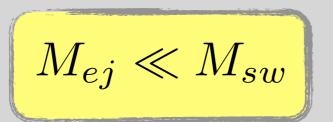
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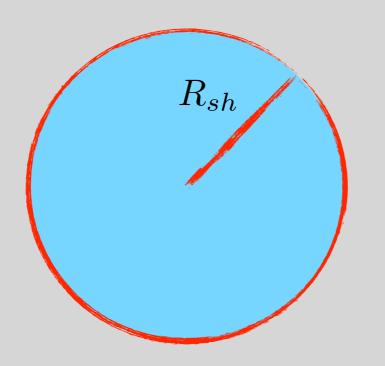
$$M_{ej}$$
  $E_{SN}$   $P$   $\varrho$ 



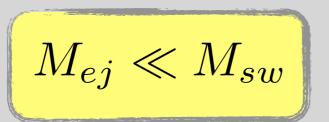
#### interstellar medium



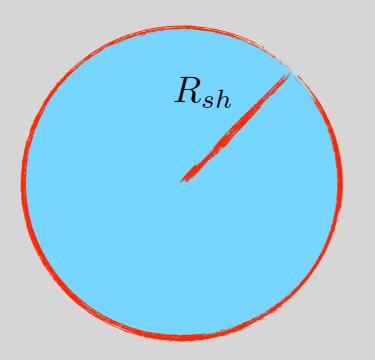
 $M_{ej}$   $E_{SN}$  P  $\varrho$ 



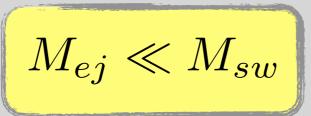
#### interstellar medium







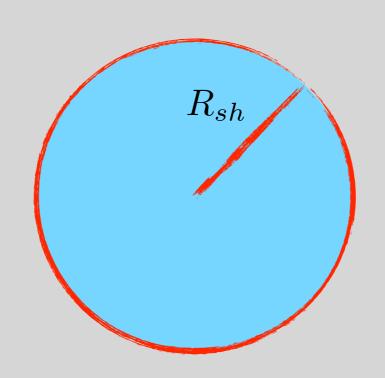
#### interstellar medium





 $c_s \approx 10 \text{ km/s}$ 

strong shock



#### interstellar medium

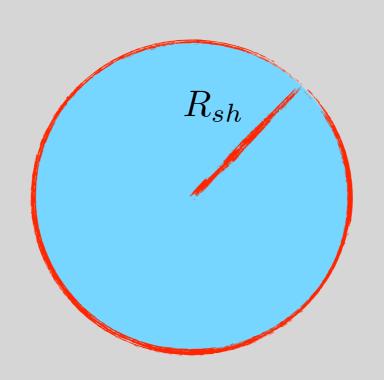




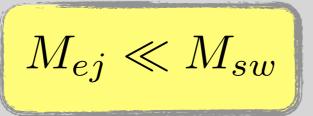


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#### interstellar medium

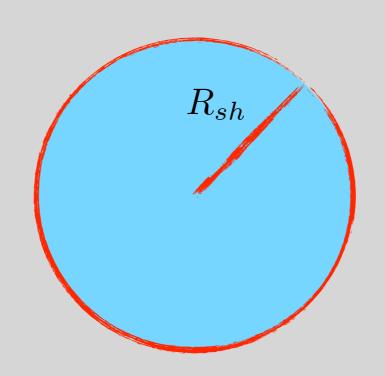






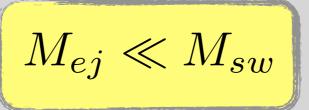
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non-dimensional quantity: 
$$a=\frac{\varrho~R_{sh}^5}{E_{SN}~t^2}$$

#### interstellar medium

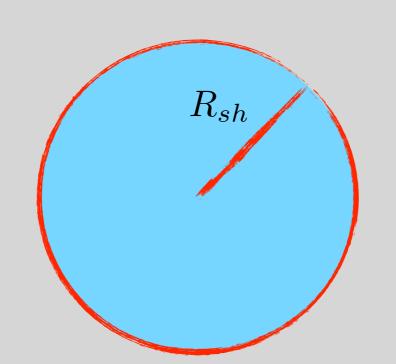






$$c_s \approx 10 \text{ km/s}$$

strong shock



non-dimensional quantity: 
$$a=\frac{\varrho\ R_{sh}^5}{E_{SN}\ t^2}\longrightarrow R_{sh}=a\left(\frac{E_{SN}}{\varrho}\right)^{1/5}t^{2/5}$$

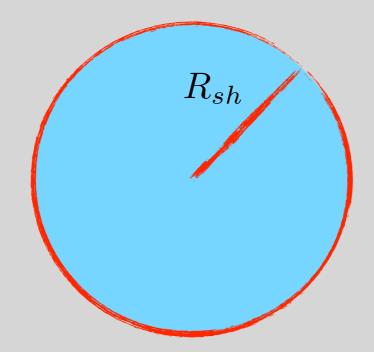
#### interstellar medium







Sedov-Taylor solution



$$R_{sh} = a \left(\frac{E_{SN}}{\varrho}\right)^{1/5} t^{2/5}$$

$$u_{sh} = \frac{2}{5} \frac{R_{sh}}{t} \propto t^{-3/5}$$

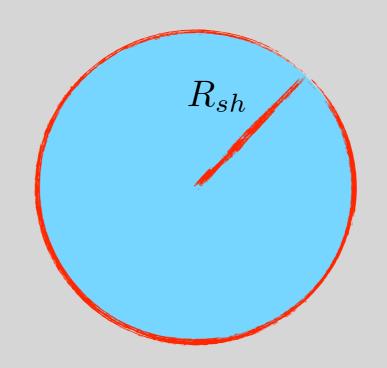
#### interstellar medium







Sedov-Taylor solution

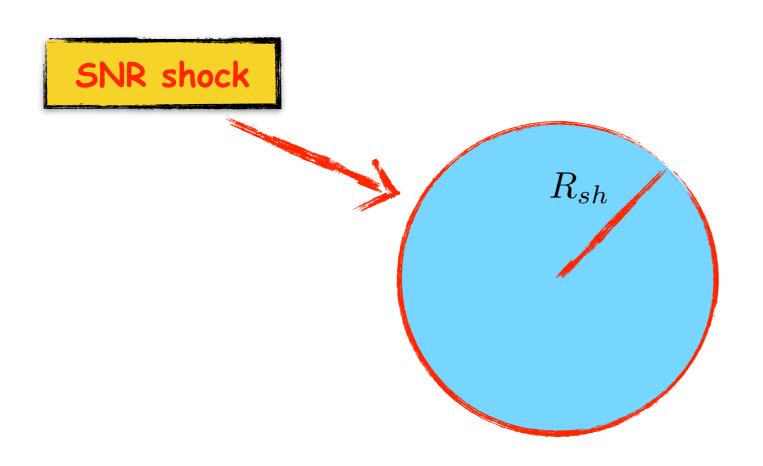


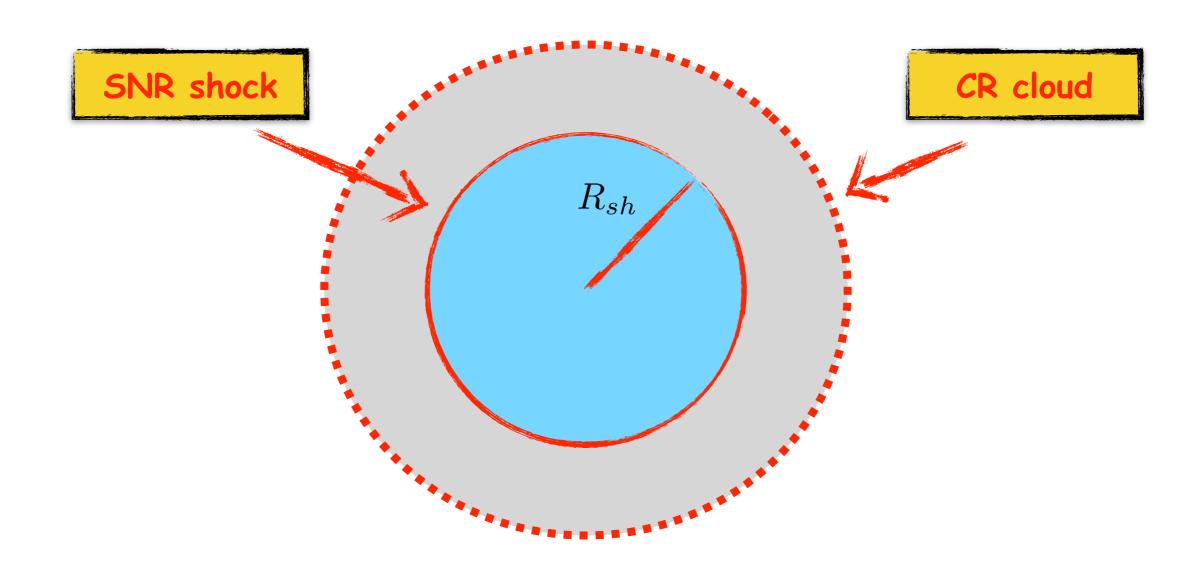
This solution holds until  $t\sim 10^4 - 10^5$  yr, after that the SNR cools due to emission of X-ray photons

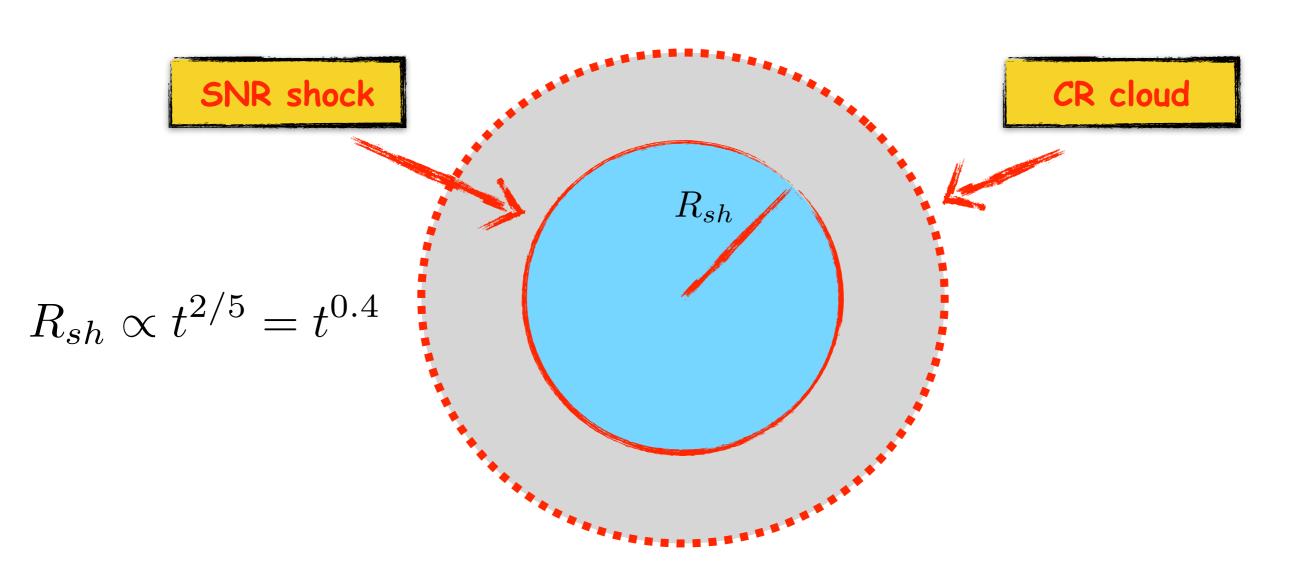
$$R_{sh} = a \left(\frac{E_{SN}}{\varrho}\right)^{1/5} t^{2/5}$$

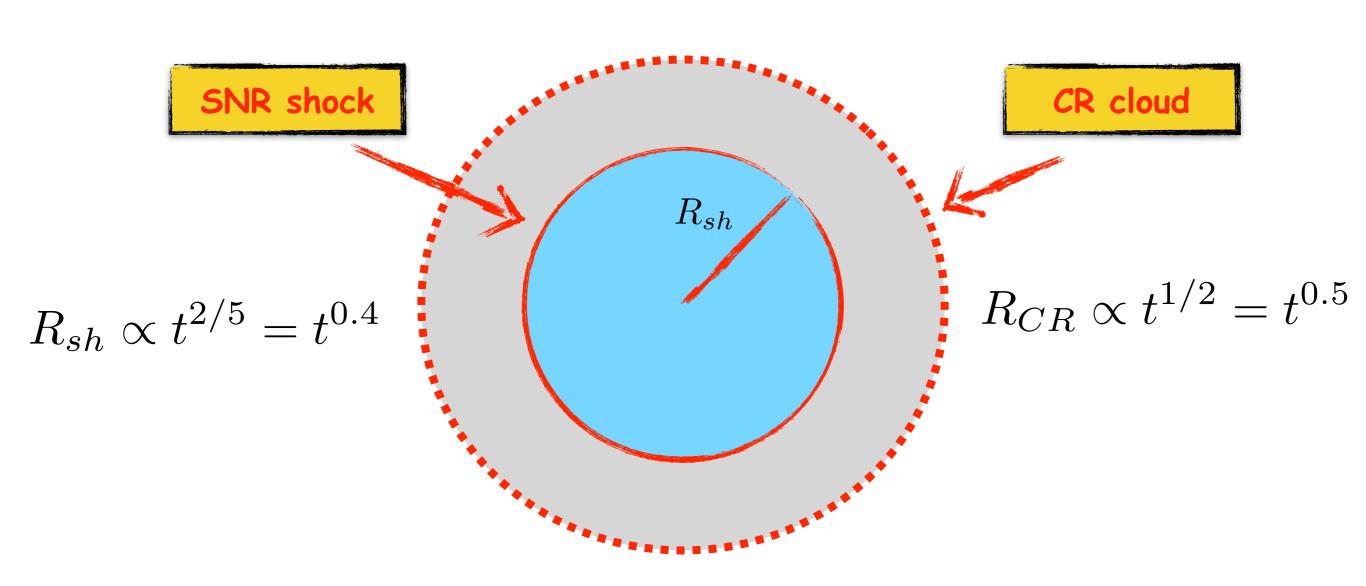
$$u_{sh} = \frac{2}{5} \frac{R_{sh}}{t} \propto t^{-3/5}$$

# How do cosmic rays escape from their sources?

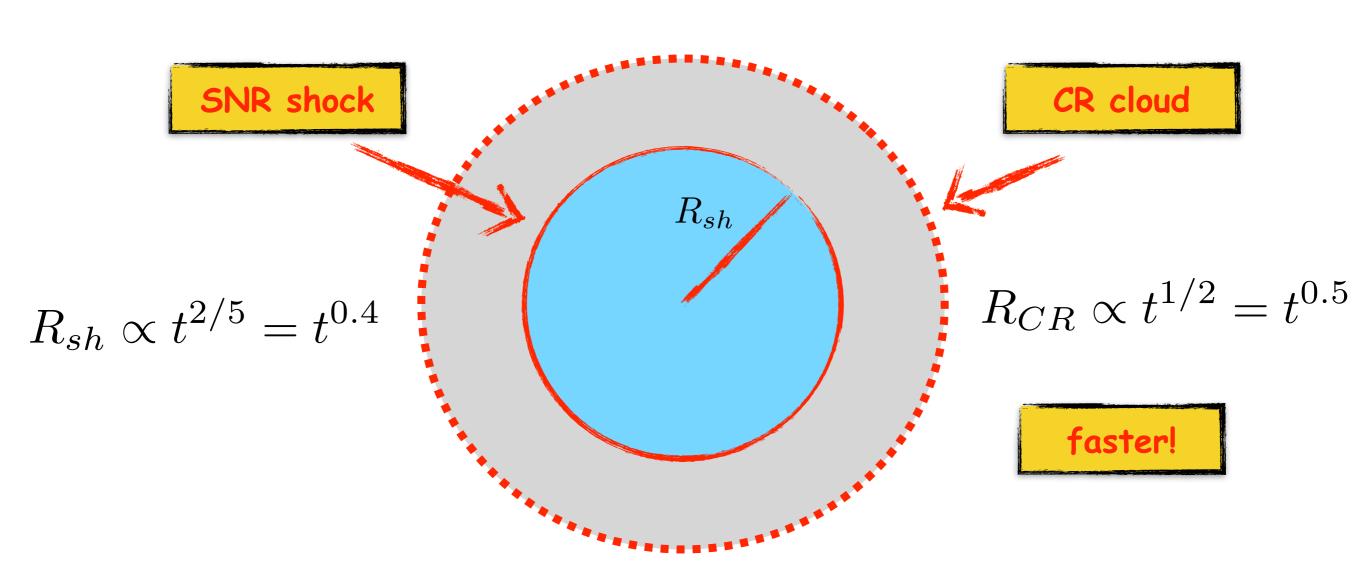




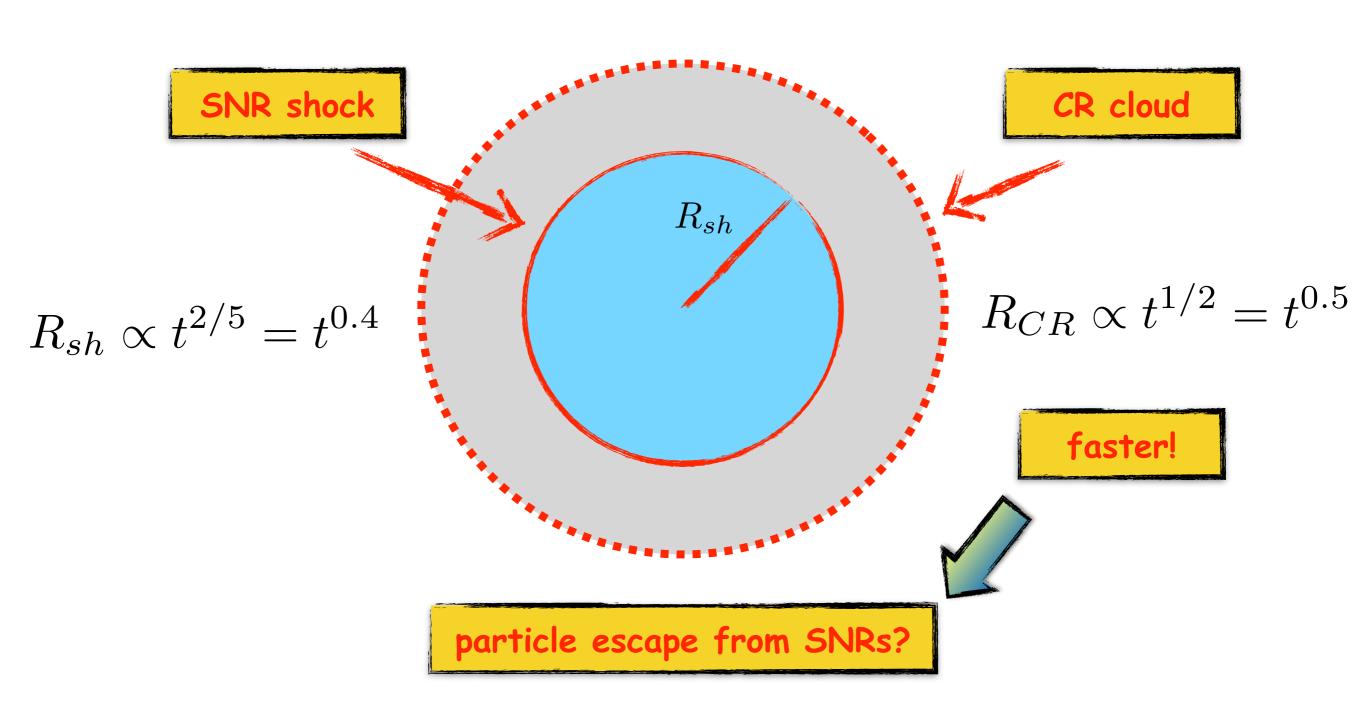




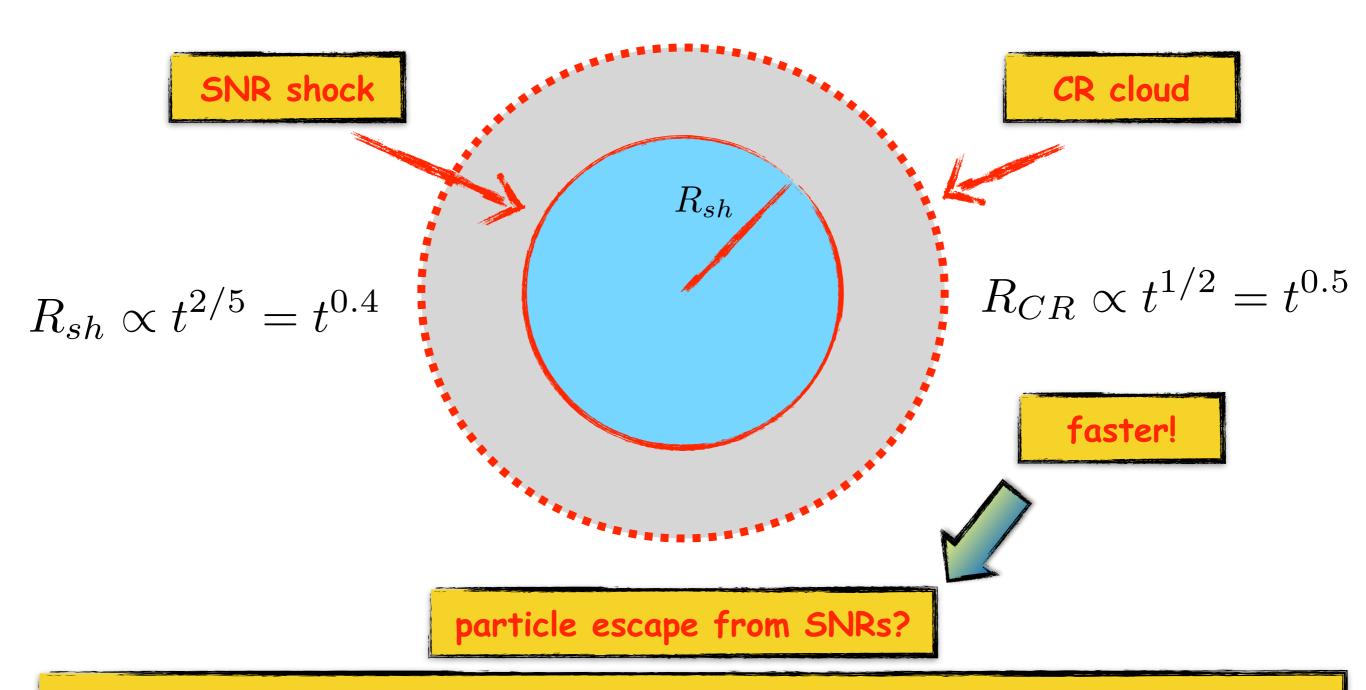
# SNR shocks are spherical -> CR escape



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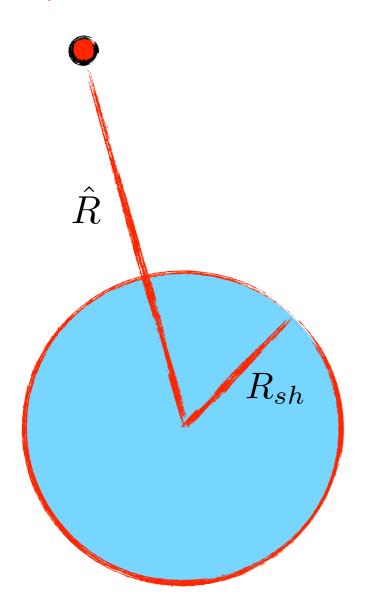
## SNR shocks are spherical -> CR escape



diffusion is faster for larger energies —> high energy particles escape first?

return probability to the shock for a particle located upstream

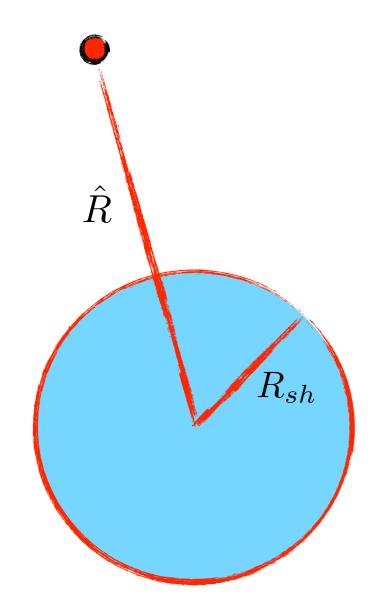
CR particle



for simplicity let's take the shock to be at rest

return probability to the shock for a particle located upstream

CR particle



for simplicity let's take the shock to be at rest

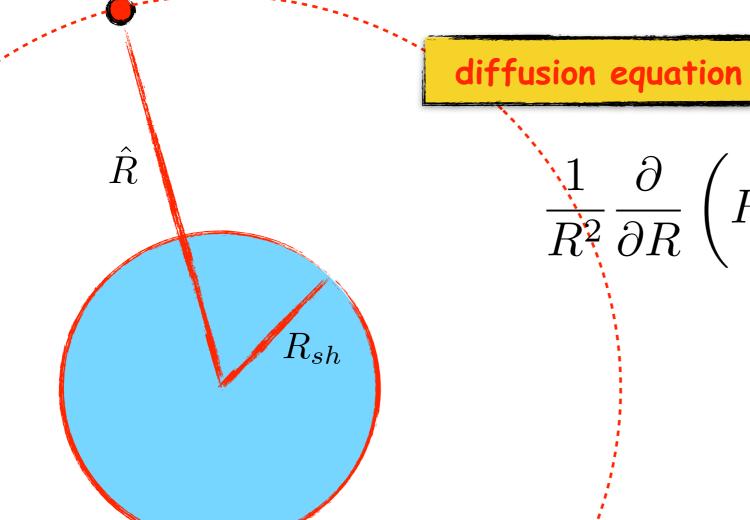
diffusion equation

$$\frac{1}{R^2} \frac{\partial}{\partial R} \left( R^2 D \frac{\partial f}{\partial R} \right) = \delta(R - \hat{R})$$

return probability to the shock for a particle located upstream

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fictitious source

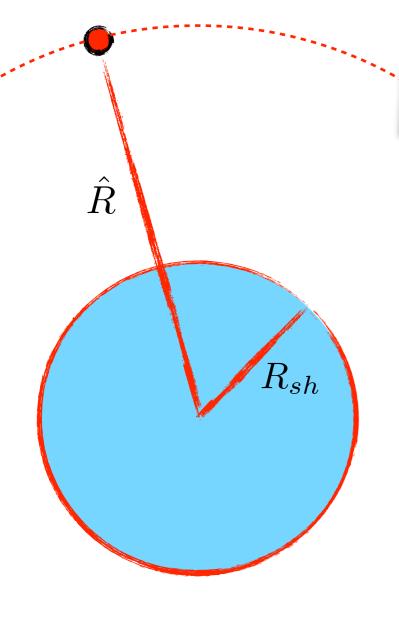
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**Drury 2011** 

return probability to the shock for a particle located upstream

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diffusion equation

 $\frac{1}{R^2} \frac{\partial}{\partial R} \left( R^2 D \frac{\partial f}{\partial R} \right) = \delta(R - \hat{R})$ 

boundary conditions

$$\lim_{R \to \infty} f = 0$$

$$f(R_{sh}) = 0$$

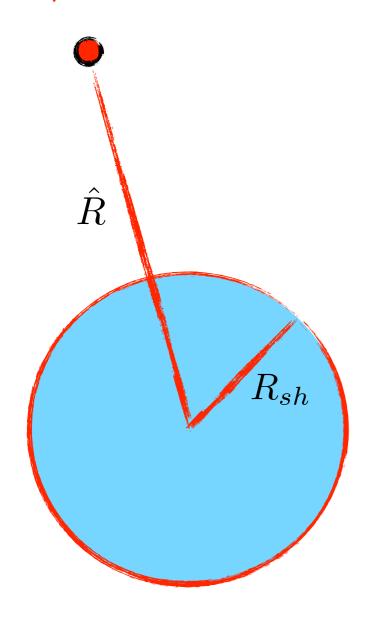
we treat the shock as an absorbing boundary

fictitious source

**Drury 2011** 

return probability to the shock for a particle located upstream

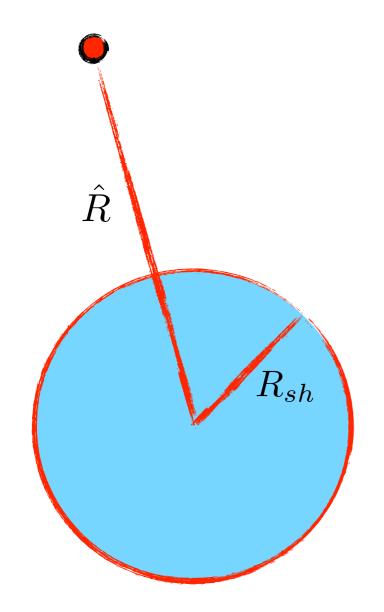
CR particle



let's solve the equation for  $R \neq \hat{R}$ 

return probability to the shock for a particle located upstream

CR particle



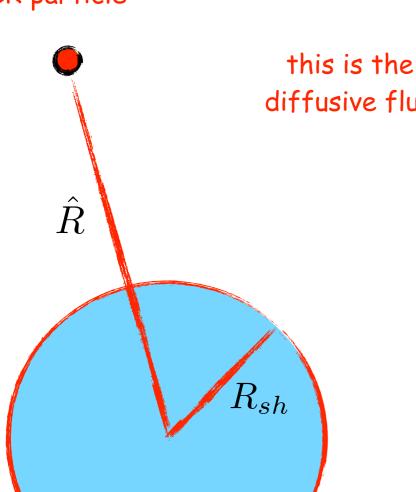
let's solve the equation for  $R 
eq \hat{R}$ 

$$R^{2}D\frac{\mathrm{d}f}{\mathrm{d}R} = \phi \to f = -\frac{\phi}{D}\left(\frac{1}{R} + a\right)$$

return probability to the shock for a particle located upstream



let's solve the equation for  $R 
eq \hat{R}$ 



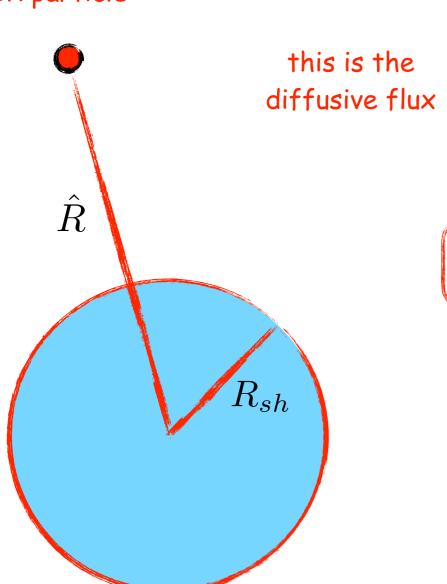
diffusive flux
$$R^2 D \frac{\mathrm{d}f}{\mathrm{d}R} = \phi \to f = -\frac{\phi}{D} \left( \frac{1}{R} + a \right)$$

this is the diffusive flux

return probability to the shock for a particle located upstream

CR particle

let's solve the equation for  $R \neq \hat{R}$ 



$$R^{2}D\frac{\mathrm{d}f}{\mathrm{d}R} = \phi \to f = -\frac{\phi}{D}\left(\frac{1}{R} + a\right)$$

$$R_{sh} < R < \hat{R}$$

this is the diffusive flux

$$f(R_{sh}) = 0 \to f = -\frac{\phi_{sh}}{D} \left( \frac{1}{R} - \frac{1}{R_{sh}} \right)$$

return probability to the shock for a particle located upstream

CR particle

 $\hat{R}$ 

this is the

let's solve the equation for  $R \neq \hat{R}$ 

diffusive flux
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this is the diffusive flux

$$f(R_{sh}) = 0 \to f = -\frac{\phi_{sh}}{D} \left( \frac{1}{R} - \frac{1}{R_{sh}} \right)$$

$$R > \hat{R}$$

, this is negative

$$f(R \to \infty) = 0 \to f = -\frac{\phi_{\infty}}{D} \frac{1}{R}$$

return probability to the shock for a particle located upstream

CR particle

this is the diffusive flux

let's solve the equation for  $R \neq \hat{R}$ 

$$R^{2}D\frac{\mathrm{d}f}{\mathrm{d}R} = \phi \rightarrow f = -\frac{\phi}{D}\left(\frac{1}{R} + a\right)$$

$$R_{sh} < R < \hat{R}$$

this is the diffusive flux

$$f(R_{sh}) = 0 \to f = -\frac{\phi_{sh}}{D} \left( \frac{1}{R} - \frac{1}{R_{sh}} \right)$$

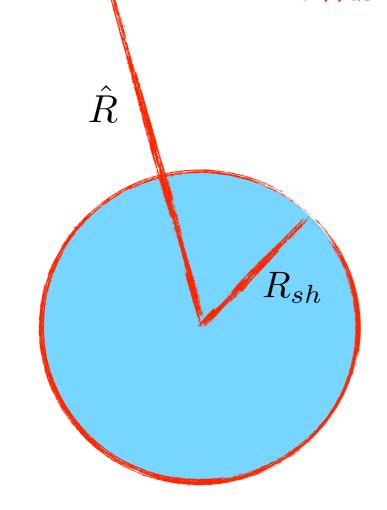
$$R > \hat{R}$$

, this is negative

constant

$$f(R \to \infty) = 0 \to f = +\frac{\phi_{\infty}}{D} \frac{1}{R}$$

we make it positive



return probability to the shock for a particle located upstream

the two solutions must be equal (continuity) in  $\,R=\hat{R}\,$ 

$$R_{sh} < R < \hat{R} \qquad f = -\frac{\phi_{sh}}{D} \left( \frac{1}{R} - \frac{1}{R_{sh}} \right) \qquad \qquad f = \frac{\phi_{\infty}}{D} \frac{1}{R} \quad (R > \hat{R})$$

return probability to the shock for a particle located upstream

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$$R_{sh} < R < \hat{R} \qquad f = -\frac{\phi_{sh}}{D} \left( \frac{1}{R} - \frac{1}{R_{sh}} \right) \qquad f = \frac{\phi_{\infty}}{D} \frac{1}{R} \quad R > \hat{R}$$

$$-\frac{\phi_{sh}}{D} \left( \frac{1}{\hat{R}} - \frac{1}{R_{sh}} \right) = \frac{\phi_{\infty}}{D} \frac{1}{\hat{R}}$$

return probability to the shock for a particle located upstream

the two solutions must be equal (continuity) in  $R=\hat{R}$ 

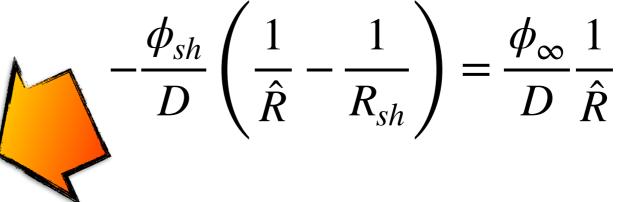
$$R_{sh} < R < \hat{R} \qquad f = -\frac{\phi_{sh}}{D} \left( \frac{1}{R} - \frac{1}{R_{sh}} \right)$$

$$f = \frac{\phi_{\infty}}{D} \frac{1}{R} \quad \left( R > \hat{R} \right)$$





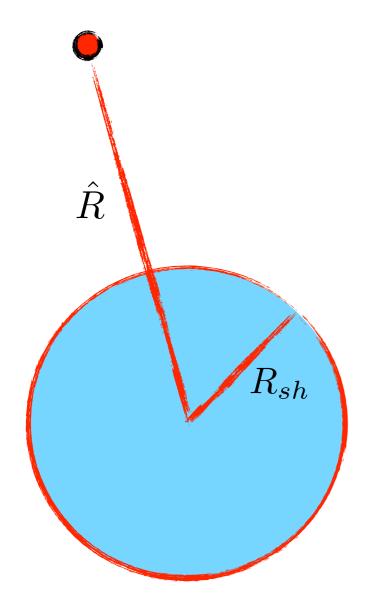
$$\phi_{\infty} = \phi_{sh} \left( \frac{\hat{R}}{R_{sh}} - 1 \right)$$



$$=\frac{\phi_{\infty}}{D}\frac{1}{\hat{R}}$$

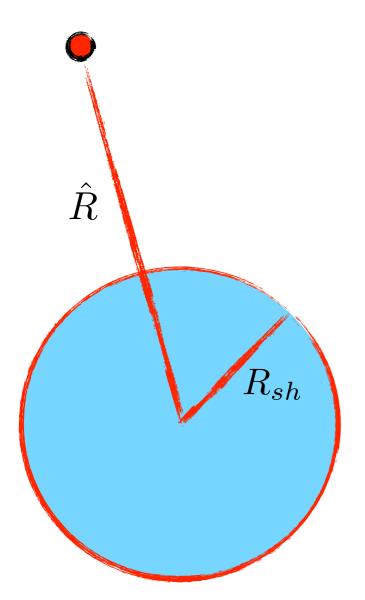
return probability to the shock for a particle located upstream





$$\phi_{\infty} = \phi_{sh} \left( \frac{\hat{R}}{R_{sh}} - 1 \right)$$

return probability to the shock for a particle located upstream



$$\phi_{\infty} = \phi_{sh} \left( \frac{\hat{R}}{R_{sh}} - 1 \right)$$

$$P_{ret} = \frac{\phi_{sh}}{\phi_{sh} + \phi_{\infty}} = \frac{R_{sh}}{\hat{R}}$$

$$P_{esc} = 1 - \frac{R_{sh}}{\hat{R}}$$

DSA theory —> we computed the return probability for a plane shock

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plane shock (DSA)

$$P_{ret}^{DSA} = 1 - \frac{u_{sh}}{c}$$

$$P_{esc}^{DSA} = \frac{u_{sh}}{c}$$

DSA theory  $\rightarrow$  we computed the return probability for a plane shock

plane shock (DSA)

$$P_{ret}^{DSA} = 1 - \frac{u_{sh}}{c}$$
$$P_{esc}^{DSA} = \frac{u_{sh}}{c}$$

this is the probability (per cycle)
that the particle stops being
accelerated because it escapes
DOWNSTREAM (inside the SNR)

DSA theory —> we computed the return probability for a plane shock

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spherical shock (geometry)

$$P_{ret}^{geom} = \frac{R_{sh}}{\hat{R}}$$

$$P_{esc}^{geom} = 1 - \frac{R_{sh}}{\hat{R}}$$

DSA theory —> we computed the return probability for a plane shock

plane shock (DSA)

$$P_{ret}^{DSA} = 1 - \frac{u_{sh}}{c}$$

$$P_{esc}^{DSA} = \frac{u_{sh}}{c}$$

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spherical shock (geometry)

$$P_{ret}^{geom} = \frac{R_{sh}}{\hat{R}}$$

$$P_{esc}^{geom} = 1 - \frac{R_{sh}}{\hat{R}}$$

this is the probability that the particle stops being accelerated because it escapes UPSTREAM (instead of going back to the shock)

DSA theory —> we computed the return probability for a plane shock

plane shock (DSA)

$$P_{ret}^{DSA} = 1 - \frac{u_{sh}}{c}$$

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spherical shock (geometry)

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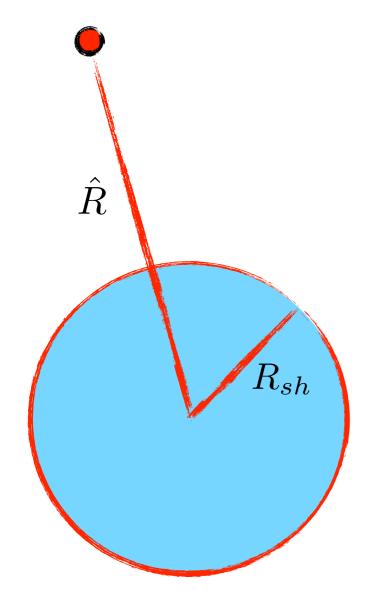
$$P_{esc}^{geom} = 1 - \frac{R_{sh}}{\hat{R}}$$

this is the probability that the particle stops being accelerated because it escapes UPSTREAM (instead of going back to the shock)

$$P_{esc}^{geom} \approx P_{esc}^{DSA} \longrightarrow \frac{\hat{R} - R_{sh}}{\hat{R}} = \frac{u_{sh}}{c} \ll 1$$

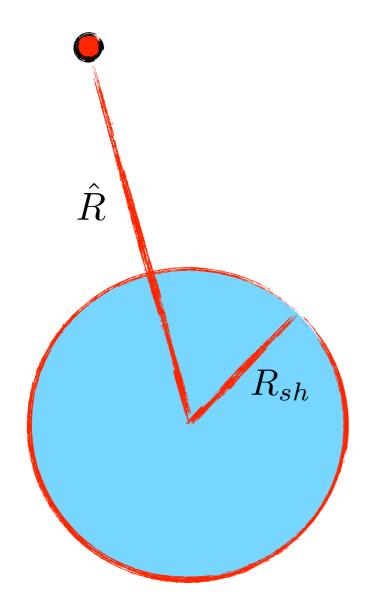
consequences of what said so far...

$$1 - \frac{R_{sh}}{\hat{R}} = \frac{u_{sh}}{c} \ll 1$$



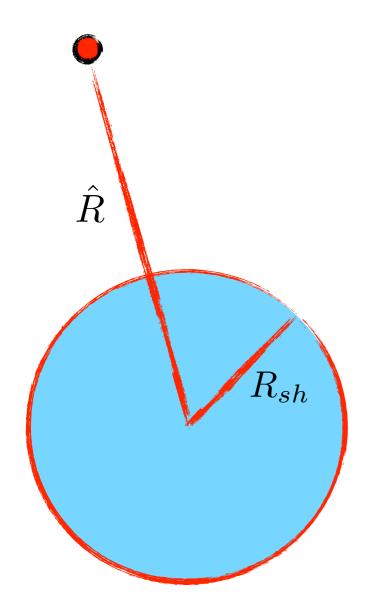
consequences of what said so far...

$$1 - \frac{R_{sh}}{\hat{R}} = \frac{u_{sh}}{c} \ll 1 \longrightarrow \frac{\hat{R}}{R_{sh}} = \left(1 - \frac{u_{sh}}{c}\right)^{-1}$$



consequences of what said so far...

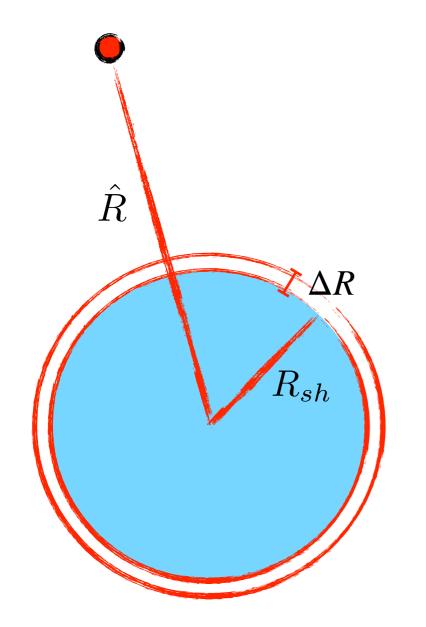
$$1 - \frac{R_{sh}}{\hat{R}} = \frac{u_{sh}}{c} \ll 1 \longrightarrow \frac{\hat{R}}{R_{sh}} = \left(1 - \frac{u_{sh}}{c}\right)^{-1} \approx 1 + \frac{u_{sh}}{c} \sim 1 + 0.03 \left(\frac{u_{sh}}{10^4 \text{ km/s}}\right)^{-1}$$



consequences of what said so far...

this is very small

$$1 - \frac{R_{sh}}{\hat{R}} = \frac{u_{sh}}{c} \ll 1 \longrightarrow \frac{\hat{R}}{R_{sh}} = \left(1 - \frac{u_{sh}}{c}\right)^{-1} \approx 1 + \frac{u_{sh}}{c} \sim 1 + 0.03 \left(\frac{u_{sh}}{10^4 \text{ km/s}}\right)$$

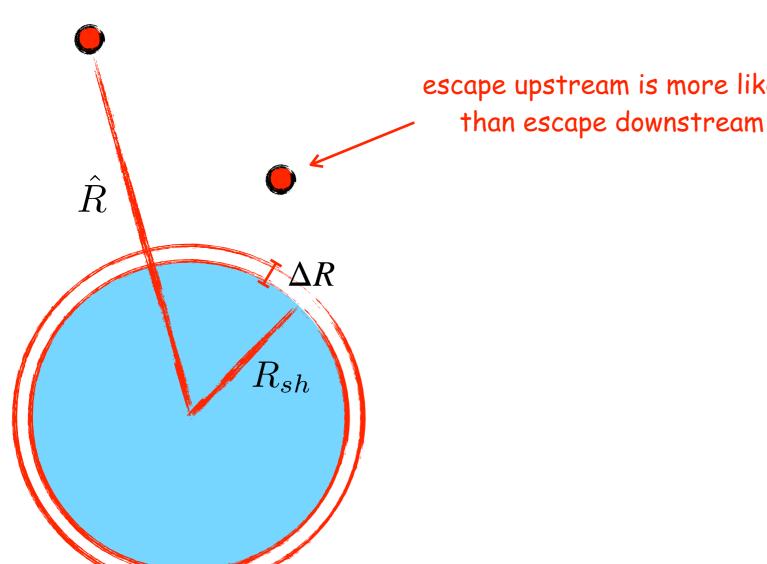


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CR particle



escape upstream is more likely



this is very small

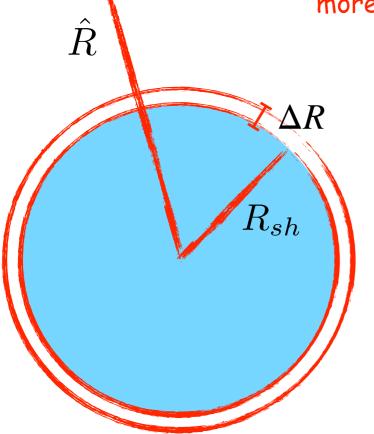
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CR particle



more accurate estimate  $\longrightarrow$ 

$$\frac{\Delta R}{R_{sh}} = \frac{\hat{R} - R_{sh}}{R_{sh}} \approx 5 - 10\%$$





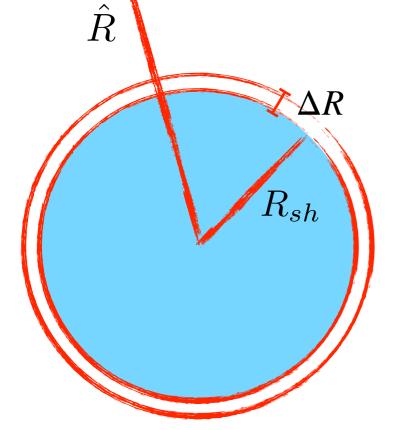
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CR particle



more accurate estimate 
$$\longrightarrow \frac{\Delta R}{R_{sh}} = \frac{\hat{R} - R_{sh}}{R_{sh}} \approx 5 - 10\,\%$$



[2] in the Hillas criterion we should not use Rsh, but rather  $\Delta R$ 

-> E<sub>max</sub> goes down by ~1 order of magnitude

#### Plane (infinite) versus spherical shocks

plane (infinite)

spherical (finite)

particles can escape DOWNSTREAM ONLY —> escape BOTH down and up-stream

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plane (infinite)

spherical (finite)

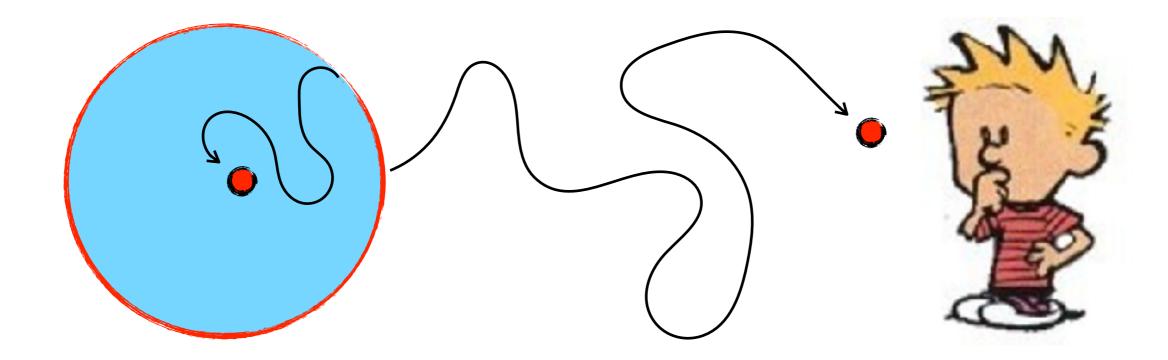
- particles can escape DOWNSTREAM ONLY —> escape BOTH down and up-stream
- mate infinite time —> arbitrarily large energy —> escape upstream limits  $E_{max}$ !

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plane (infinite)

spherical (finite)

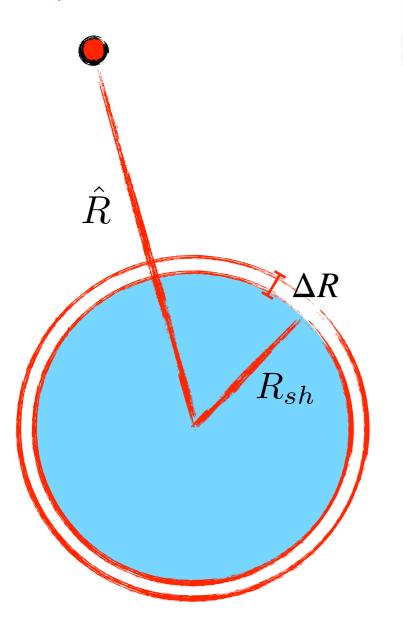
- particles can escape DOWNSTREAM ONLY —> escape BOTH down and up-stream
- $\blacksquare$  infinite time —> arbitrarily large energy —> escape upstream limits  $E_{max}$ !
- an observer at Earth sees —> NOTHING! —> what escapes upstream



#### Which E<sub>max</sub> at SNR shocks?

three possibilities:

CR particle



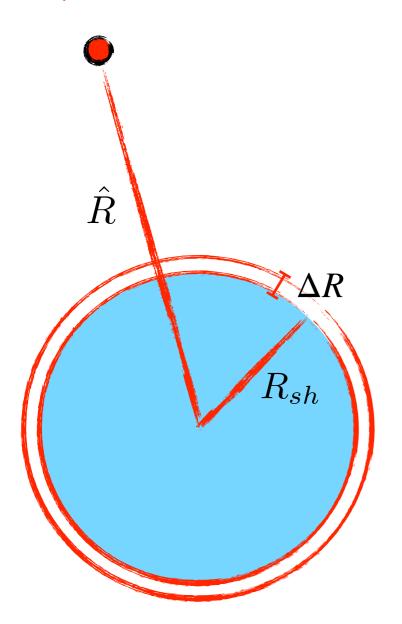
[1] age limited ->

$$\tau_{acc}(E) = \tau_{age}$$

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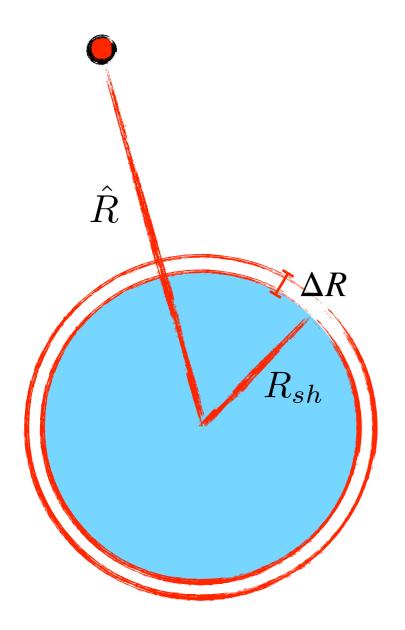


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$$l_d(E) = \Delta R$$

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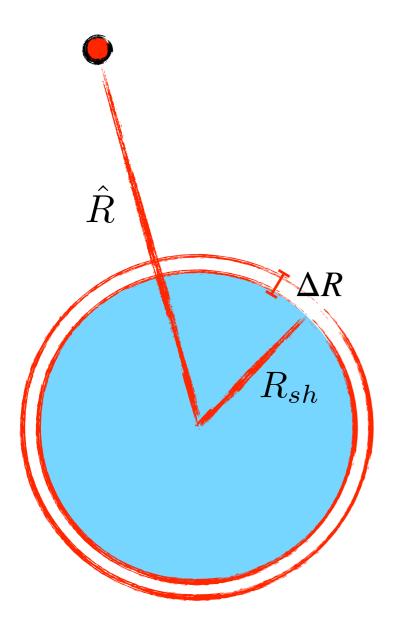
[1] age limited —>

$$\tau_{acc}(E) = \tau_{age}$$
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$$l_d(E) = \Delta R$$

$$\tau_{acc}(E) = \tau_{loss}$$

three possibilities:

CR particle

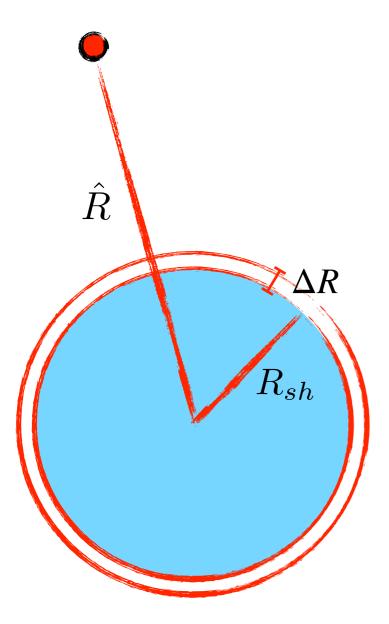


$$\tau_{acc}(E) = \tau_{age} \qquad \text{time}$$
 
$$l_d(E) = \Delta R \qquad \text{space}$$

$$au_{acc}(E) = au_{loss}$$
 energy

three possibilities:

CR particle



[2] loss limited 
$$\rightarrow$$
  $\tau_{acc}(E) = \tau_{loss}$  energy

$$au_{acc}(E)$$

 $\tau_{acc}(E) = \tau_{age}$ 

 $l_d(E) = \Delta R$ 

time

diffusion length

ambient

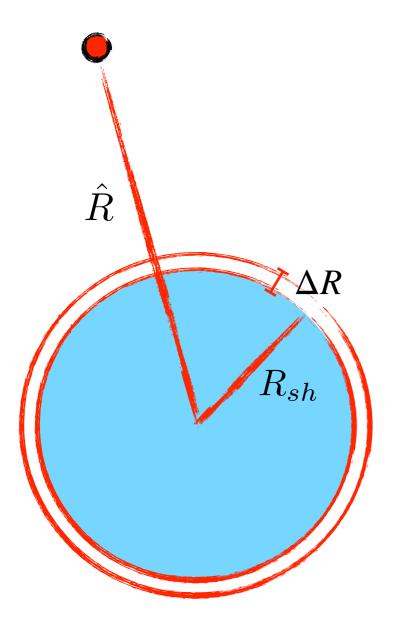
inelastic proton-proton interactions

$$t_{pp} = (n_{gas} \sigma_{pp} c k)^{-1} \approx 60 \left(\frac{n}{\text{cm}^{-3}}\right)^{-1} \text{Myr}$$

$$4 \times 10^{-26} \text{ cm}^2 \qquad 0.45 \text{ (inelasticity)}$$

three possibilities:





ted 
$$\rightarrow$$
  $\tau_{acc}(E) = \tau_{age}$ 

diffusion length

$$l_d(E) = \Delta R$$

time

$$au_{acc}(E) = au_{loss}$$
 energy

$$p + p \xrightarrow{\text{medium}} p + p + p + \pi^0$$

ambient

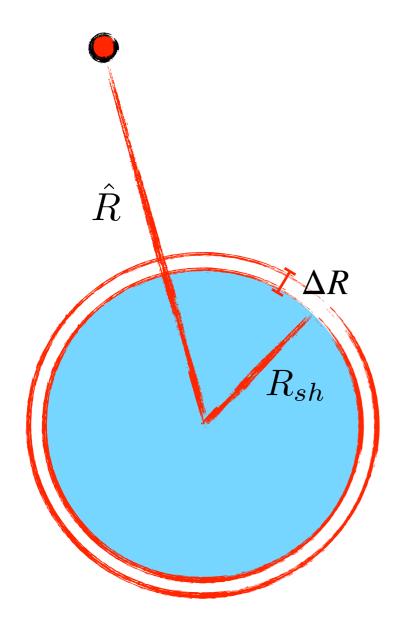
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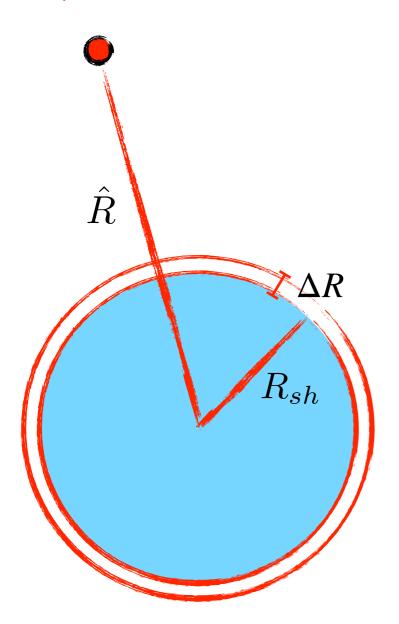
#### CR particle





$$\tau_{acc}(E) = \tau_{age}$$

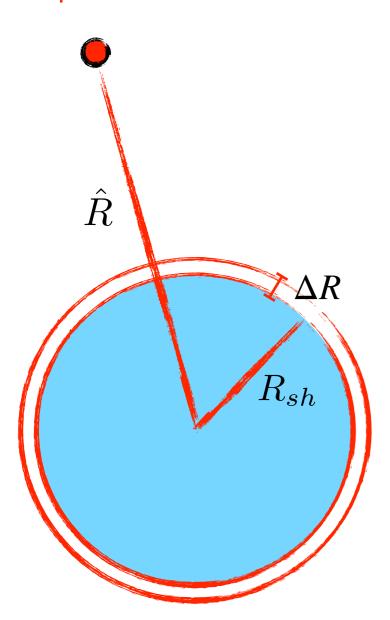
CR particle



$$\tau_{acc}(E) = \frac{1}{r_{acc}(E)} = 20 \frac{D(E)}{u_{sh}^2} = \frac{20R_L(E)c}{3u_{sh}^2}$$

#### [1] age limited ->

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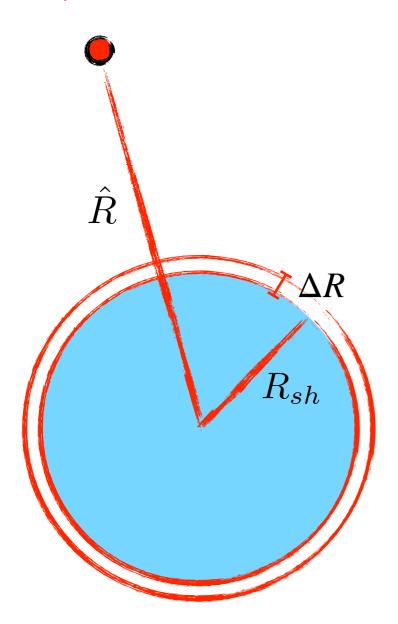
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$$R_L(E_{max}) = \frac{3}{20} \left(\frac{u_{sh}}{c}\right) u_{sh} \tau_{age}$$

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CR particle



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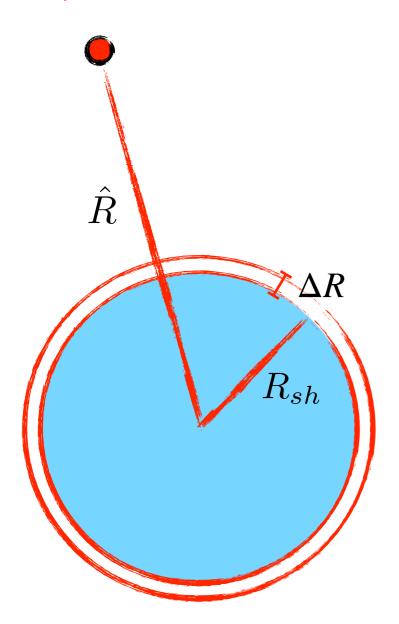
[2] size limited ->

$$l_d(E) = \Delta R$$

[1] age limited  $\rightarrow$   $\tau_{acc}(E) = \tau_{age}$ 

$$\tau_{acc}(E) = \tau_{age}$$

CR particle



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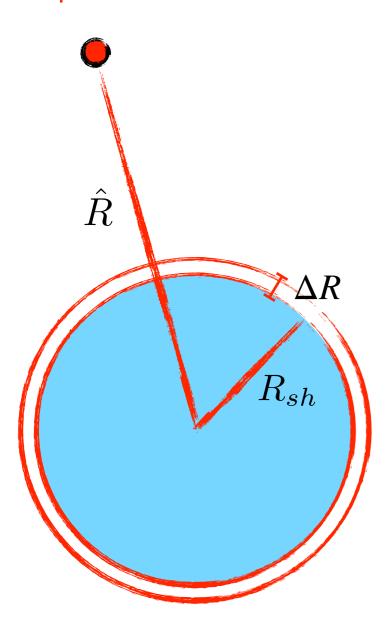
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[2] size limited ->

$$l_d(E) = \Delta R = \eta R_{sh}$$

~5%

$$l_d(E) = \frac{D(E)}{u_{sh}} = \frac{R_L(E)c}{3u_{sh}}$$

$$R_L(E_{max}) = 3\eta \left(\frac{u_{sh}}{c}\right) R_{sh}$$

[1] age limited

[2] size limited

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SNR evolution ->

$$R_{sh} \propto \tau_{age}^{\alpha} \longrightarrow u_{sh} = \alpha \frac{R_{sh}}{\tau_{age}}$$

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identical

Jir tudily co

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G

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identical

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SNR evolution ->

$$R_{sh} \propto \tau_{age}^{\alpha} \longrightarrow u_{sh} = \alpha \frac{R_{sh}}{\tau_{age}}$$

free expansion ->

$$\alpha = 1 \rightarrow R_L(E_{max}) \propto E_{max} \propto \tau_{age}$$

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$$R_L(E_{max}) = \frac{3}{20} \left(\frac{u_{sh}}{c}\right) u_{sh} \tau_{age}$$

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identical

virtually de dico

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6

SNR evolution ->

$$R_{sh} \propto au_{age}^{\alpha} \longrightarrow u_{sh} = \alpha \frac{R_{sh}}{ au_{age}}$$

free expansion ->

$$\alpha = 1 \rightarrow R_L(E_{max}) \propto E_{max} \propto \tau_{age}$$

Sedov-Taylor ->

$$\alpha = \frac{2}{5} \to R_L(E_{max}) \propto E_{max} \propto \tau_{age}^{-1/5}$$

$$R_L(E_{max}) = 3\eta \left(\frac{u_{sh}}{c}\right) R_{sh}$$

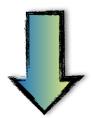
$$R_L(E_{max}) = 3\eta \left(\frac{u_{sh}}{c}\right) R_{sh}$$
  $R_L(E) = \frac{E(\text{eV})}{300 \ B(\text{G})} \text{ cm}$ 

$$E_{max} \approx 30 \left(\frac{\eta}{0.1}\right) \left(\frac{B}{3 \mu G}\right) \left(\frac{u_{sh}}{10^4 \text{ km/s}}\right) \left(\frac{R_{sh}}{\text{pc}}\right) \text{TeV}$$

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$$R_* = R_{sh}(\tau_{age}^*) \approx 2 \text{ pc}$$

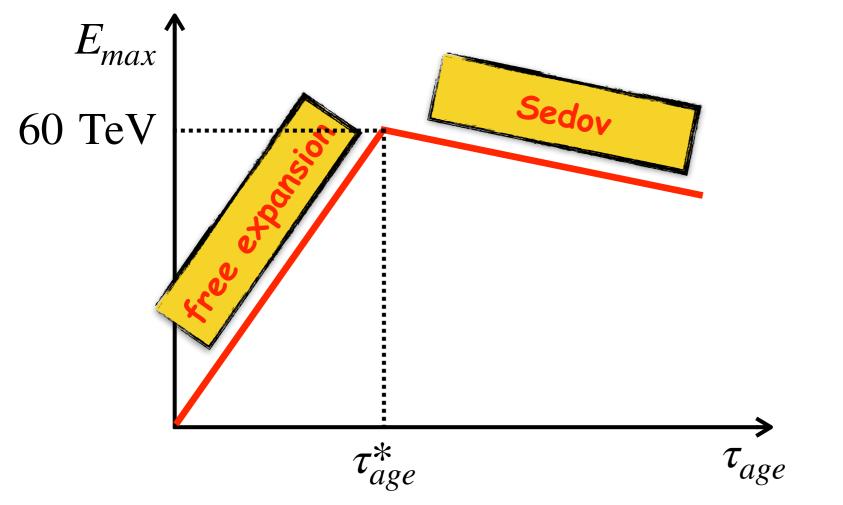


 $E_{max} \approx 60 \text{ TeV}$ 

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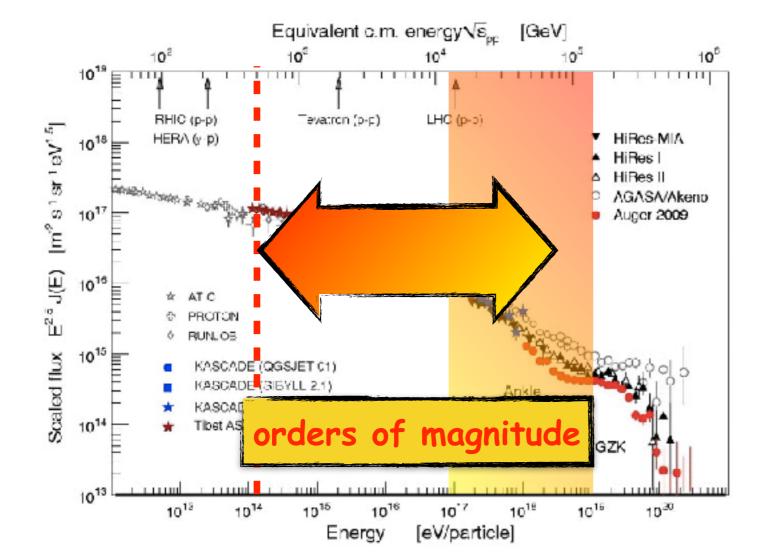


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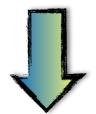
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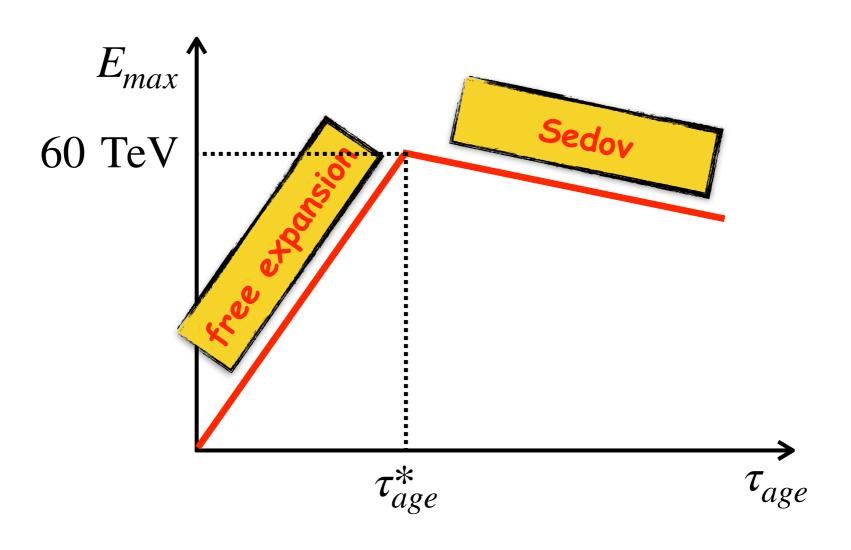
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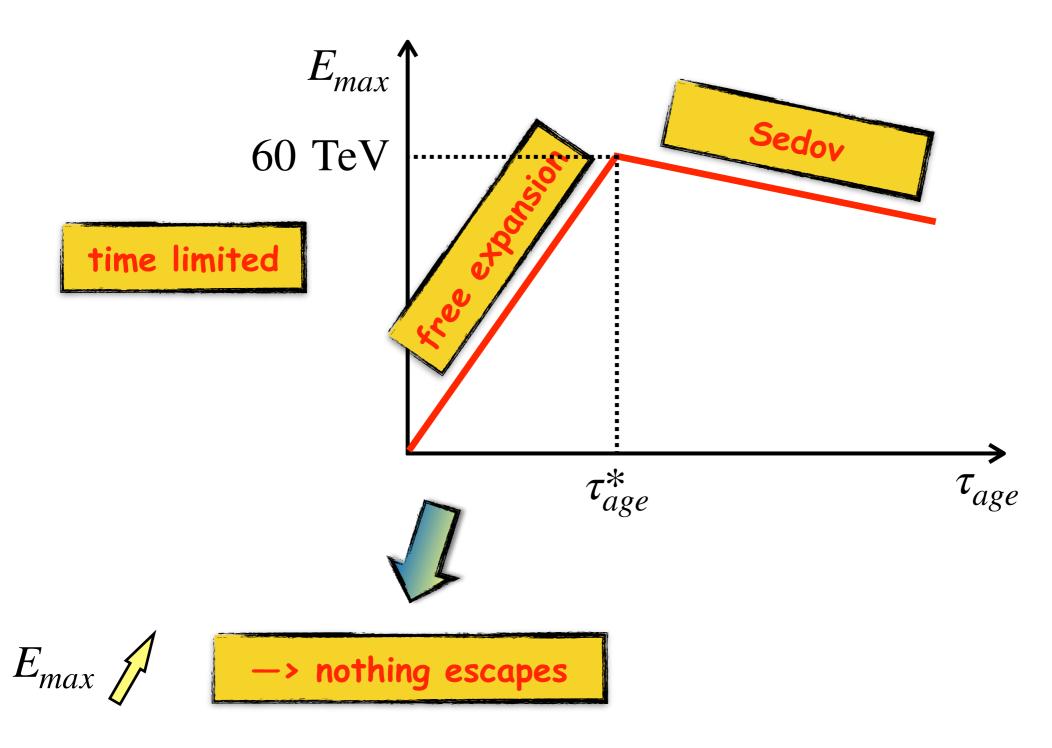


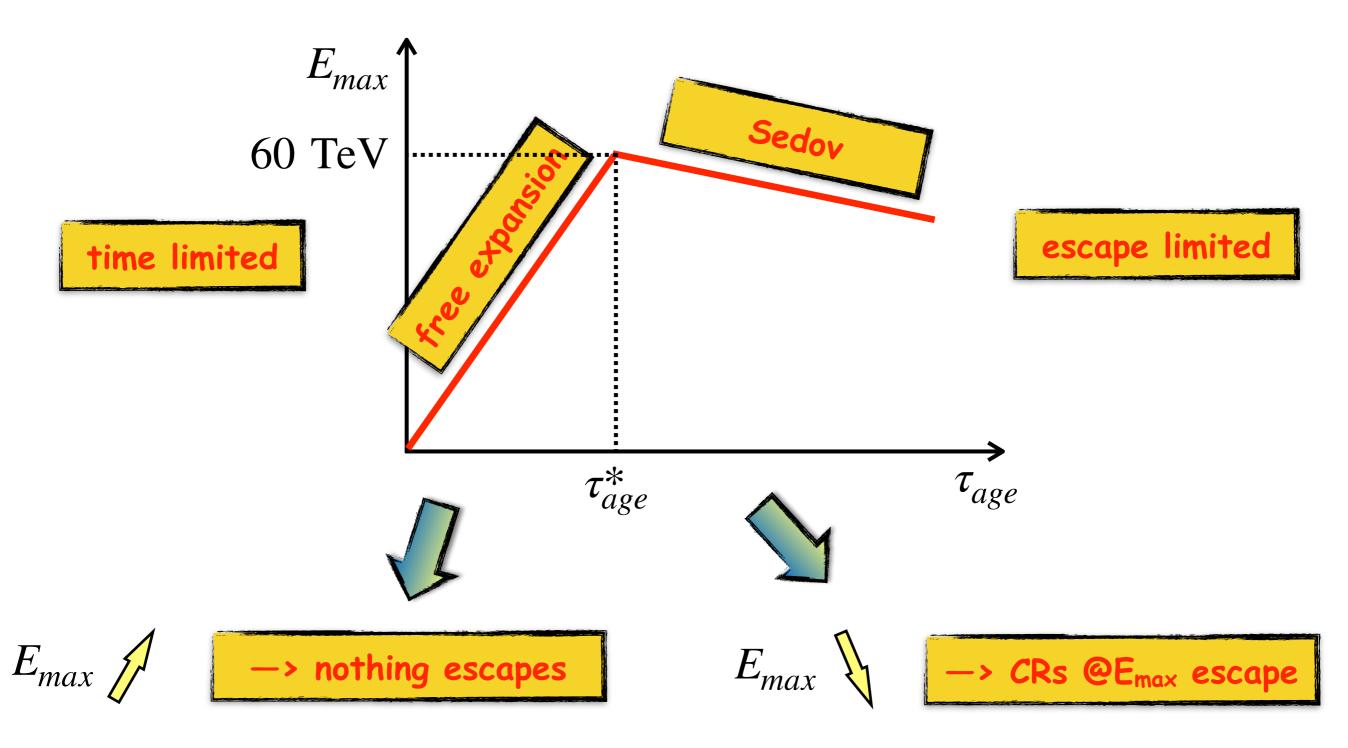
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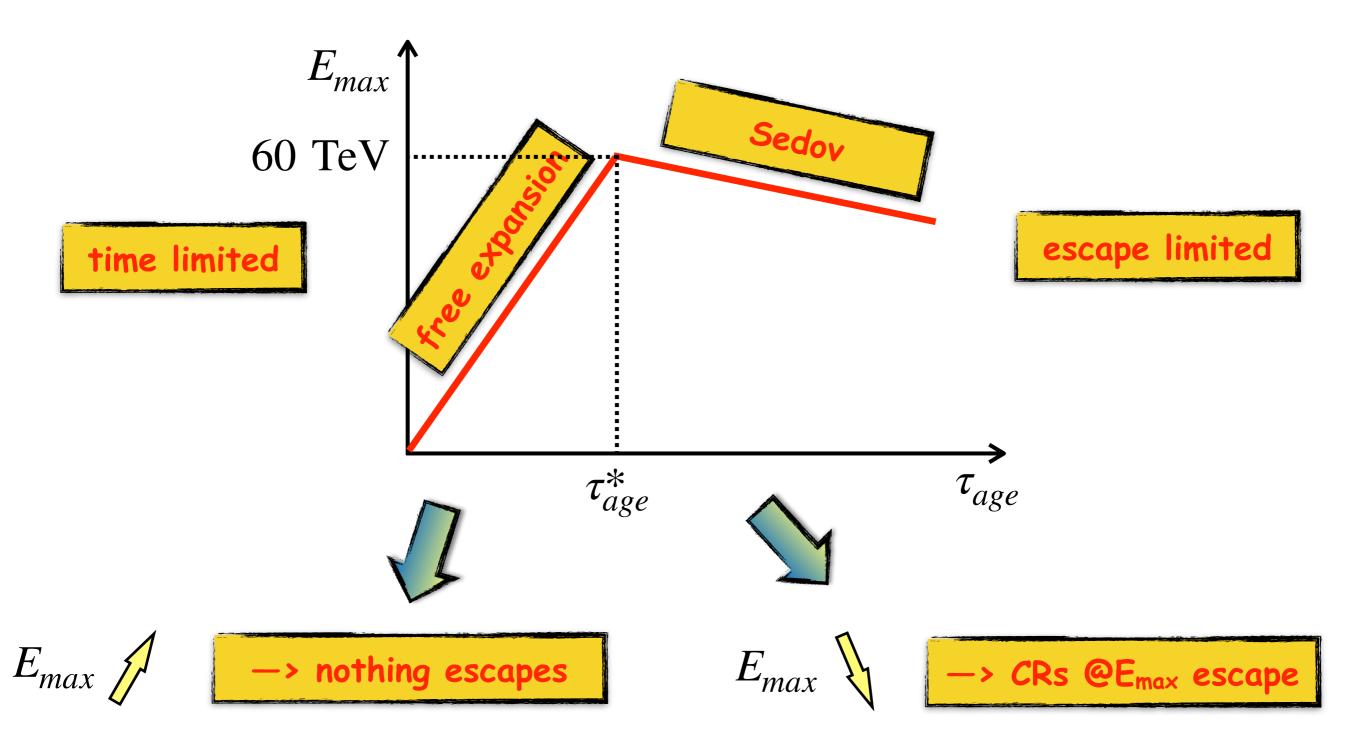


 $E_{max} \approx 60 \text{ TeV}$ 









real life: u<sub>sh</sub> not necessarily constant in free expansion, it may slowly decelerate —> few CR escape also during this phase

## Way outs?

$$E_{max} \approx 30 \left(\frac{\eta}{0.1}\right) \left(\frac{B}{3 \mu G}\right) \left(\frac{u_{sh}}{10^4 \text{ km/s}}\right) \left(\frac{R_{sh}}{\text{pc}}\right) \text{TeV}$$

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these are very well measured/constrained

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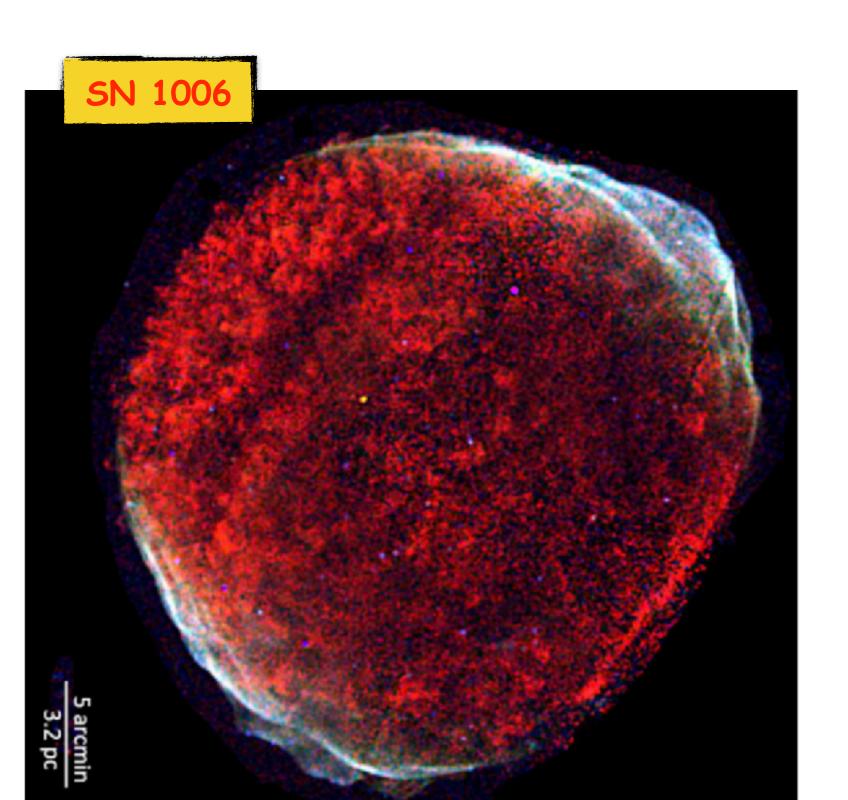
this is (was) not



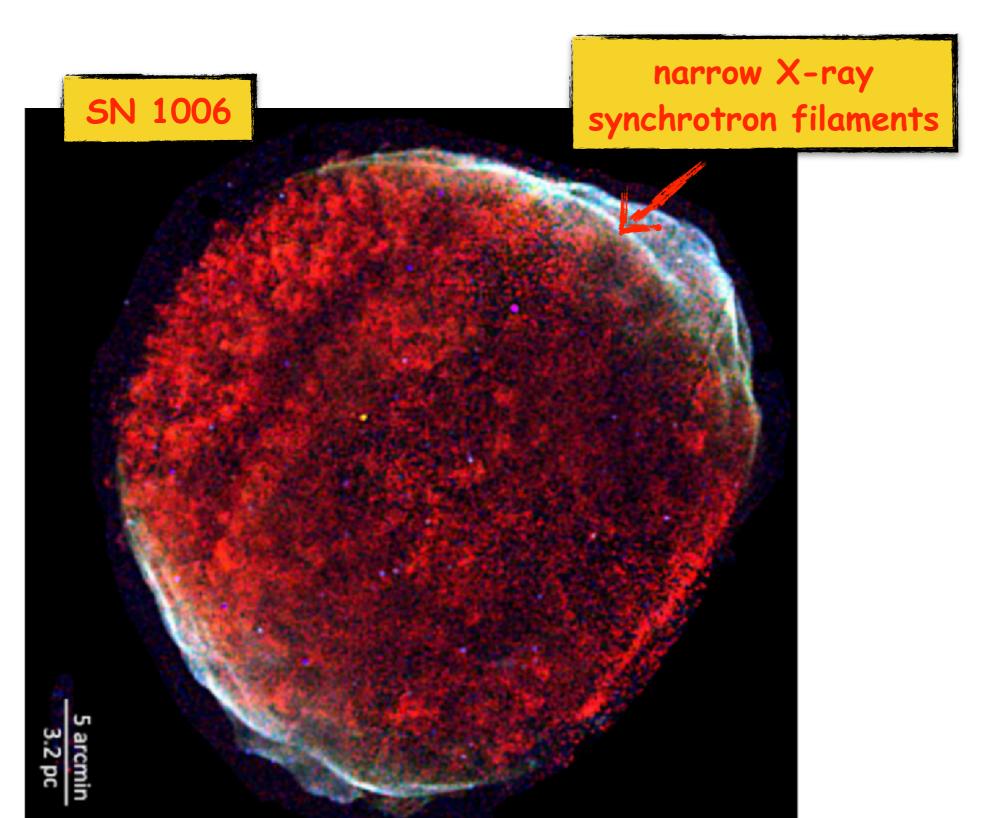


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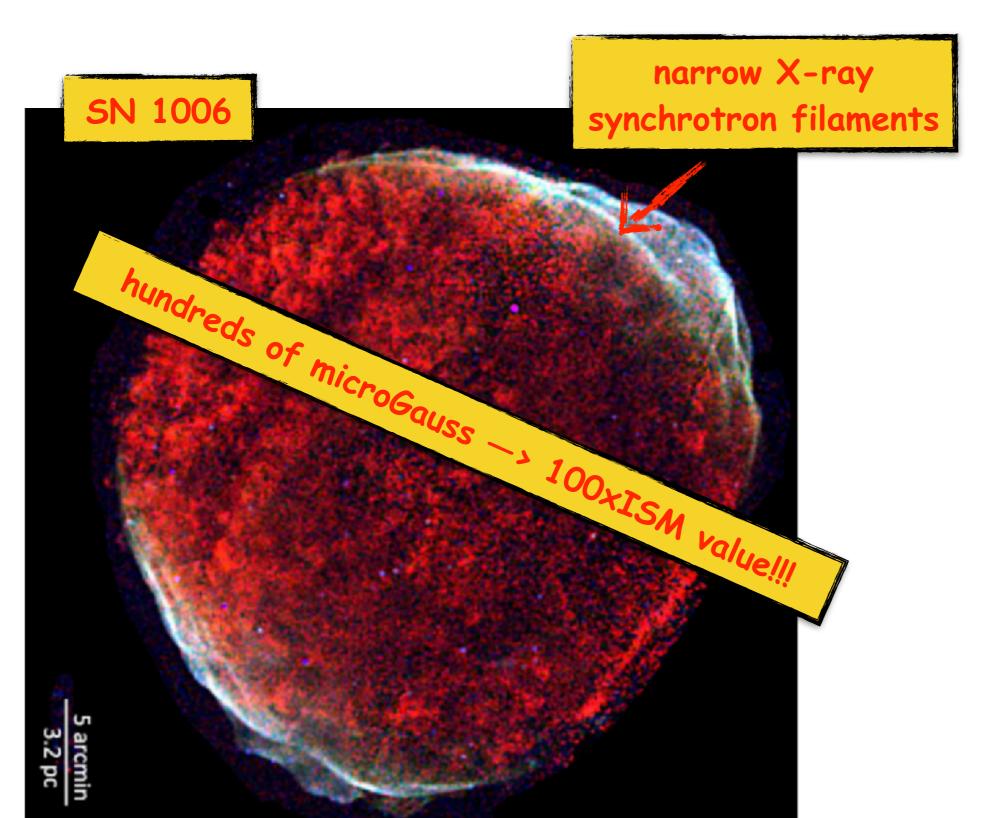
# Large B fields are observed! (~100xISM values)

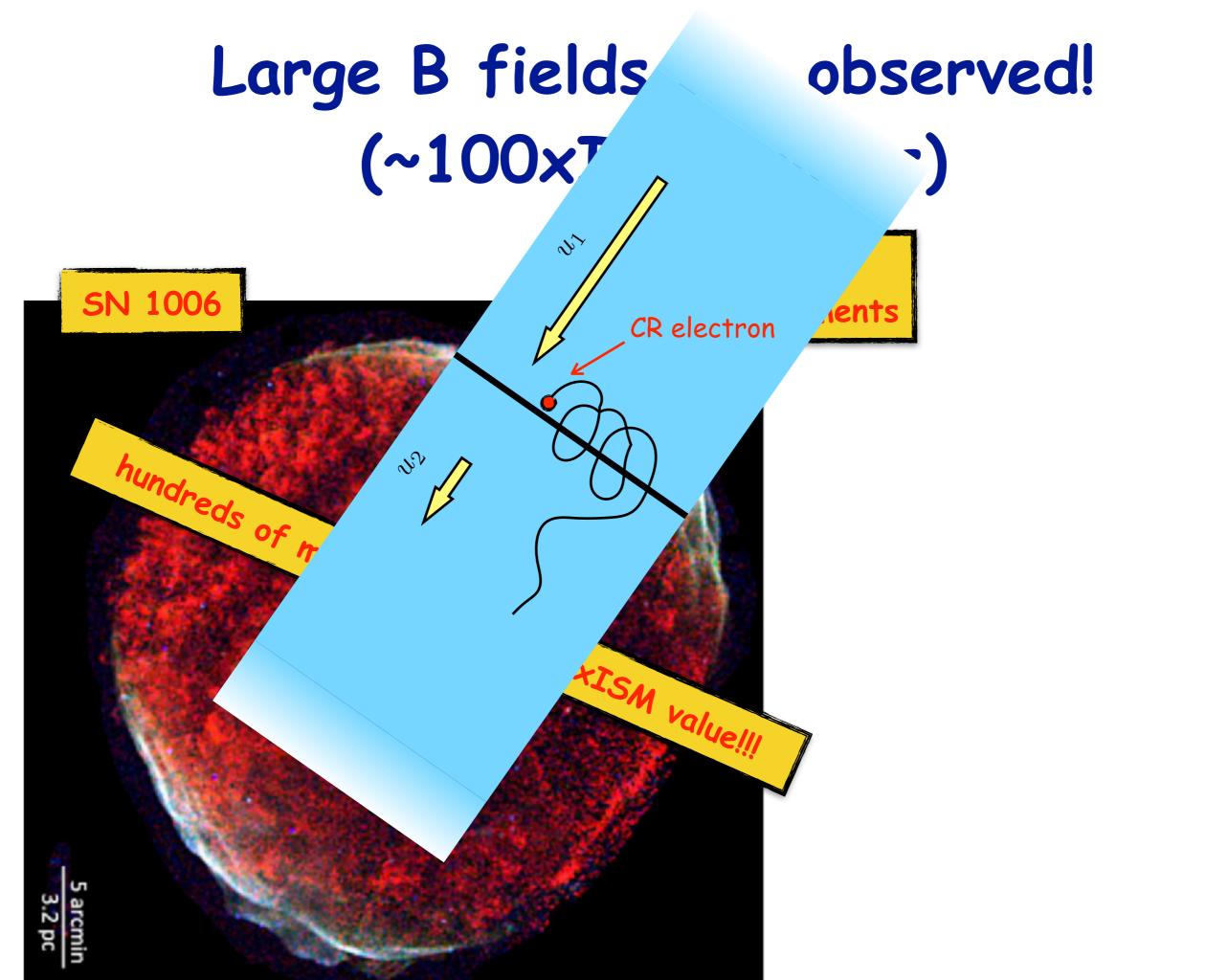


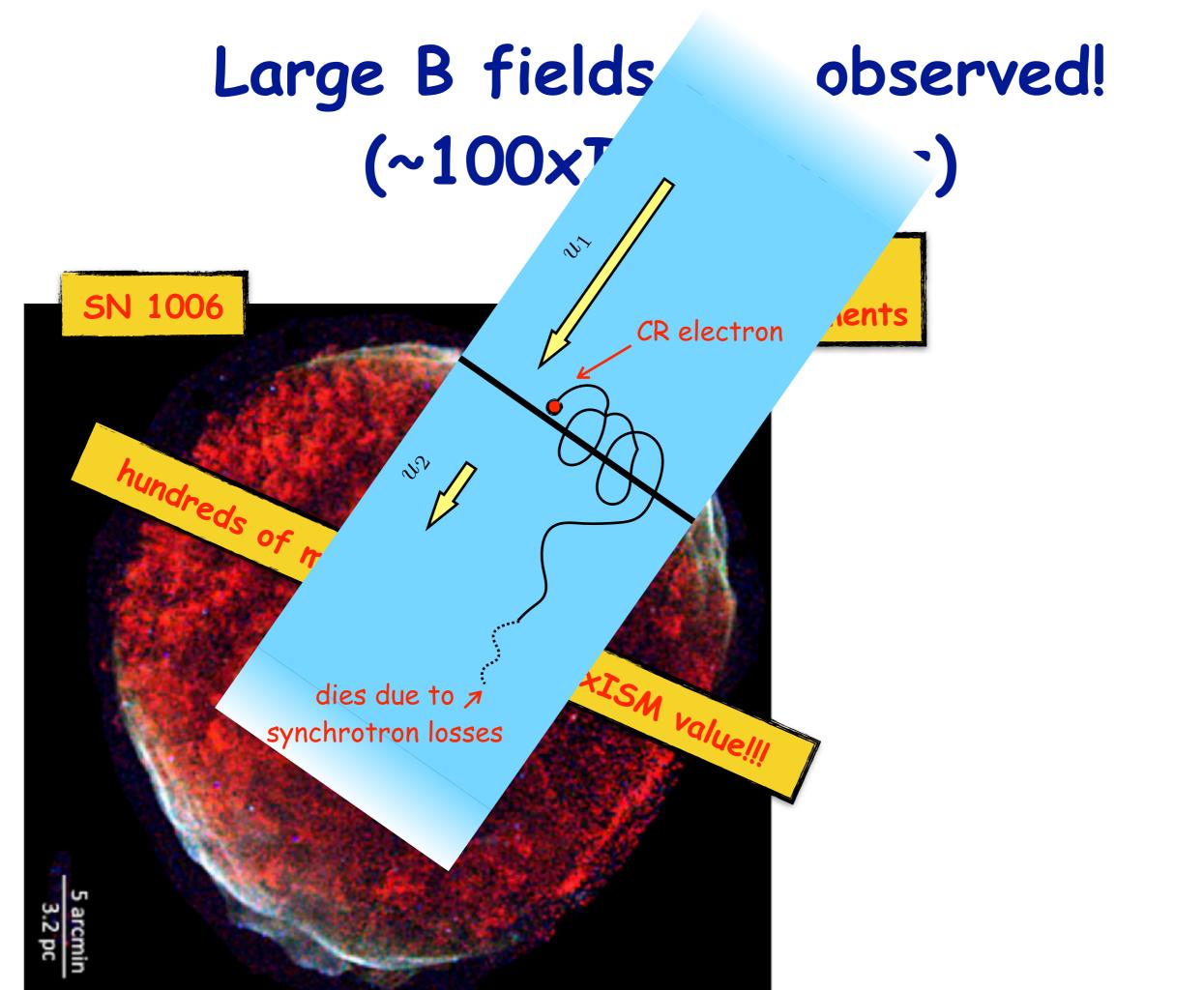
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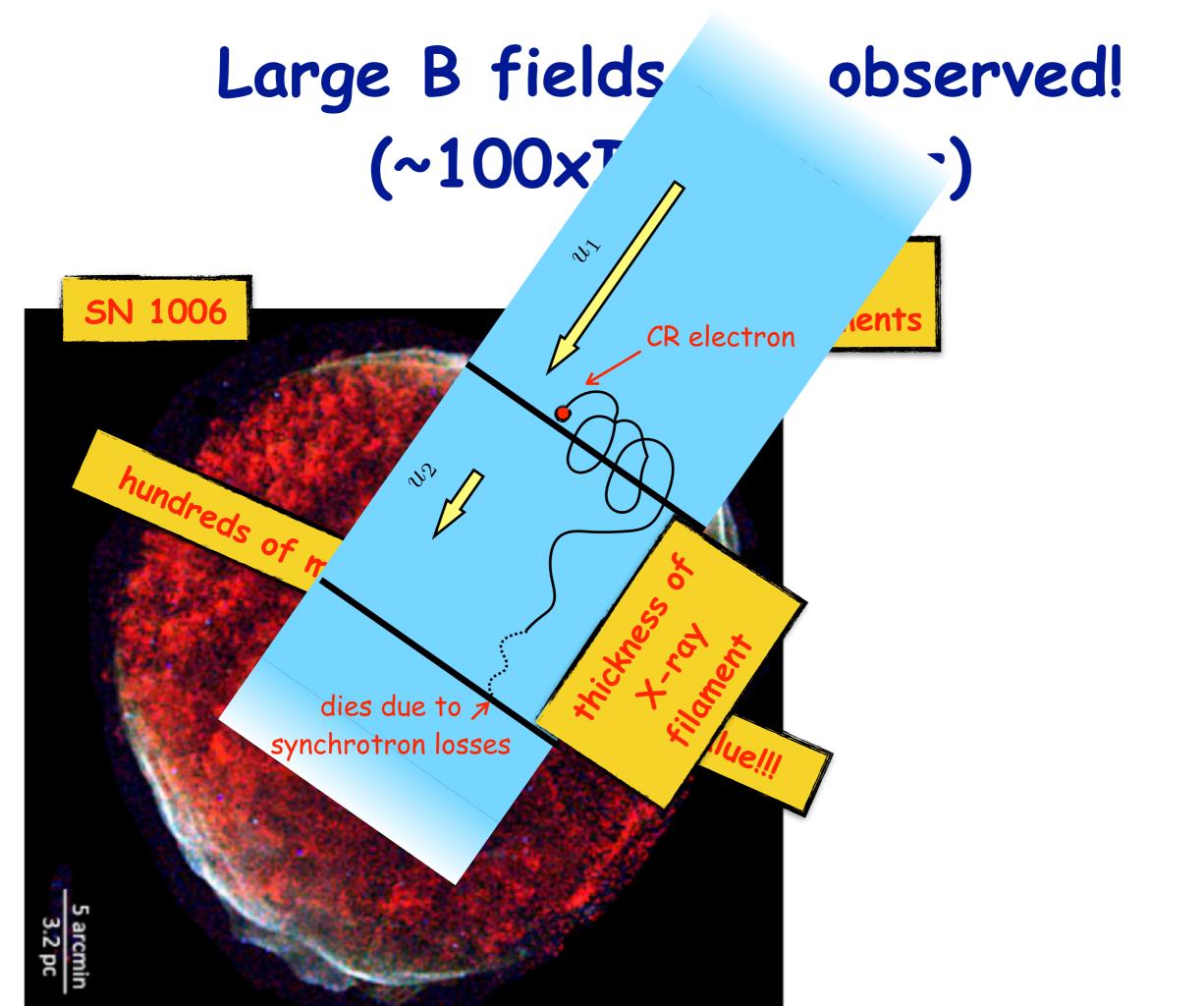


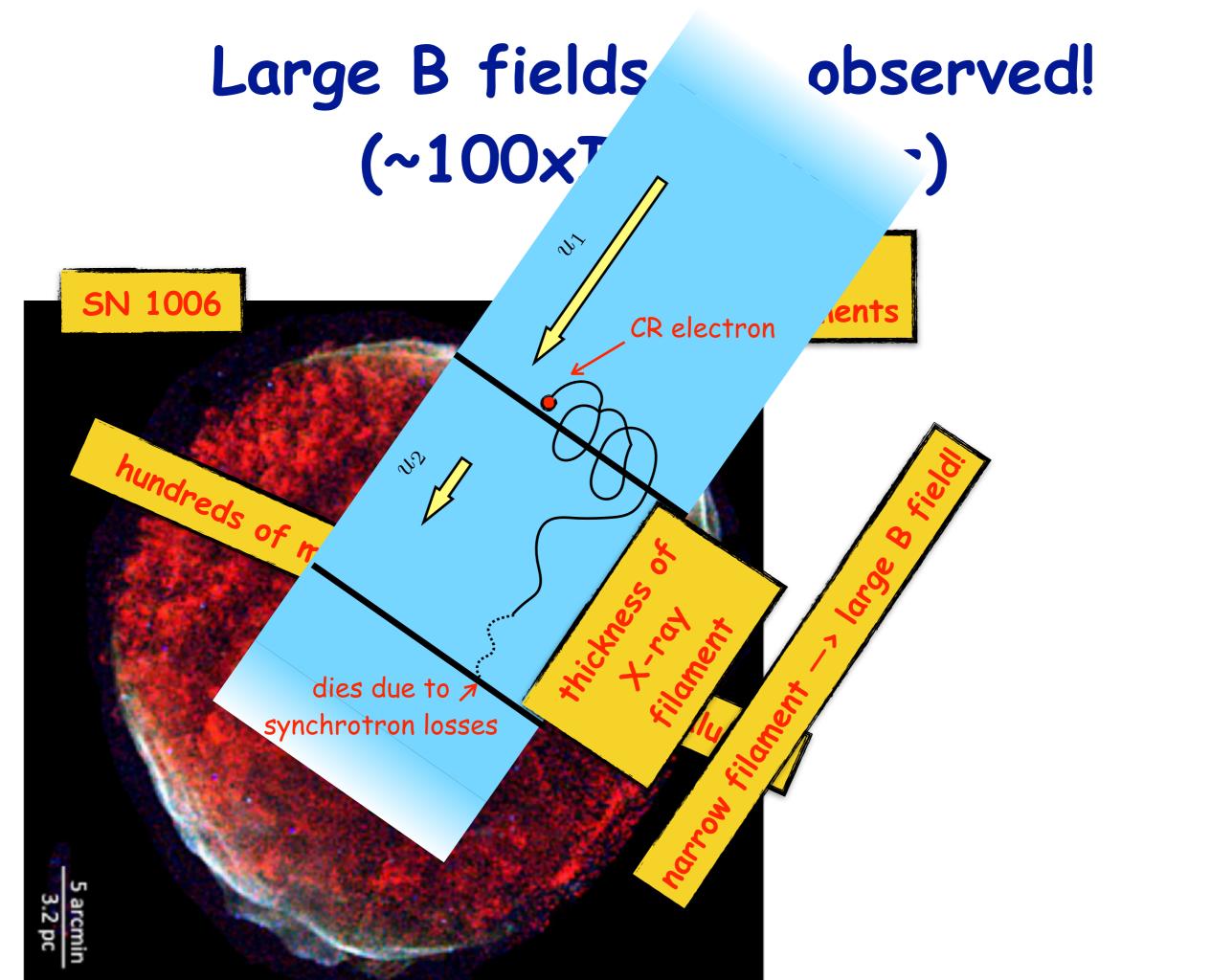
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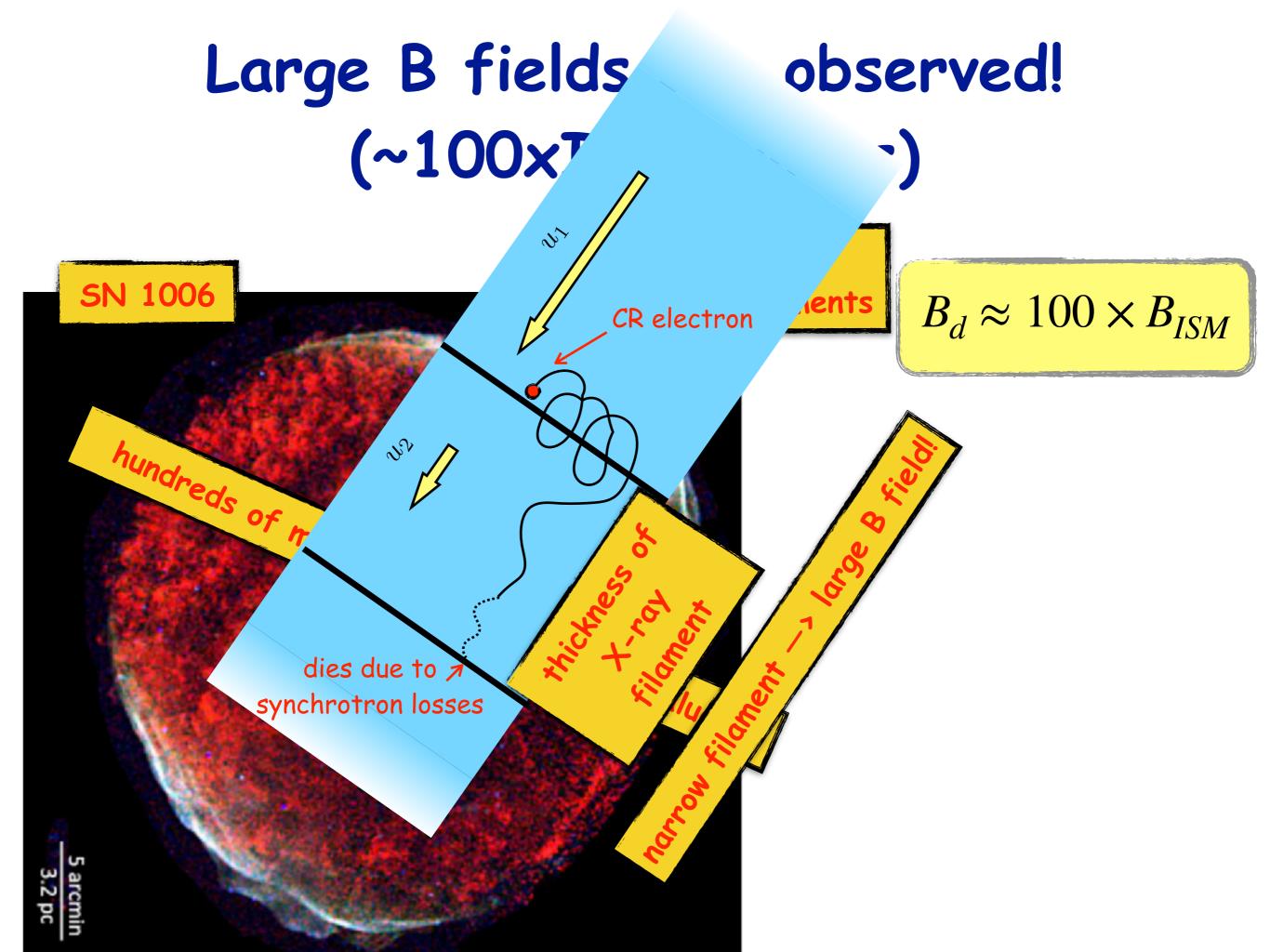


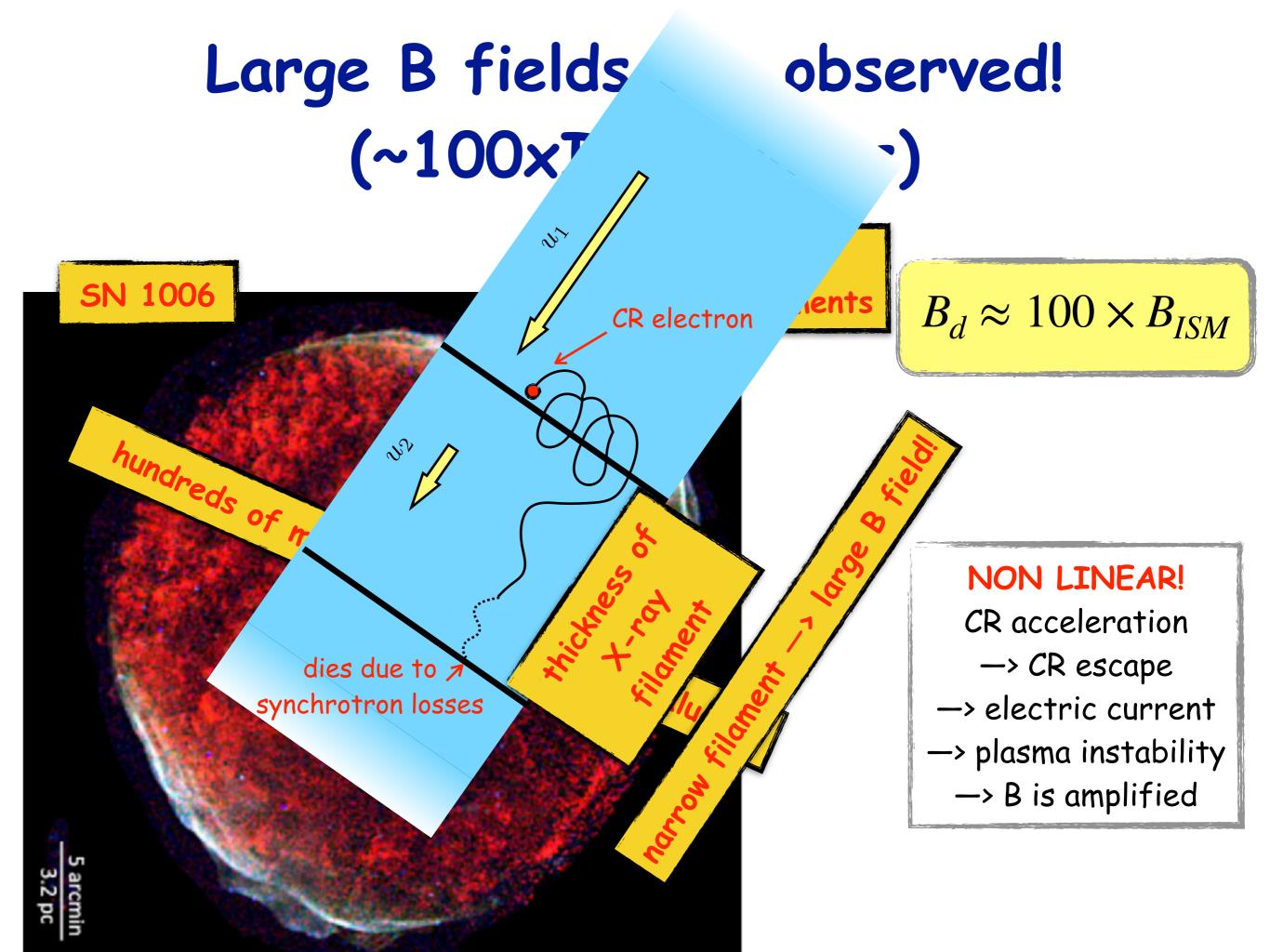




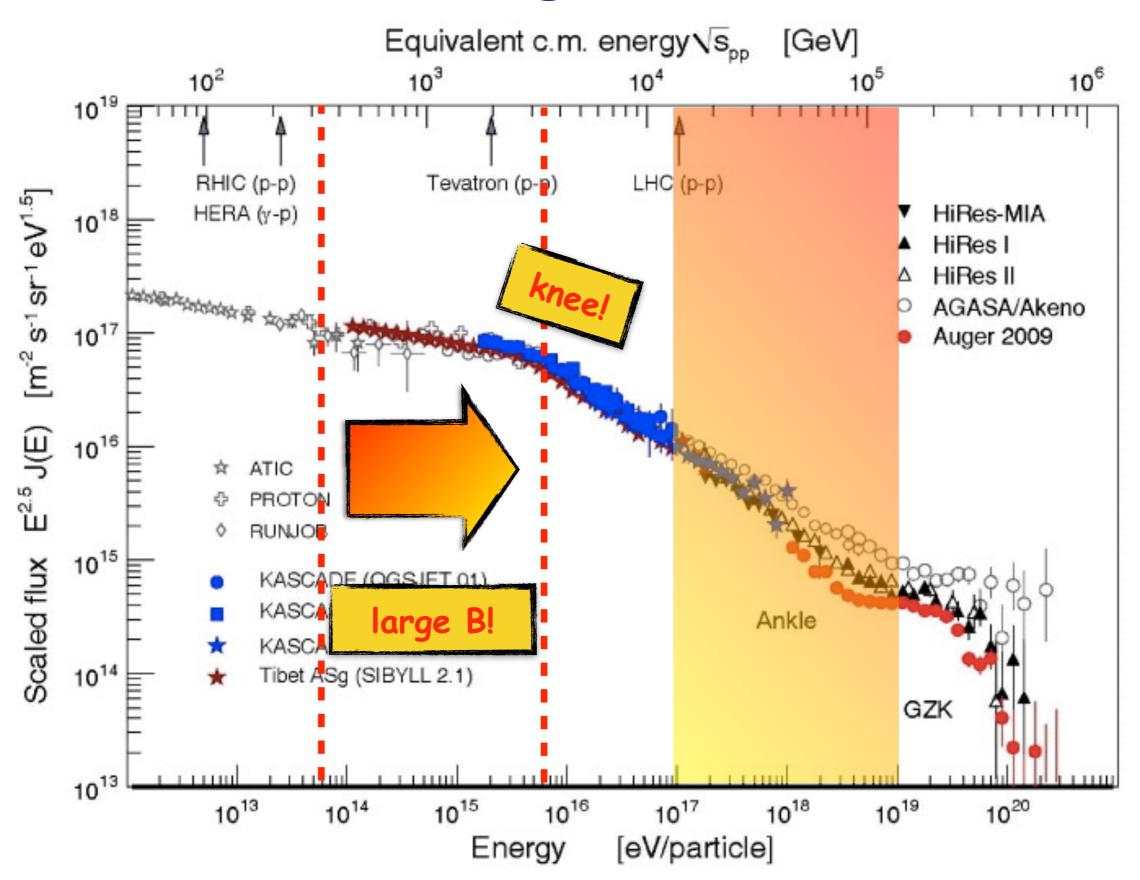




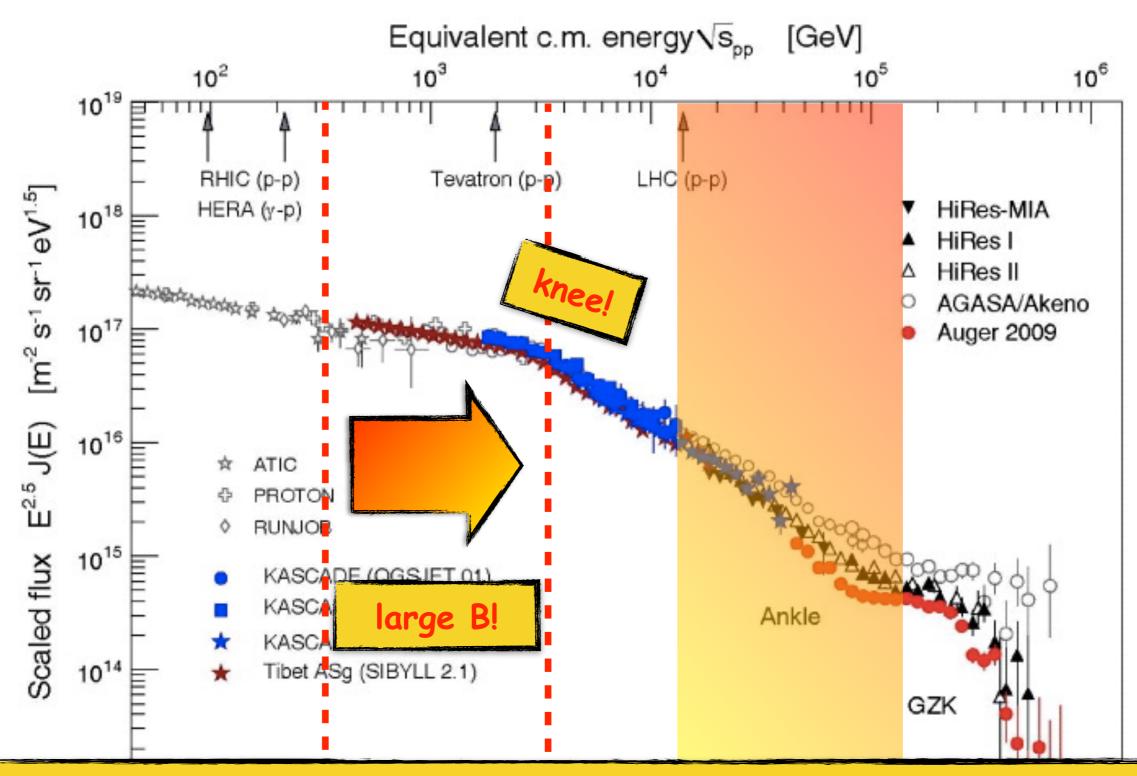




#### Getting close...

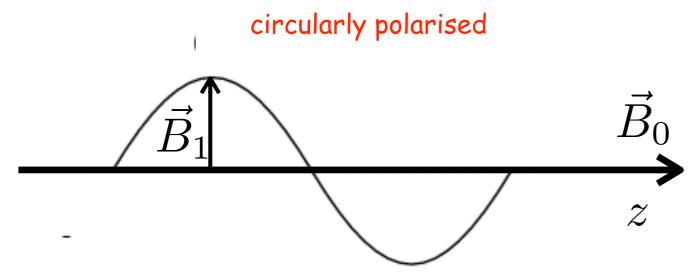


#### Getting close...



boosting  $E_{max}$  is not enough! Can SNR accelerate ENOUGH particles up there?

#### How is that? Non-resonant "Bell" instability



escaping CRs barely deflected

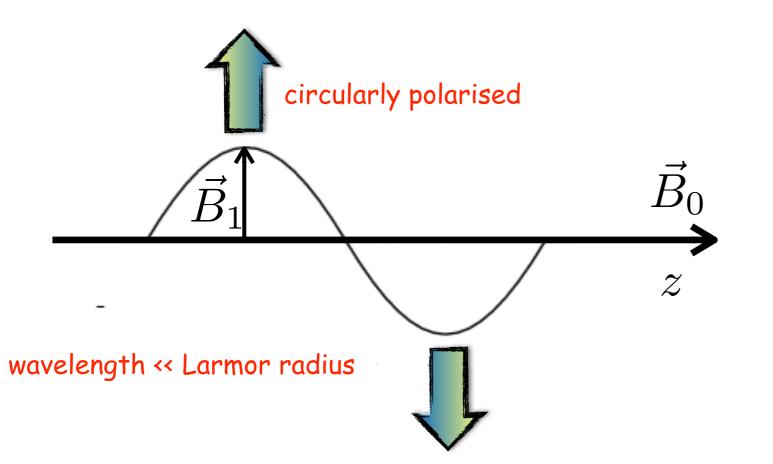
--> CR current j along B<sub>0</sub>

--> return current in the opposite direction

wavelength << Larmor radius

Bell 2004 ... Bell et al 2013

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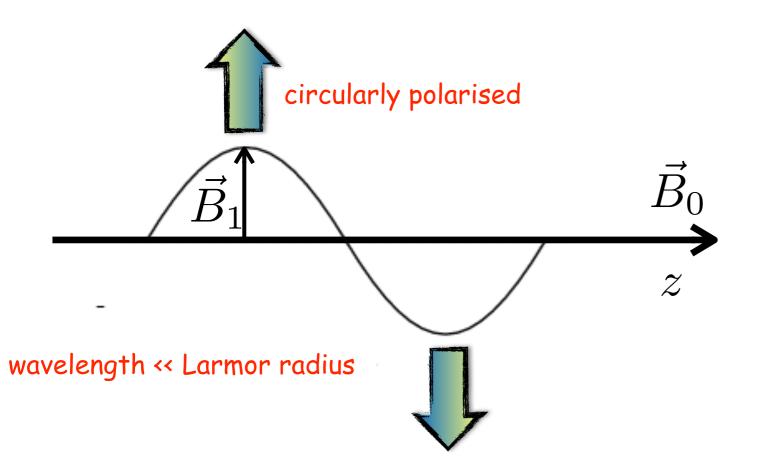
--> return current in the opposite direction

 $-ec{j} imesec{B}_1$  force acting on the plasma —> expands the helical perturbation of B

Bell 2004 ... Bell et al 2013

see also earlier works (space plasma community): Sentman+81, Winske & Leroy 84, Gary 93

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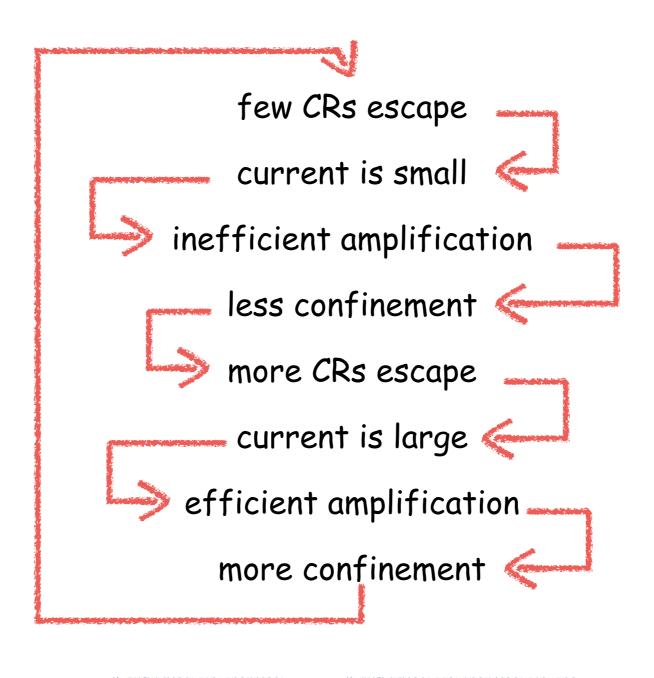
(until the size of the perturbation is of the order of the Larmor radius or magnetic tension balances it )

Bell 2004 ... Bell et al 2013

see also earlier works (space plasma community): Sentman+81, Winske & Leroy 84, Gary 93

## A non-linear (self regulating) process...

CR current-driven instability: a self-regulating mechanism



Bell 2004

Bell et al. 2013

assumption: pareticles with E < Emax are diffusively confined within the shock, while particles with E > Emax can freely escape

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spectrum at the shock -> 
$$f_0(p) = Ap^{-q}$$

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spectrum at the shock -> 
$$f_0(p) = Ap^{-q}$$
 unknown diffusive shock acceleration theory -> acceleration rate at p\_max -> j(p\_max) !!!

try a  $p_{max}$  -> determine current j -> get B -> get a new  $p_{max}$  -> adjust and restart

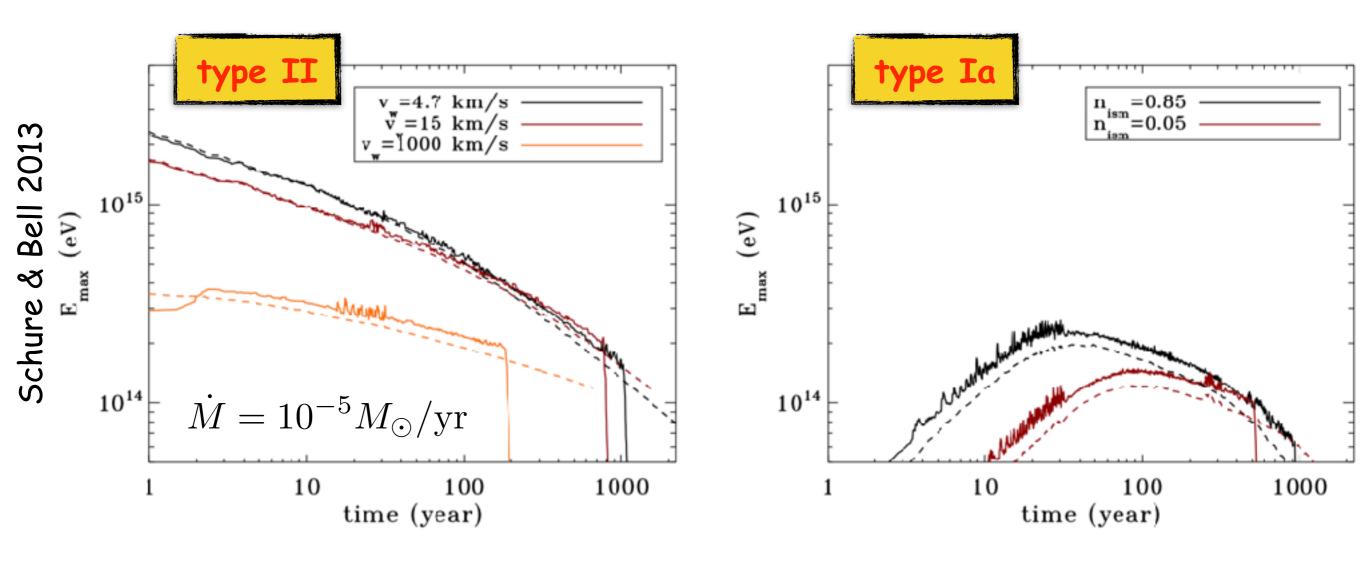
assumption: pareticles with E < Emax are diffusively confined within the shock, while particles with E > Emax can freely escape

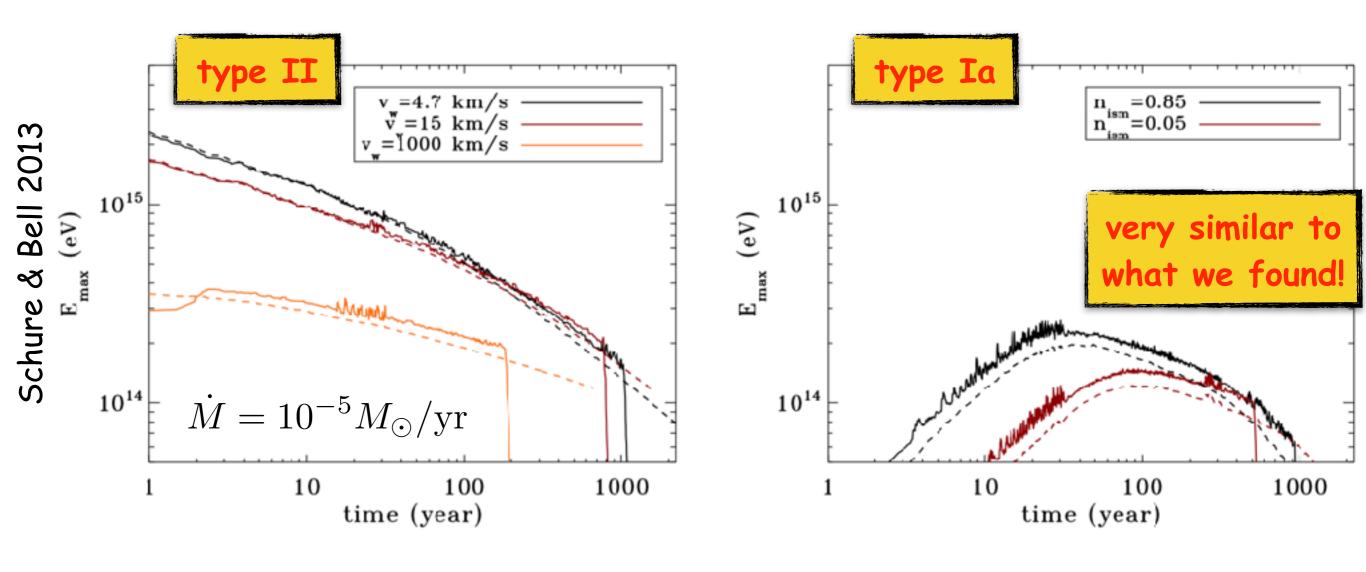
spectrum at the shock -> 
$$f_0(p) = Ap^{-q}$$
 unknown  $\swarrow$ 

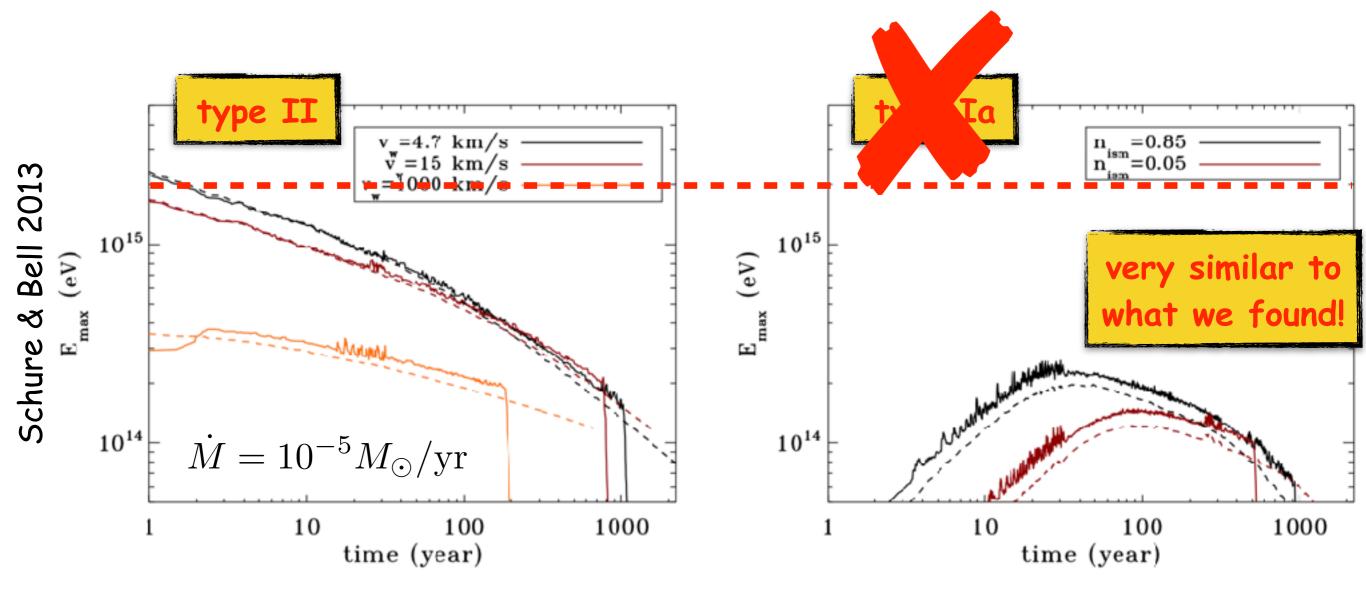
diffusive shock acceleration theory —> acceleration rate at  $p_{max}$  —>  $j(p_{max})$  !!!

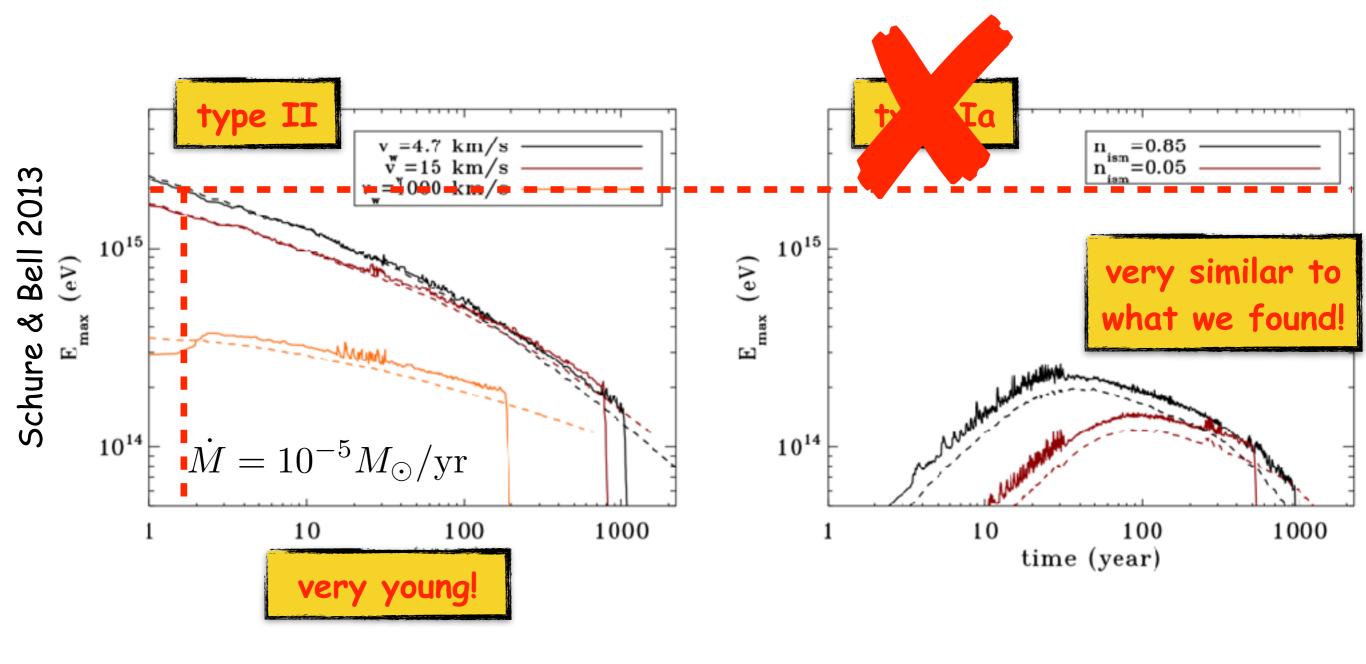
try a  $p_{max}$  -> determine current j -> get B -> get a new  $p_{max}$  -> adjust and restart

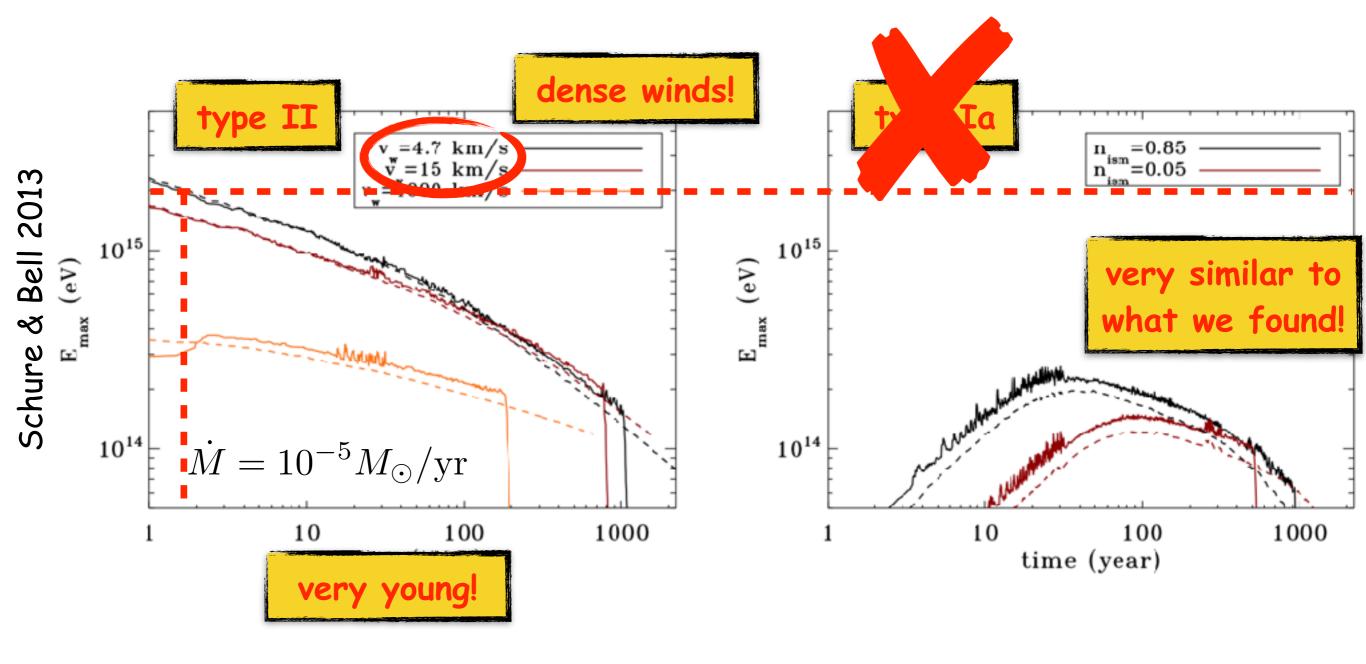
note that in the case B depends on time -> different scalings for  $E_{\text{max}}(t)$ 

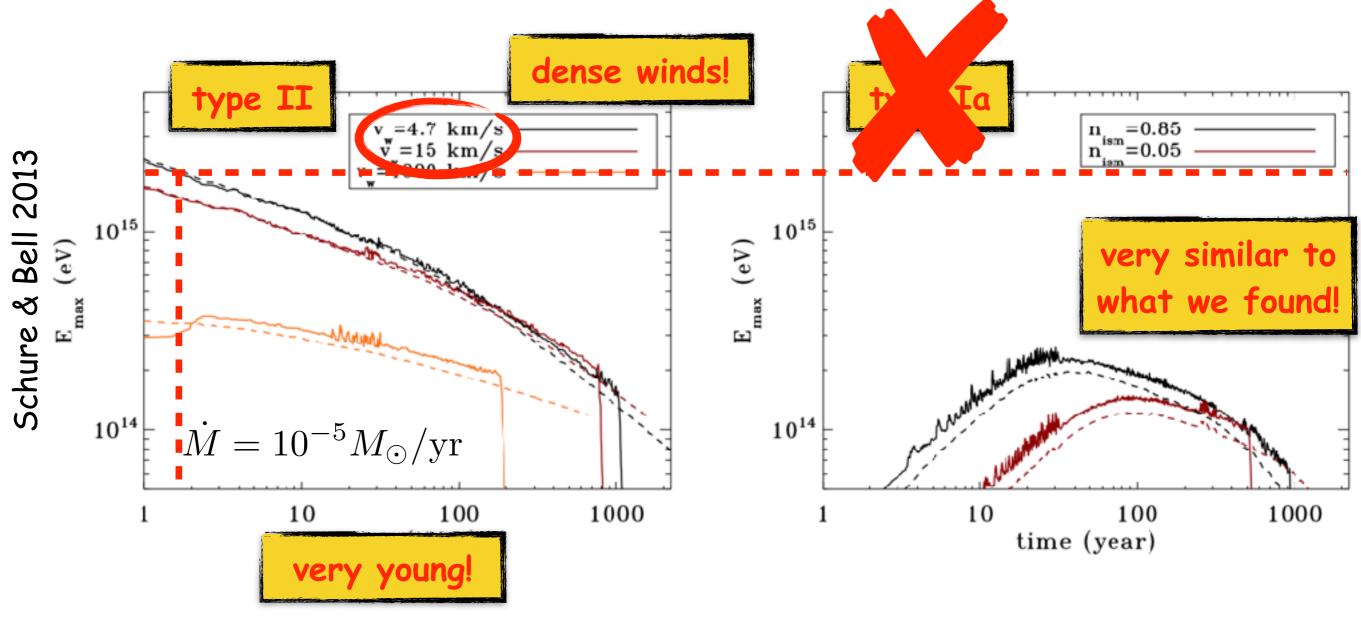






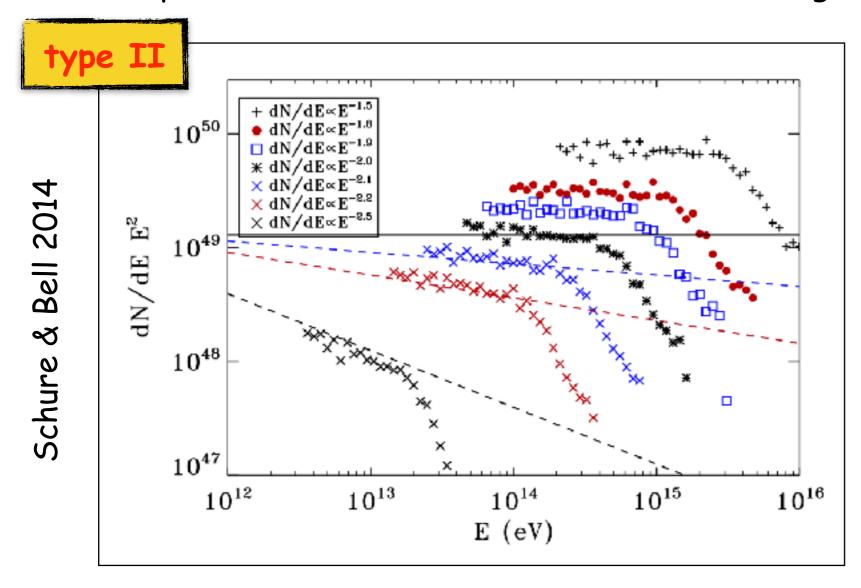




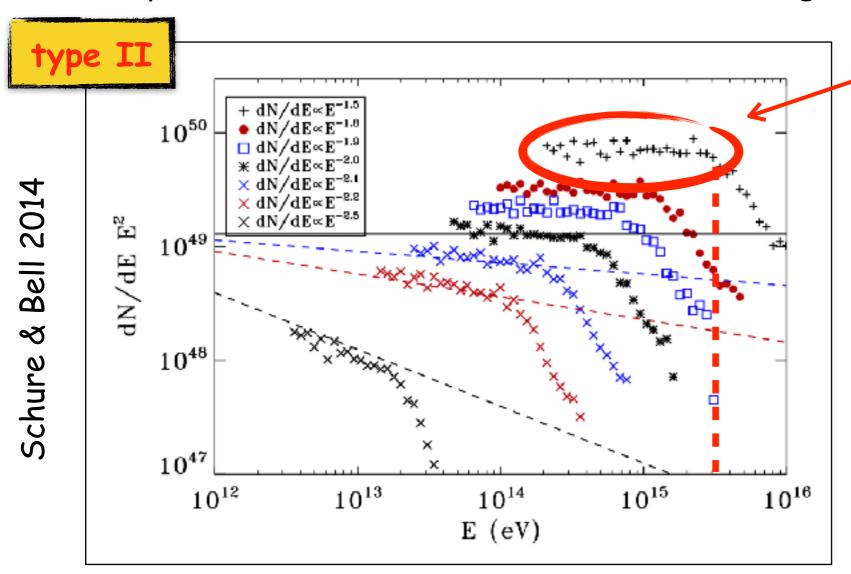


- 3 consequences:
- can SNR accelerate CRs up to the knee and beyond? —> most likely yes!
- very rare events -> # of active PeV SNRs = 0 -> enough CRs? -> maybe not?
- "knee" in the spectrum from one SNR at transition to Sedov

spectrum of CRs released in the ISM during the entire SNR life



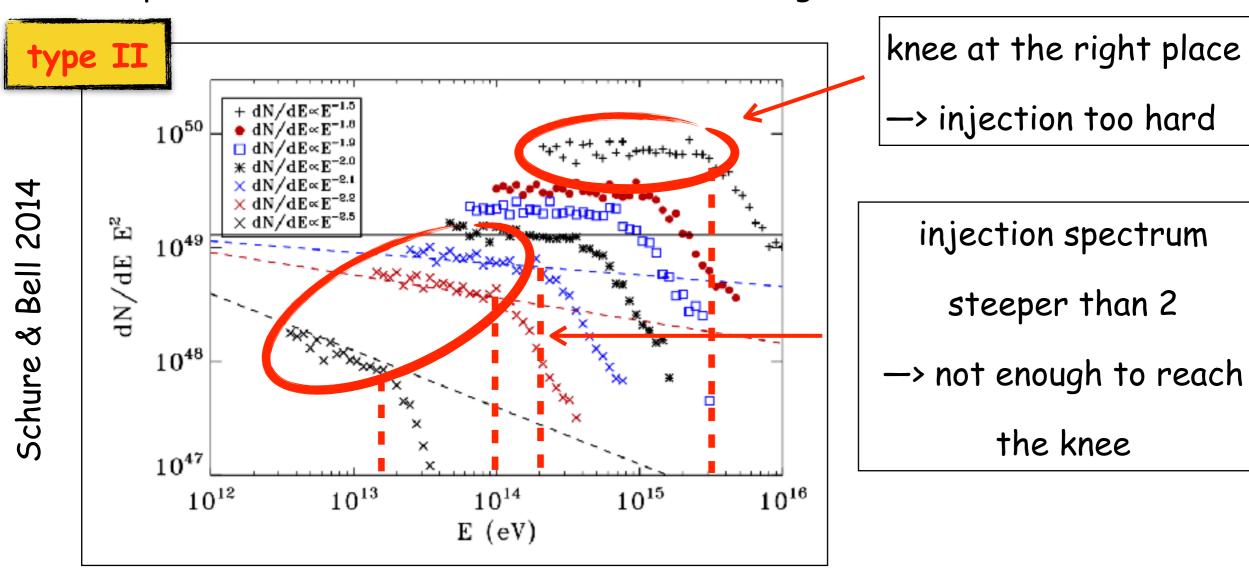
spectrum of CRs released in the ISM during the entire SNR life



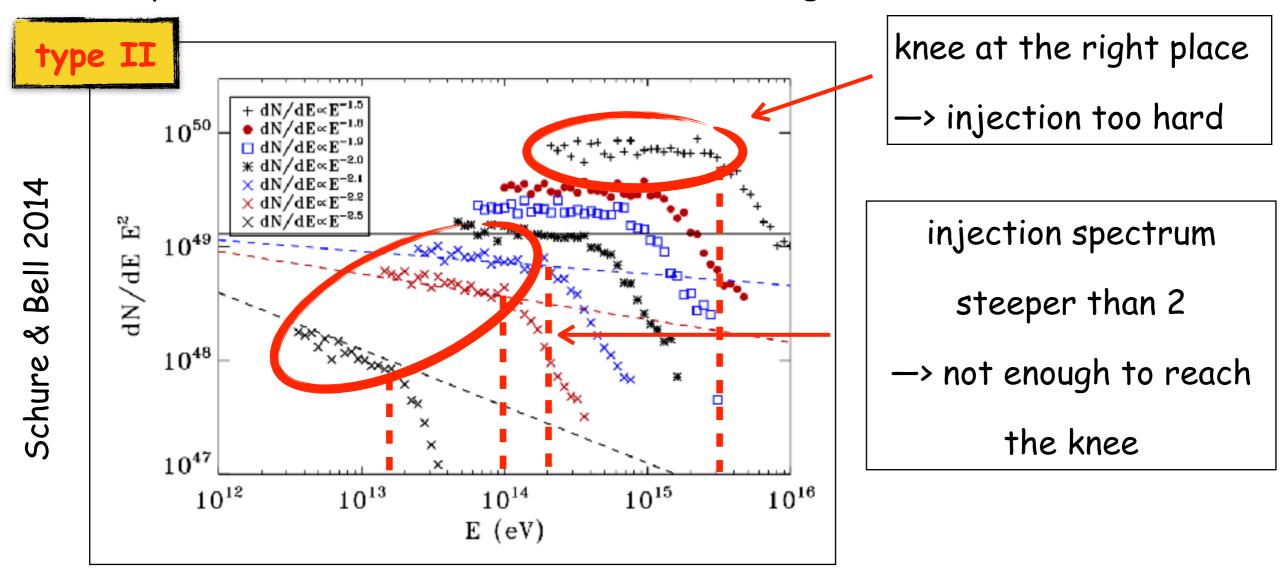
knee at the right place

-> injection too hard

spectrum of CRs released in the ISM during the entire SNR life



spectrum of CRs released in the ISM during the entire SNR life

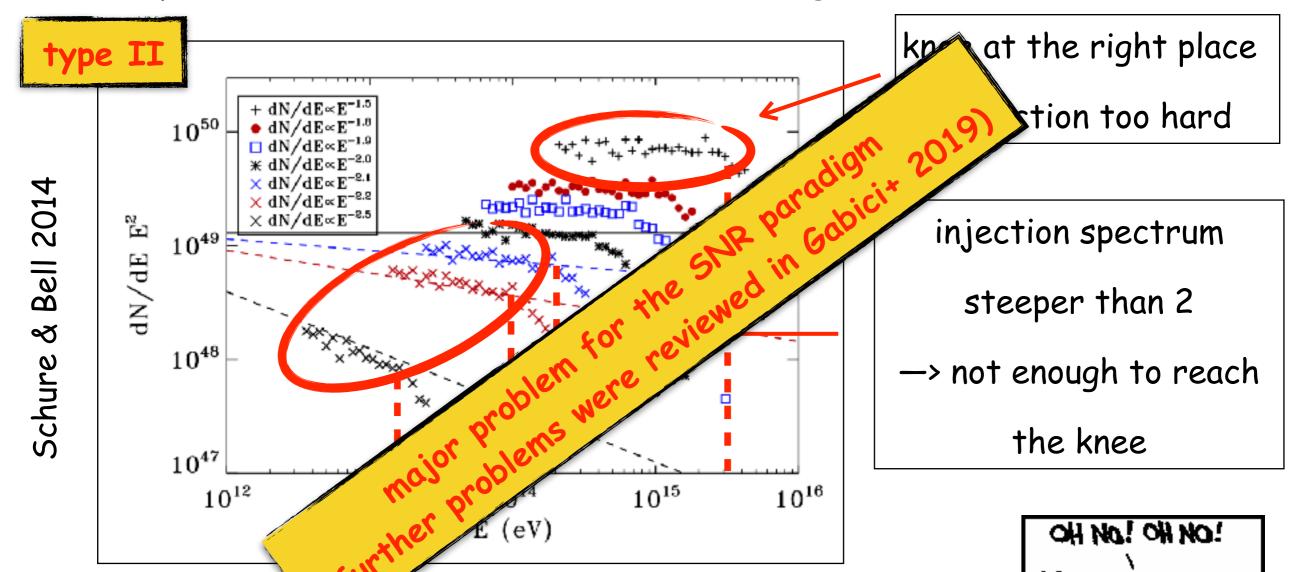


can we tune it?

It is also worth noticing that none of the types of SNRs considered here is able alone to describe the relatively smooth CR spectrum that we measure over many decades in energy. In a way, rather than being surprised by the appearance of features, one should be surprised by the fact that the CR spectrum is so regular.

(Cristofari+ 2020)

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(Cristofari+ 2020)

# How to conclude?

The bulk of the energy of cosmic rays originates from supernova explosions in the Galactic disk

Cosmic rays are diffusively confined within an extended and magnetised Galactic halo

Cosmic rays are accelerated out of the (dusty) interstellar medium through diffusive shock acceleration in supernova remnants

- The bulk of the energy of (PeV and beyond)

  from

  from accelerate ALL CRs? (PeV and beyond)

  Do SNRs accelerate ALL CRs? (PeV and beyond)

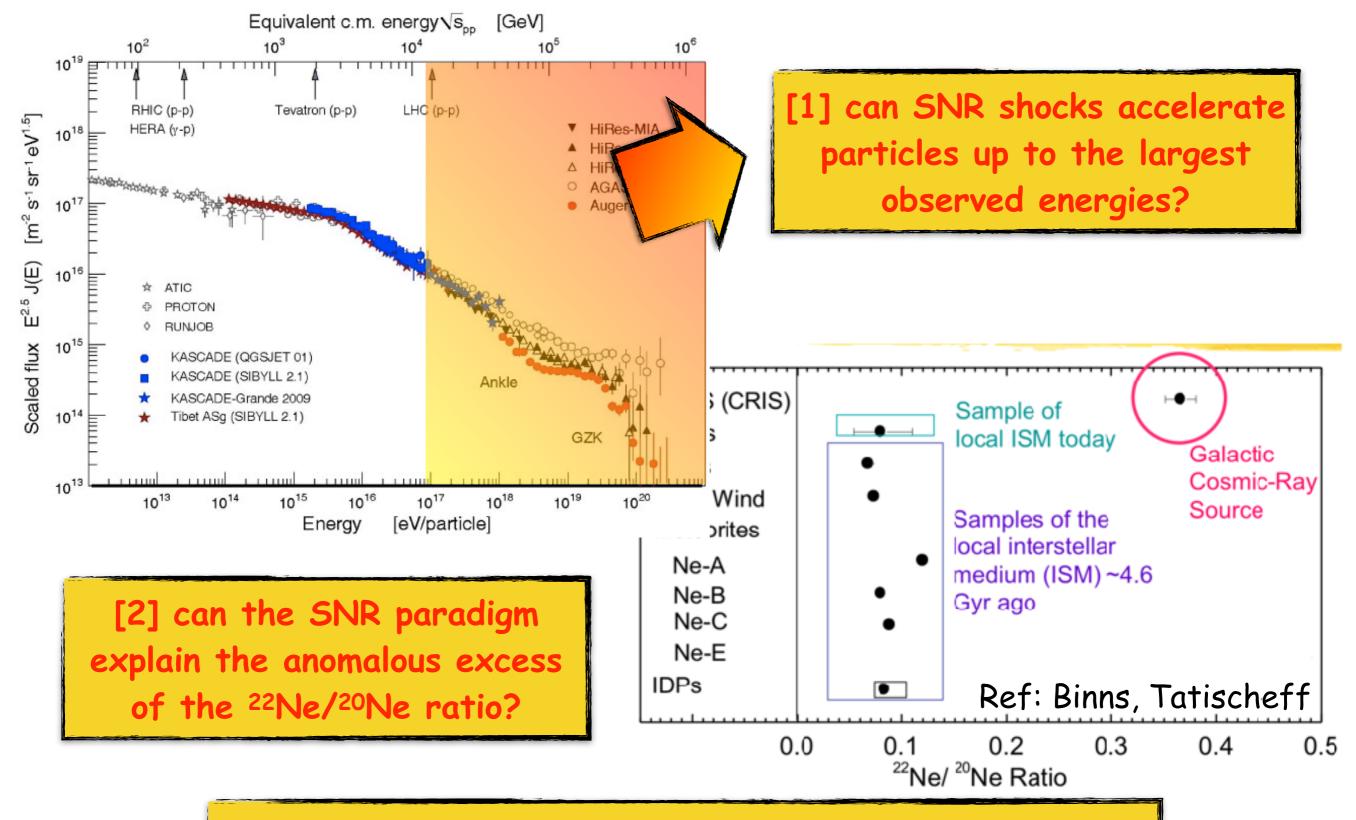
  The bulk of the energy of the control of the following the control of the con
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The bulk of the energy of (PeV and beyond)
from from accelerate ALL CRs? (PeV and beyond)
Do 5NRs accelerate ALL CRs? (PeV and beyond)
The bulk of the energy of the following in the Galactic disk

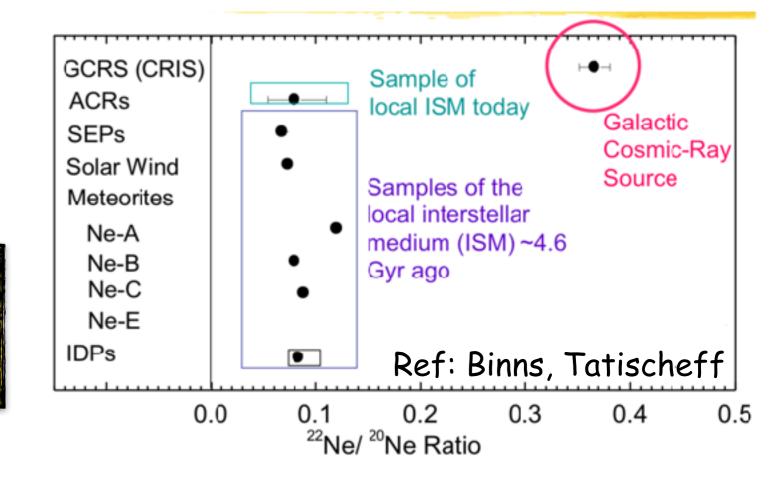
Cosmic rays are diffusively confined within an extended and magnetised Galactic halo

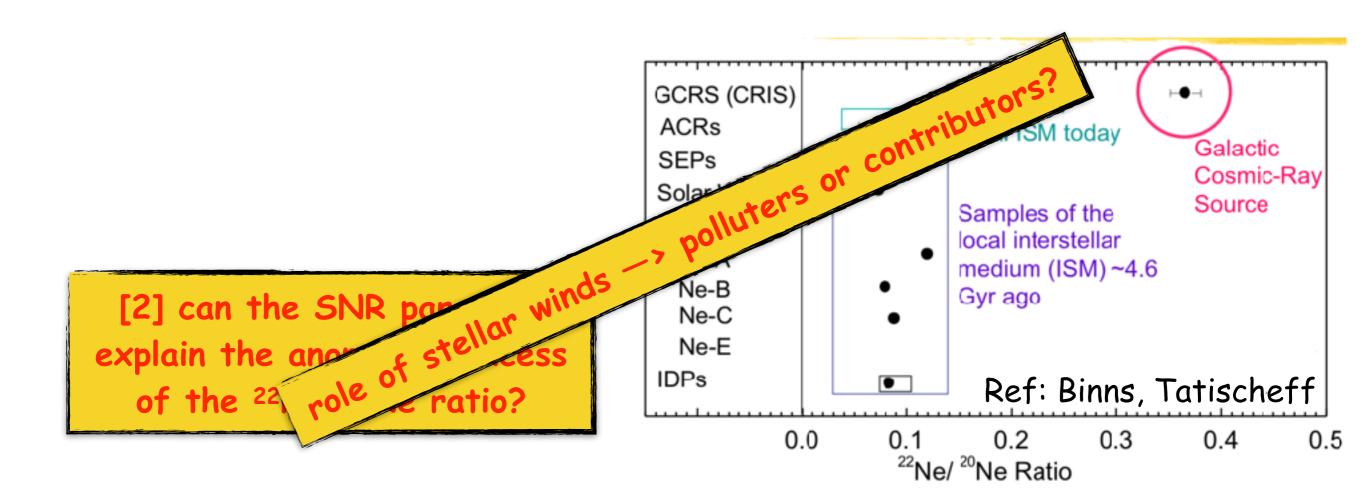
Cosmic rays are accelerated stellar winds interstellar medical accelerated about supernova remnants



[3] DSA predicts E-2 spectra, but we need E-2.2!

[2] can the SNR paradigm explain the anomalous excess of the <sup>22</sup>Ne/<sup>20</sup>Ne ratio?





The bulk of the energy of cosmic rays originates from supernova explosions in the Galactic disk

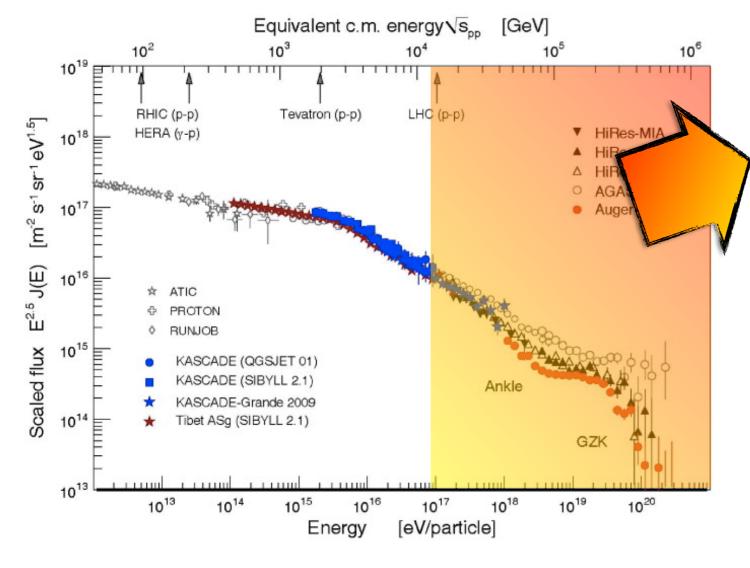
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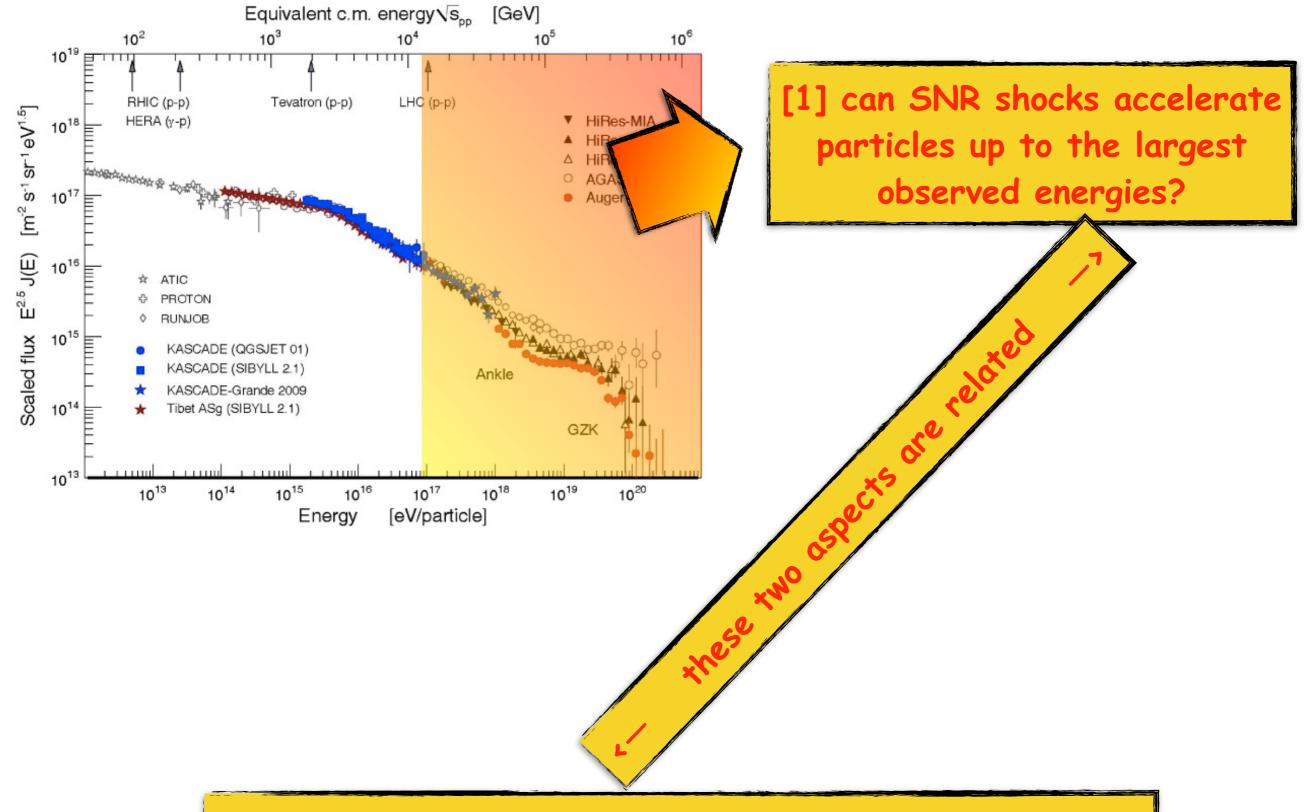
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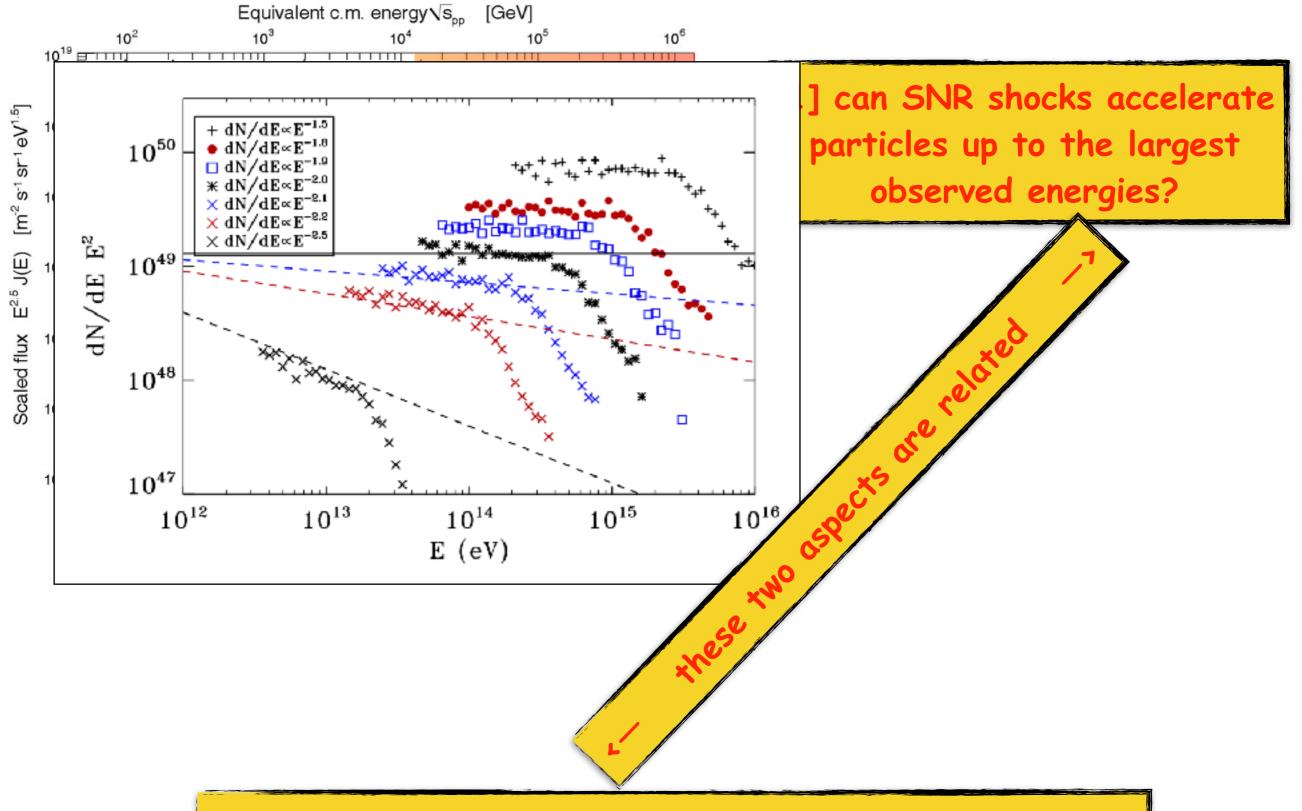
Cosmic rays are accelerated might we (dusty) interstellar medicated accelerated might we (dusty) interstellar medicated and diffusive shock accelerated might we (dusty)



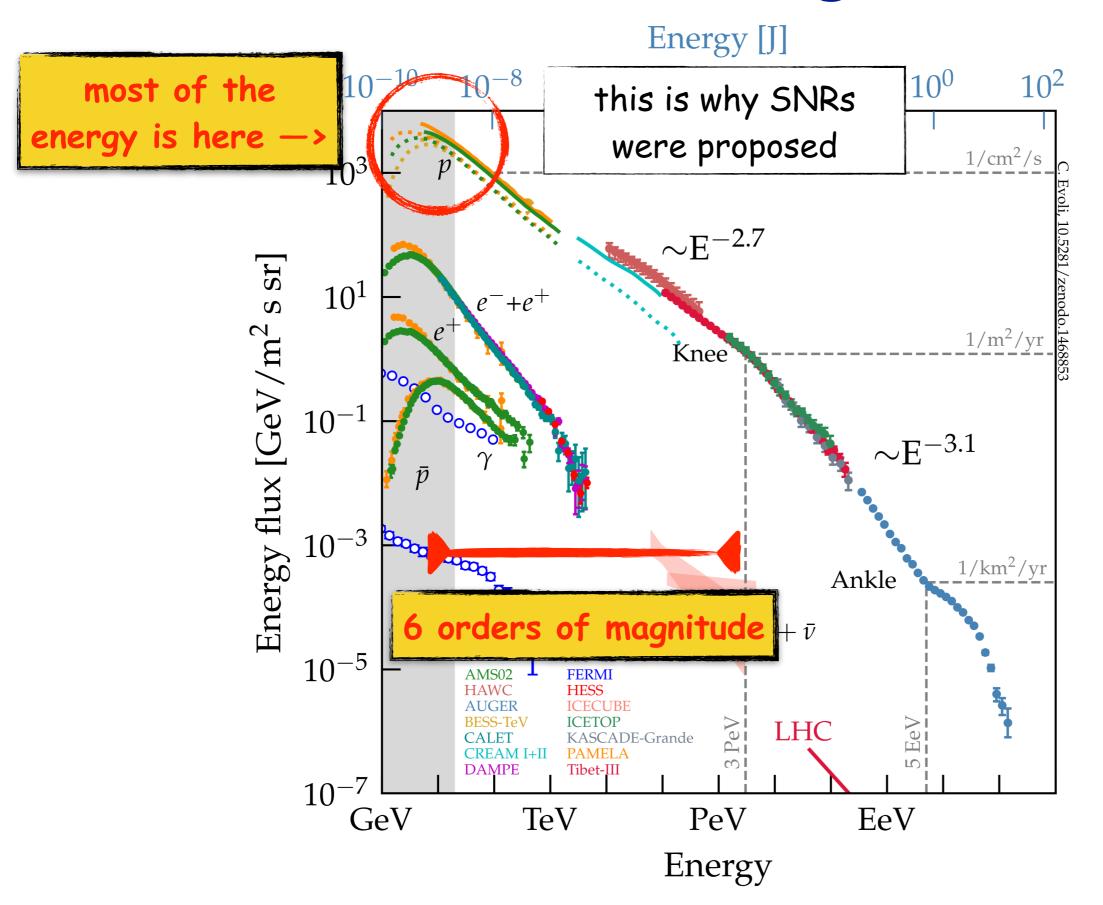
[1] can SNR shocks accelerate particles up to the largest observed energies?

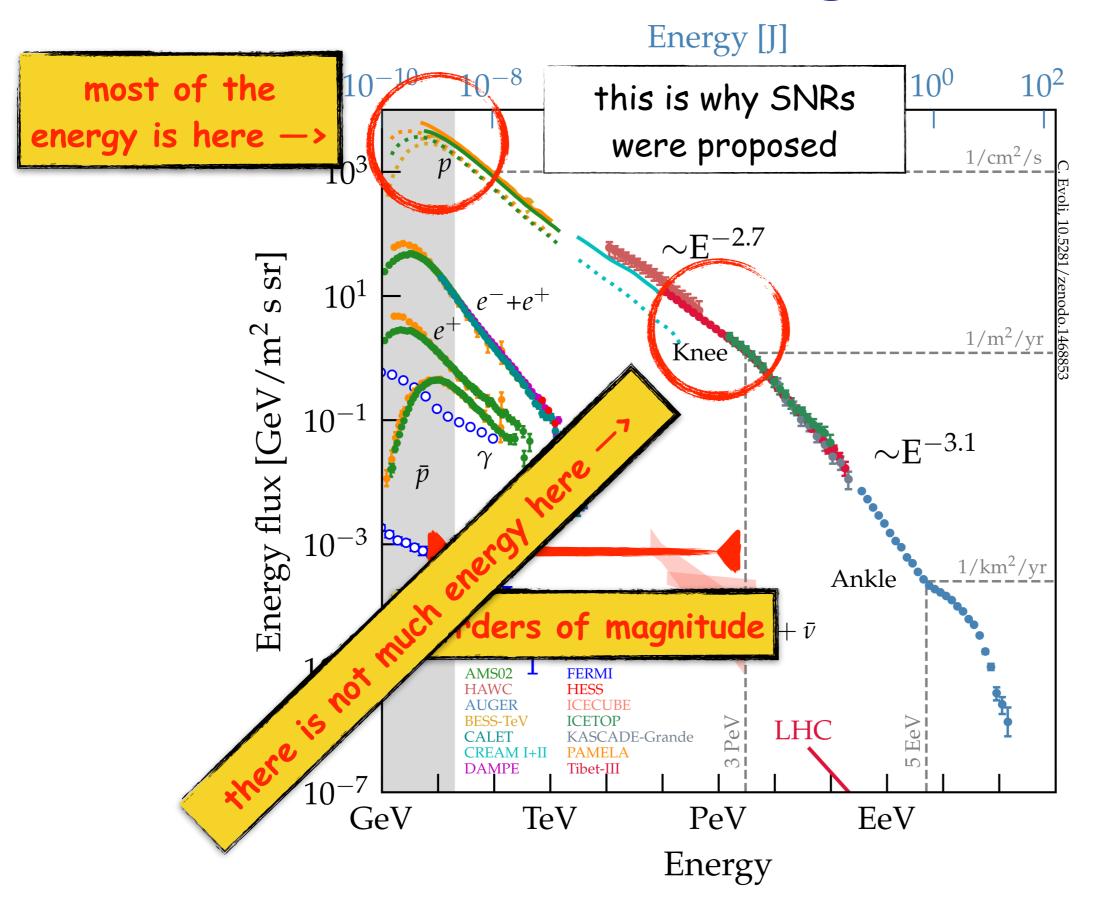


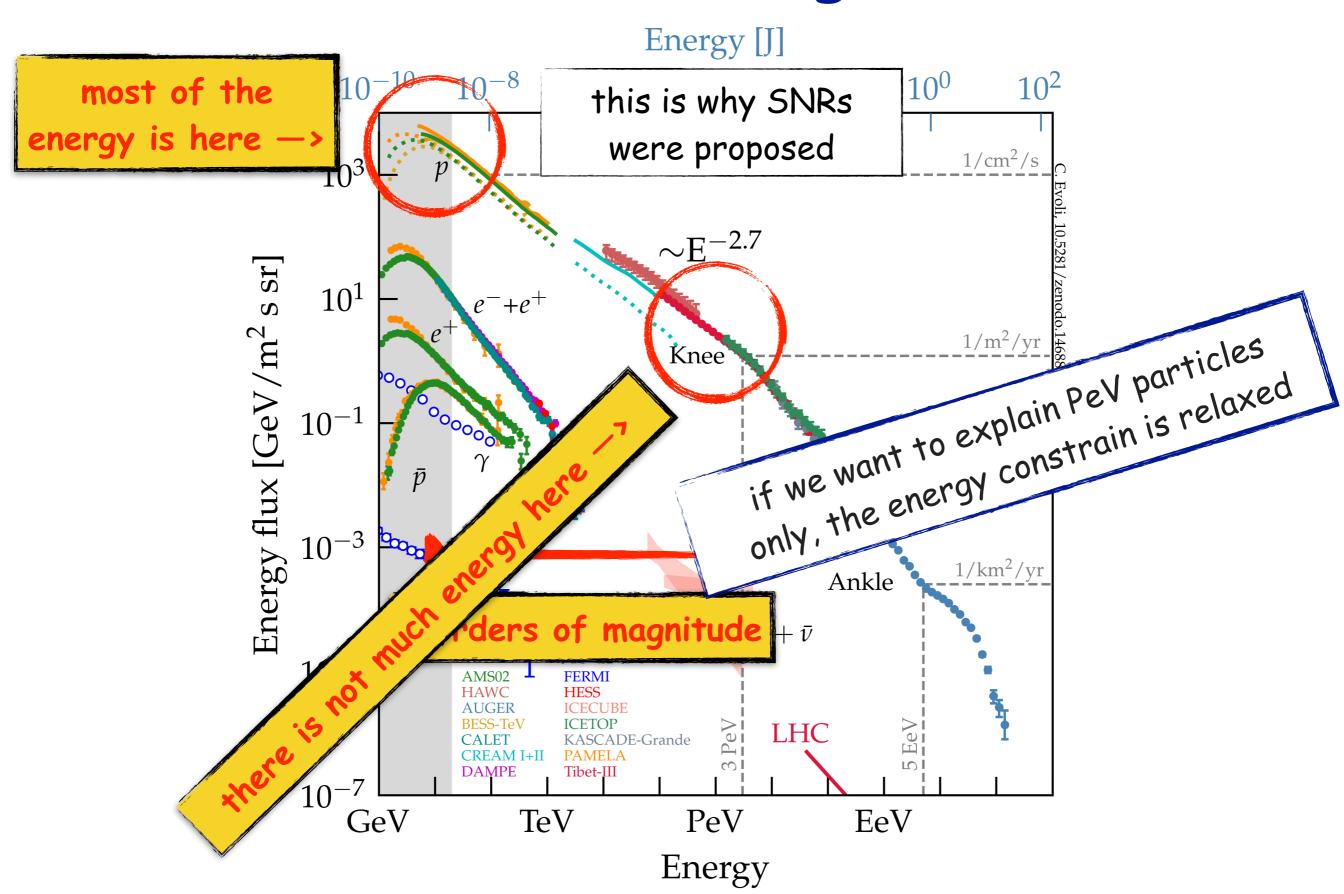
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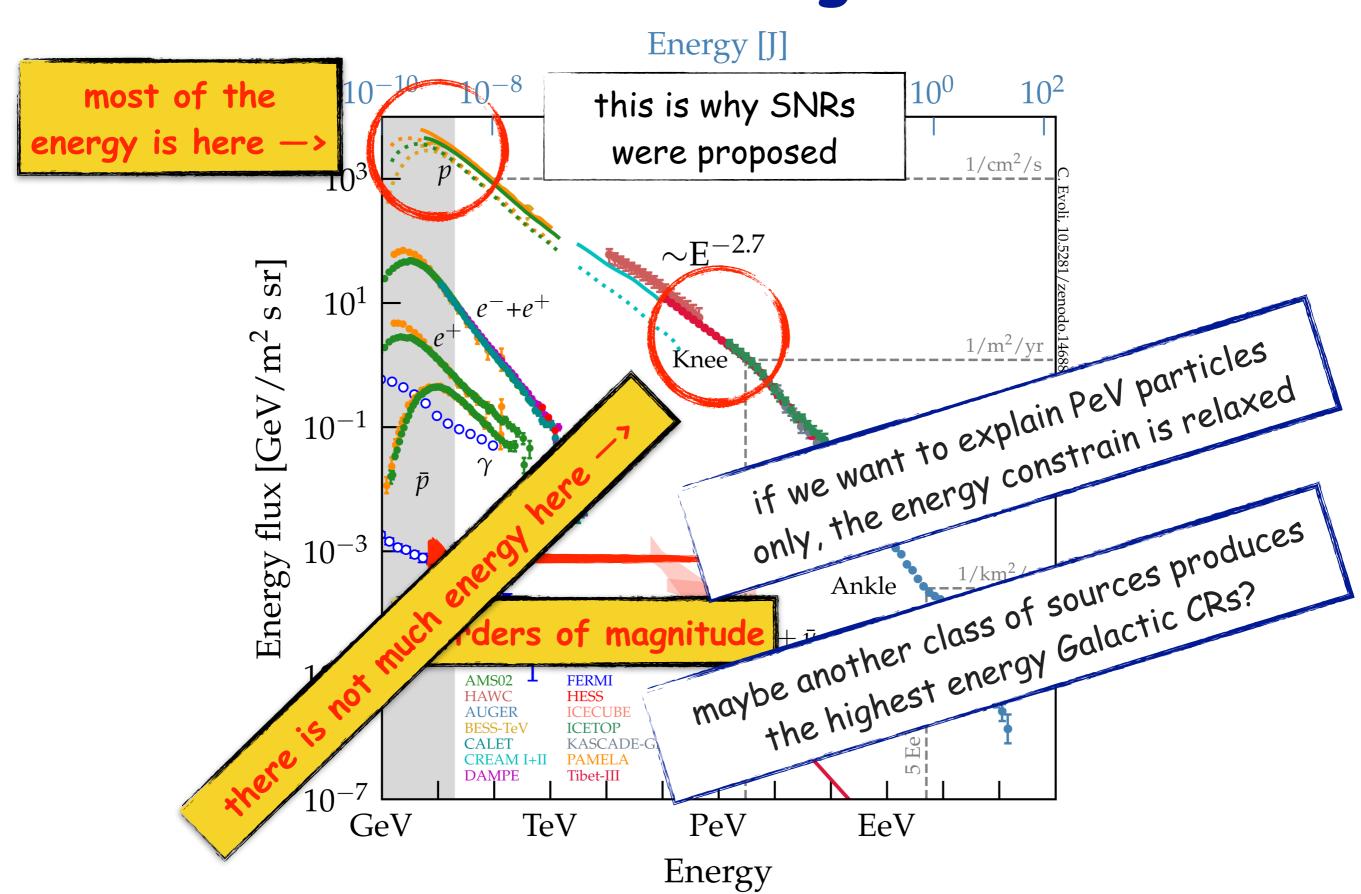


[3] DSA predicts E-2 spectra, but we need E-2.2!









The bulk of the energy of cosmic rays originates from supernova explosions in the Galactic disk

Cosmic rays are diffusively confined within an extended and magnetised Galactic halo

Cosmic rays are accelerated might we (dusty) interstellar medicated accelerated might we (dusty) interstellar medicated and diffusive shock accelerated might we (dusty)

- The bulk of the another class of sources to explain PeV and beyond another class of sources to explain PeV and beyond (rare SNRs, star clusters... most fashionable now microquasars) in the Galactic disk
  - Cosmic rays are diffusively confined within an extended and magnetised Galactic halo
  - Cosmic rays are accelerated might work interstellar medistellar winds might we (dusty) interstellar medistellar winds might work accelerated might work accelerated might work interstellar medistriction winds might work accelerated might work (dusty) interstellar medistriction winds might work (dusty) interstellar medistriction winds might we (dusty) interstellar medistriction winds might work (dusty) interstellar medistriction winds might work (dusty) interstellar medistriction winds winds might work (dusty) interstellar medistriction winds winds