



Analysis of the lateral distribution of air showers at Augers SD-array

SAT - OBERTRUBACH-BÄRNFELS, 03.-11. Okt. 2018

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$$S_{opt} = S_i^\alpha \times \left(\frac{r_{opt}}{r_i}\right)^\beta \left(\frac{r_{opt} + r_{far}}{r_i + r_{far}}\right)^\gamma \times (1 + b_{asy} \times \cos(\Psi_i))^\delta$$

$$\gamma = \gamma_0 + \sum_{\chi} \sum_{k=1}^{\infty} [\gamma_{\chi,k} \times \chi^k]$$

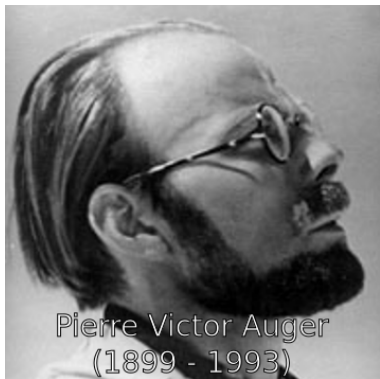
$$\beta = \beta_0 + \sum_{\chi} \sum_{k=1}^{\infty} [\beta_{\chi,k} \times \chi^k]$$

$$S(r) = S_{opt} \times \left(\frac{r}{r_{opt}}\right)^\beta \times \left(\frac{r + r_{700}}{r_{opt} + r_{700}}\right)^{\beta + \gamma}$$

$$\mathcal{D}(S, \mu) = -2 \log \left(\frac{\mathcal{L}(S, \mu)}{\max_{\mu} \{\mathcal{L}(S, \mu)\}} \right)$$

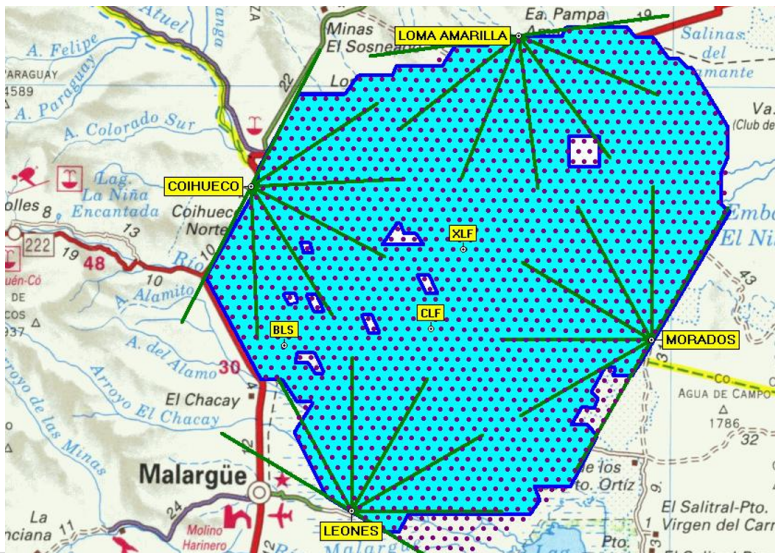
$$\mathcal{L}(S, \mu) = \delta(S) \times \left(1 + \mathcal{P}_{ring}(\mu) \left(\frac{N(S, \mu, \sigma)}{\frac{1}{2} \left[1 + \operatorname{erf} \left(\frac{\mu}{\sqrt{2}\sigma} \right) \right] - 1} \right) \right)$$

About the Pierre Auger Observatory



- area of 3000km^2 near the city of Malargüe in Mendoza Province
- hybrid detector of over 1600 water cherenkov detectors, 24 fluorescence telescopes + 150 radio antennas & Upgrades

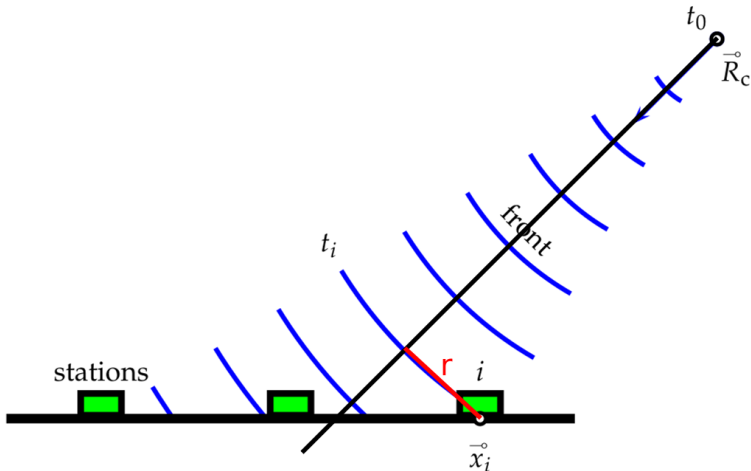
Map of the Detector Site



Pictures of SD-tanks

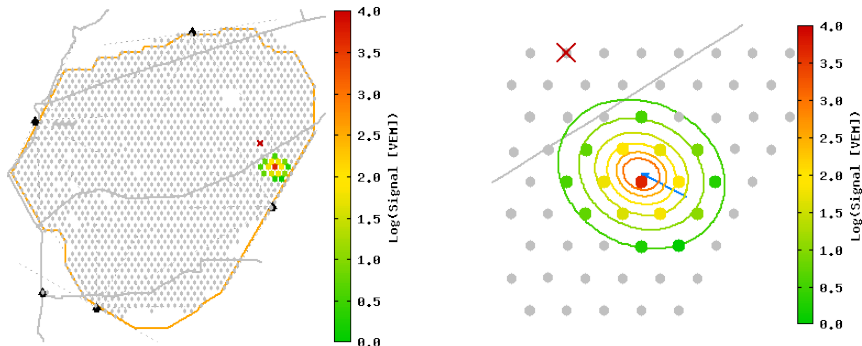


What's the Setting?



properties

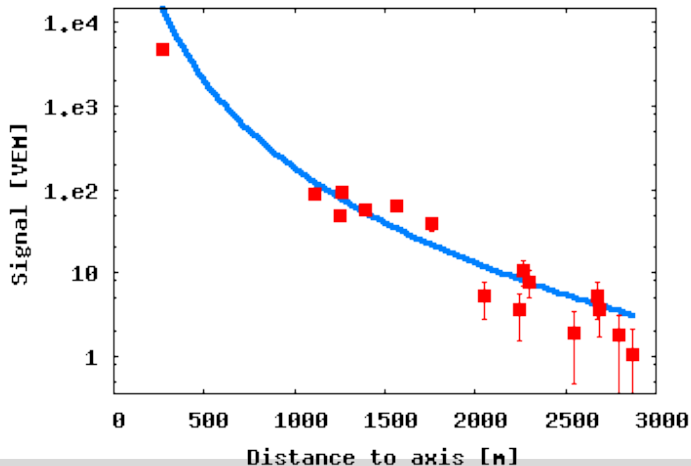
• ID: 32112000 (26.03.2015) • $E = 38.8 \pm 2.0 \text{EeV}$ • $\theta = 34.5 \pm 0.2 \text{deg}$



Auger Data

properties

- ID: 32112000 (26.03.2015) • $E = 38.8 \pm 2.0 \text{ EeV}$ • $\theta = 34.5 \pm 0.2 \text{ deg}$



1. implemented state of reconstruction
2. goals of my analysis
3. preliminary results

describes the **lateral distribution of signal S**

$$S(r) = S_{\text{opt}} \times \left(\frac{r}{r_{\text{opt}}} \right)^{\beta} \times \left(\frac{r + r_{700}}{r_{\text{opt}} + r_{700}} \right)^{\beta + \gamma} \quad (1)$$

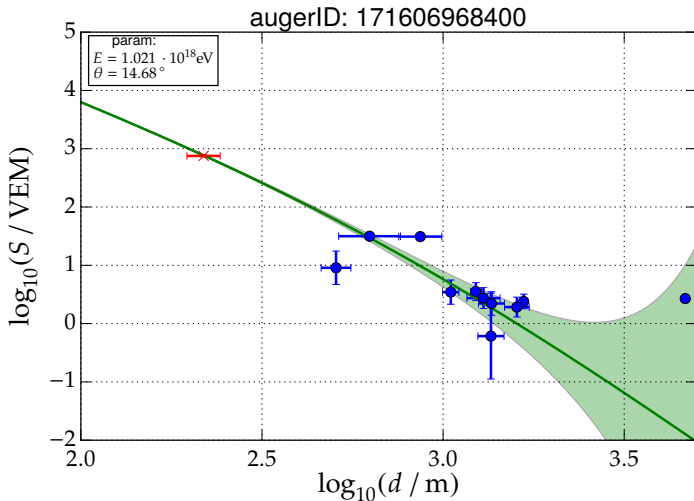
and uncertainty

$$\sigma_S(\theta) = \underbrace{[0.32 + 0.42 \sec(\theta)]}_{f_S(\theta)} \times \sqrt{S} \quad (2)$$

energy estimator

$$E \propto S \quad (3)$$

Plot of the LDF in log-log-scale



Overfitted Slope Parameters

$$\begin{aligned}\beta = & (-3.720 + 0.0967s) & (4) \\ & +(+1.740 - 0.2420s) \times \sec(\theta) \\ & +(-0.274 + 0.0349s) \times \sec^2(\theta)\end{aligned}$$

and

$$\begin{aligned}\gamma = & (-1.870 - 0.1830s) & (5) \\ & +(+0.490 - 0.0650s) \times \frac{1}{a+1} \\ & -0.272(\cos(\theta))^{4.64} \times \frac{1}{\exp[18.01(s-1.95)] + 1}\end{aligned}$$

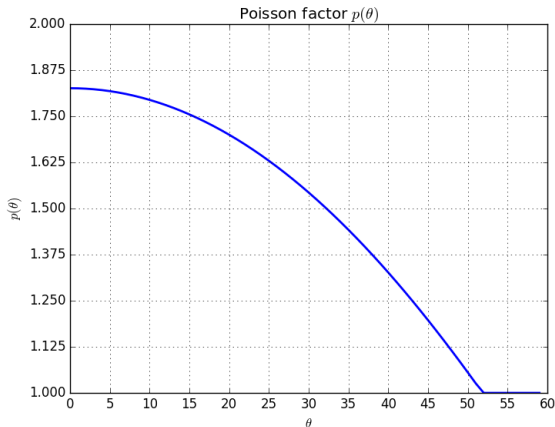
with

$$a = \exp \left[(19.6 - 2.10s) \times (\cos^2(\theta) - (0.483 + 0.005s)) \right] \quad (6)$$

Particle ↔ Signal

Signals S dependence on number of particles n via *Poisson factor* p :

$$S = p \times n \quad (7)$$



Maximum Likelihood Function \mathcal{L}

Likelihood of LDF-expectation μ_i against effective number of particles n_i per tank i :

$$\mathcal{L} = \prod_i [f_{\text{Zero}} \times f_{\text{Poi}} \times f_{\text{Std}} \times f_{\text{Sat}}] (n_i, \mu_i) \quad (8)$$

with

$$\text{Zero Signal} : f_{\text{Zero}} = \sum_{n=0}^{n_{\text{th}}} f_{\text{Poi}} (n, \mu_i) \quad (9)$$

$$\text{small Signal} : f_{\text{Poi}} = \frac{\mu_i^{n_i} e^{-\mu_i}}{n_i!} \quad (10)$$

$$\text{large Signal} : f_{\text{Std}} = \frac{1}{\sqrt{2\pi}\sigma_i} \exp\left(-\frac{(n_i - \mu_i)^2}{2\sigma^2}\right) \quad (11)$$

$$\text{Saturated Stations} : f_{\text{Sat}} = \int_{n_i}^{\infty} f_{\text{Std}} (n, \mu_i) dn \quad (12)$$

renew

- inspect new LDF parameterizations
- renew likelihood \mathcal{L}_{new}

introduce

- trigger probability $\mathcal{P}_{\text{trig}}(\mu)$
- azimuth Ψ_i asymmetry

What's the Asymmetry?

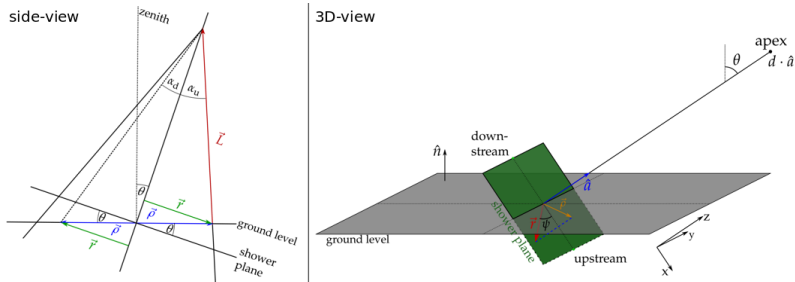


Figure: from: "*Asymmetries of the Lateral Distribution of Particles on the Ground*", by L.Armbruster, BachelorThesis June 2018, IKP at KIT

NKG-type LDF:

$$S_i = S_{\text{opt}} \times \left(\frac{r_i}{r_{\text{opt}}} \right)^\beta \left(\frac{r_i + r_{\text{far}}}{r_{\text{opt}} + r_{\text{far}}} \right)^\gamma \times (1 + b \tan(\theta) \cos(\Psi)) \quad (13)$$

new parameterizations

$$\beta = \beta_0 + \sum_{\chi} \sum_{k=1}^{\infty} [\beta_{\chi,k} \times \chi^k], \quad \gamma = \gamma_0 + \sum_{\chi} \sum_{k=1}^{\infty} [\gamma_{\chi,k} \times \chi^k] \quad (14)$$

Normalized and simplified maximum likelihood function:

$$\mathcal{L}_{\text{new}}(\mathbf{S}, \mu) = \overbrace{\delta(\mathbf{S}) \times [1 - \mathcal{P}_{\text{trig}}(\mu)]}^{\text{zero}} + \overbrace{\mathcal{P}_{\text{trig}}(\mu) \mathcal{N}(\mathbf{S}; \mu, \sigma)}^{\text{signal}} \quad (15)$$

Preliminary Results and New Approaches

results

- ✓ implement new NKG-type LDF
- X find new likelihood and compare deviances
- X introduce trigger probability
- X introduce asymmetry

new approaches

- test different likelihood with ToyMC
- compare different triggers & combined trigger probability
- define asymmetry parameter for different radii on real data
- ...